



A Comprehensive Framework for Modeling and Correcting Color Variations in Multi Projector Displays

Aditi Majumder

Slide 1



Historical Perspective

- A dream computer in 1980 (Bill Joy and others)
 - Megabytes of memory
 - Megahertz of speed
 - Mega pixels
- Today
 - Gigabytes of memory
 - Gigahertz of speed
 - And still Mega pixels !! (1000 x 1000 monitor)

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Large Area Displays

	<i>We have today in common use</i>	<i>We would like to have</i>
<i>Size</i>	19 inch diagonal	15 feet x 10 feet
<i>Resolution</i>	60 pixels/inch	100 – 300 pixels/inch
<i>Field of View</i>	20 – 30 degrees	120 – 140 degrees
<i># of pixels</i>	1 million	100 – 140 million

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Applications

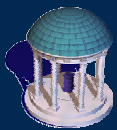
- Scientific Visualization
- Medical Visualization
- Telecollaboration
- Virtual Reality
- Training and Simulation



*Flow Visualization
of Fluids at
Argonne National
Laboratory (ANL)*

*Medical Visualization at
Radiology Department of
Stanford*



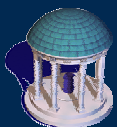


Multi Projector Displays

- Tile projectors



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Multi Projector Displays

- Tile projectors
- 15 projectors
 - 3x5 array
 - 10 feet x 8 feet
 - 50 pixels/inch
 - 12 million pixels

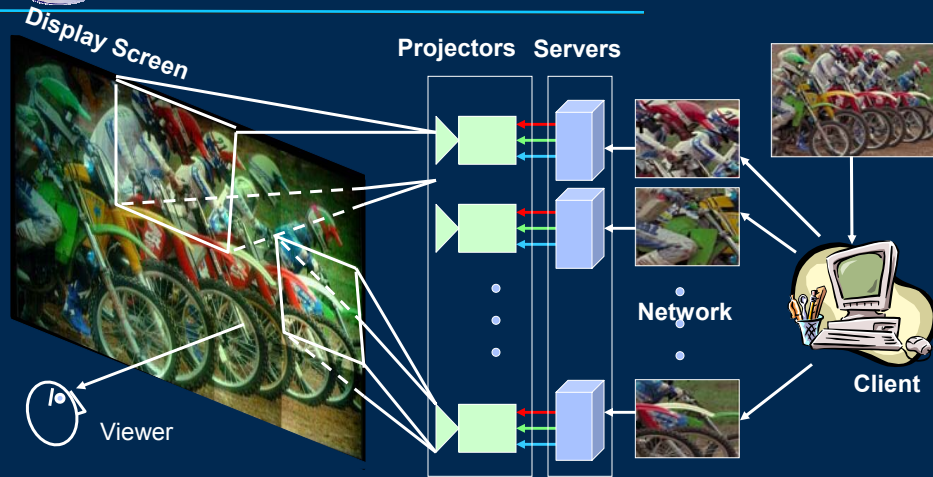


At ANL

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Building Multi Projector Displays



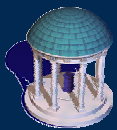
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Making them seamless

- Geometric Alignment

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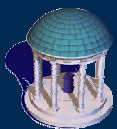


Making them seamless

- Geometric Alignment



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Making them seamless

- Geometric Alignment



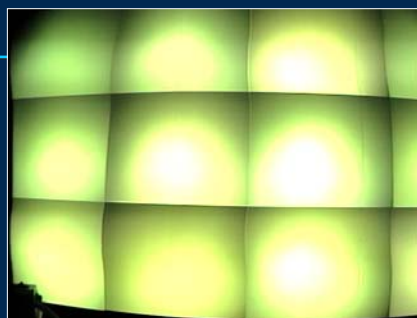
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Making them seamless

- Geometric Alignment
- Color Seamlessness

Overlapping



Abutting



Slide 11



The Problem

Even with perfect geometric alignment, color variation breaks the illusion of a single seamless display



At ANL

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The Goal of Color Seamlessness

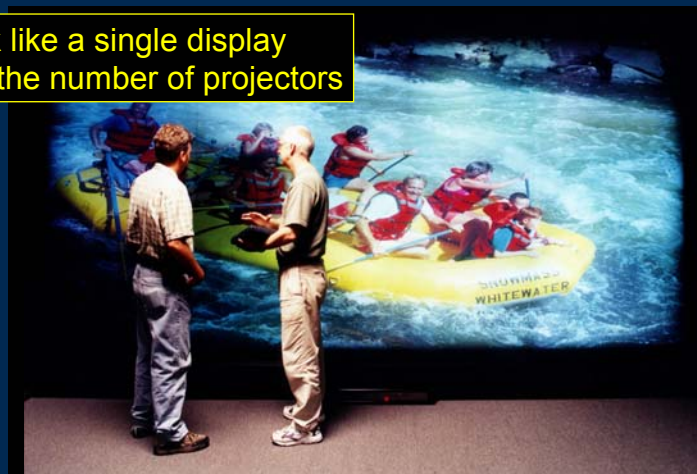


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The Goal of Color Seamlessness

Should look like a single display
Cannot tell the number of projectors



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Background: Color

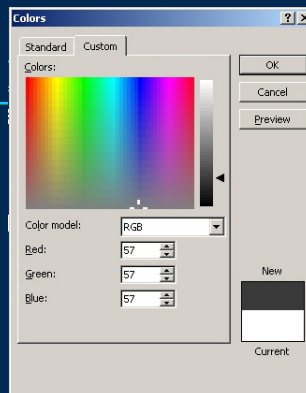
- Perceptual Representation

- Luminance (L) 

- » Sense of Brightness

- Chrominance (x, y)

- » Sense of hue



- Representation Using Primaries

- Three channels (Red, Green, Blue)



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Color Seamlessness

- Luminance Seamlessness (Brightness)

- Chrominance Seamlessness (Hue)

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Why Is It Difficult?

