

CompSci 161
Winter 2023 Lecture 22:
Greedy Algorithms On Trees

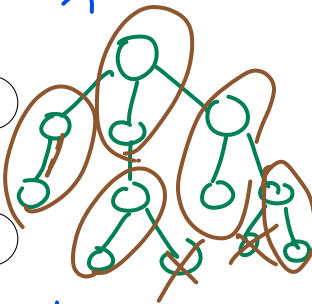
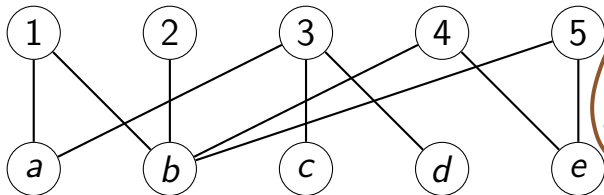
Maximum Matching

Can every puppy be adopted?

no

4

Tree:



c, d : only one house

but two dogs

max one dog per house.

Maximum Matching

- ▶ In general: complicated algorithms, solvable
- ▶ In a tree: less complicated algorithm, solvable

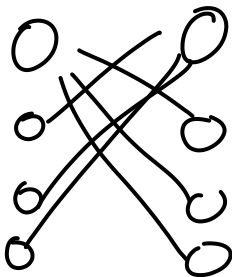
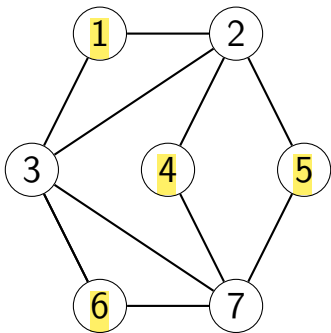
Tree: $n-1$ edges $\sum \deg(v) = 2(n-1)$

base: must be a leaf.
 $n \leq 1$, return zero

Leaf First: pick a leaf. match w/ neighbor
 remove both. Recurse on all components

Independent Set

Find an independent set of size 4 in this graph:



Max Independent Set On Tree

Coming Soon

- ▶ Tonight!
 - ▶ Interval Coloring
 - ▶ Wrapping up Greedy Algorithms
- ▶ Monday in lecture
 - ▶ Closest pair of points D&C
- ▶ Monday evening
 - ▶ Dynamic Programming Review
 - ▶ Problems TBD