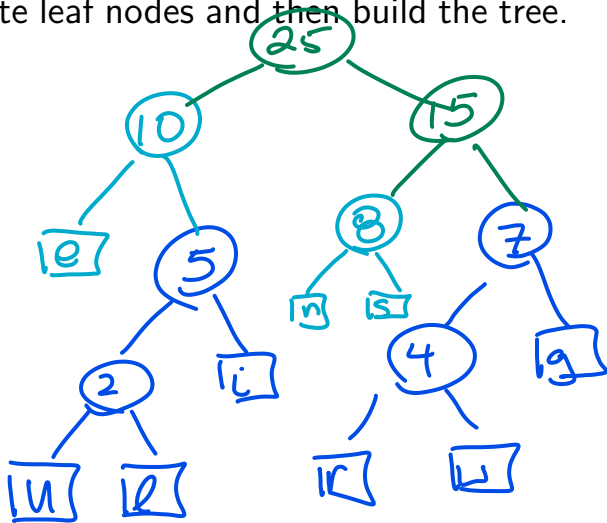


- 1 Let's build a tree for "engineering useless rings"

0010011100...

Step two : Create leaf nodes and then build the tree.

char	count
<del>e</del>	<del>5</del>
<del>n</del>	<del>4</del>
<del>s</del>	<del>4</del>
<del>g</del>	<del>3</del>
<del>i</del>	<del>3</del>
<del>r</del>	<del>2</del>
<del>_</del>	<del>2</del>
<del>u</del>	<del>1</del>
<del>l</del>	<del>1</del>



# How to Encode Message?

- ▶ Encode the tree
- ▶ Encode the message
- ▶ Decoding is similar

CompSci 161  
Winter 2023 Lecture 20:  
Greedy Algorithms:  
Fractional Knapsack and  
Comparison of Techniques

# Fractional Knapsack

how much you take

► Decide  $x_i : 0 \leq x_i \leq w_i$

► Require  $\sum_i x_i \leq W$

► Goal:  $\max \sum_i b_i(x_i/w_i) = \max \sum_i \left(\frac{b_i}{w_i}\right) x_i$

Suppose  $W = 10$  and

Item :	1	2	3	4	5
Weight:	4	8	2	6	1
Benefit:	12	32	40	30	50

## Greedy Algorithm for Fractional Knapsack

- ▶ Sort by benefit per unit wt:  $b_i/w_i$
- ▶ For each item in order (smaller  $i$ : larger  $\frac{b_i}{w_i}$ )
  - ▶ Take all (if possible) or remaining carrying capacity

- ▶ Suppose FSOC solution exists better than ours
- ▶ What do we know because of that?

$$i < K \quad x_i < w_i \quad \text{and} \quad x_K > 0$$

$$\text{but} \quad \frac{b_i}{w_i} > \frac{b_K}{w_K}$$

- ▶ How do we improve this "better" solution?

alternate

Decrease  $x_K$  increase  $x_i$ . By  $\min(w_i - x_i, x_K)$

# Review Conversations

- ▶ Why don't these work for fractional knapsack?
  - ▶ Sort by weight
  - ▶ Sort by benefit
- ▶ Why don't these work for 0-1 Knapsack?
  - ▶ Sort by weight
  - ▶ Sort by benefit
  - ▶ Sort by benefit per unit weight