

CompSci 161  
Winter 2023 Lecture 22:  
Greedy Algorithms On Trees

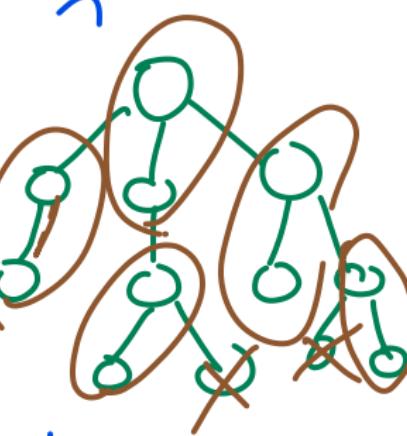
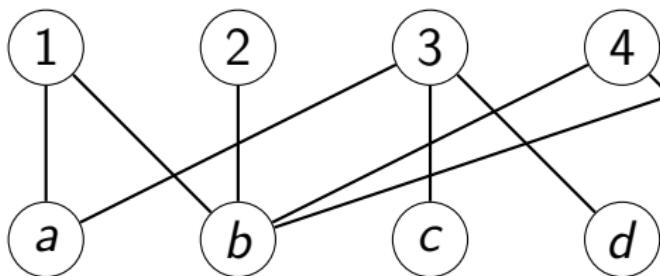
# Maximum Matching

Can every puppy be adopted?

NO

"

Tree:



$c, d$  : only one house

but two dogs

max one dog per house.

# Maximum Matching

- ▶ In general: complicated algorithms, solvable
- ▶ In a tree: less complicated algorithm, solvable

Tree:  $n-1$  edges  $\sum \delta(v) = 2(n-1)$

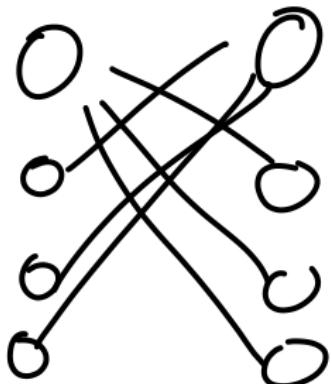
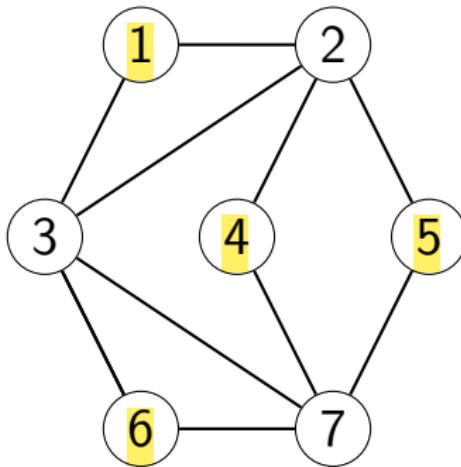
must be a leaf.

base:  $n \leq 1$ , return zero

Leaf First: pick a leaf. match w/ neighbor  
remove both. Recurse on all components

# Independent Set

Find an independent set of size 4 in this graph:



# Max Independent Set On Tree

# Coming Soon

- ▶ Tonight!
  - ▶ Interval Coloring
  - ▶ Wrapping up Greedy Algorithms
- ▶ Monday in lecture
  - ▶ Closest pair of points D&C
- ▶ Monday evening
  - ▶ Dynamic Programming Review
  - ▶ Problems TBD