- No comprehensive model of color variation
- No formal definition of *color seamlessness*
- The problem is inherently five dimensional
 - Color (3D – 1D luminance and 2D chrominance)
 - Display surface (2D)
- Humans are more sensitive **spatial** variations than to **temporal** variations in color

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Innovations

- **Emineoptic function** : Models the luminance and chrominance variation in multi projector displays
 - ‘emineoptic’ signifies ‘viewing projected light’
- A definition for color seamlessness
 - Optimization Problem
- An algorithm to address **luminance** variation (photometric seamlessness)
 - Same model projectors differ significantly in luminance
 - Humans are more sensitive to luminance than chrominance

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Thesis Statement

- *The color variation in multi-projector displays can be modeled by the **emineoptic function**.*
- *Achieving color seamlessness is an **optimization problem** that can be defined using the emineoptic function.*
- *Perceptually uniform high quality displays can be achieved by realizing a **desired emineoptic function** that **differs minimally** from the original function and has **imperceptible** color variation.*

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Organization

- Previous Work
- The Emineoptic Function
- Definition of Color Seamlessness
- Achieving Photometric Seamlessness
- Results

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Organization

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Classification of Color Variation

- Intra-projector
 - Within a single projector
- Inter-projector
 - Across different projectors
- Overlaps

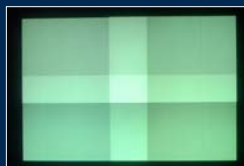


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Classification of Color Variation

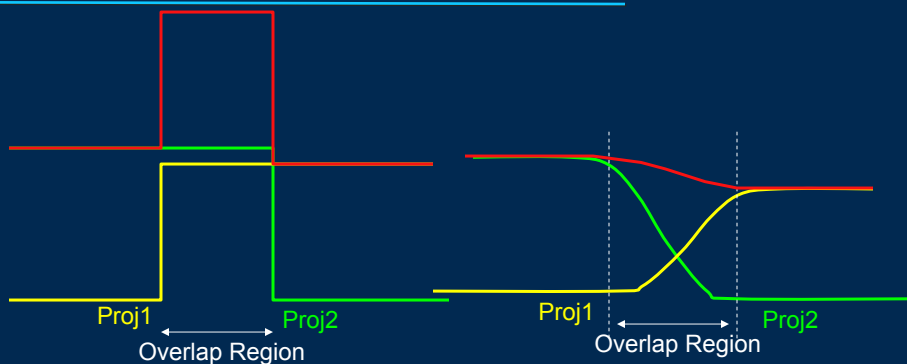
- Intra-projector
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Edge Blending



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Software Edge Blending



Before



Software Blending

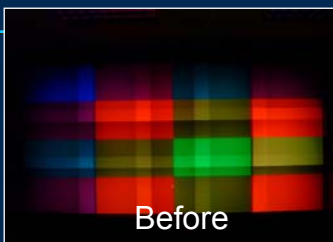
Raskar et al 1998 (UNC)

Yang et al 2001 (UNC)

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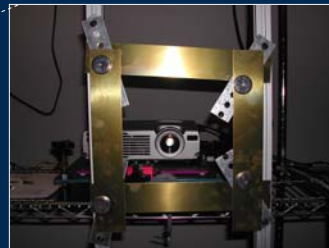
Aperture Edge Blending



Before



Aperture Blending



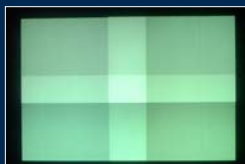
Li et al 2000 (Princeton)

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Classification of Color Variation

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Previous Work

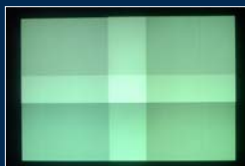
- Projector Controls
- Using the same bulb
 - Pailthorpe et al 2001 (NSCA San Diego)
- Inter-projector response matching
 - Stone et al 2000, 2001 (Stanford)
 - Chen et al 2002 (Princeton)

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Classification of Color Variation

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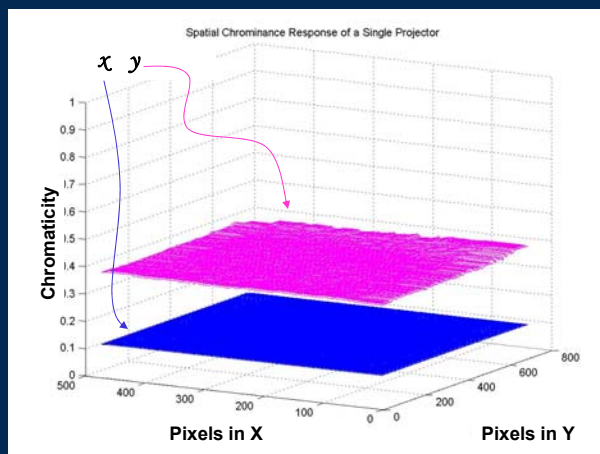


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Intra-Projector Variations

- Chrominance response

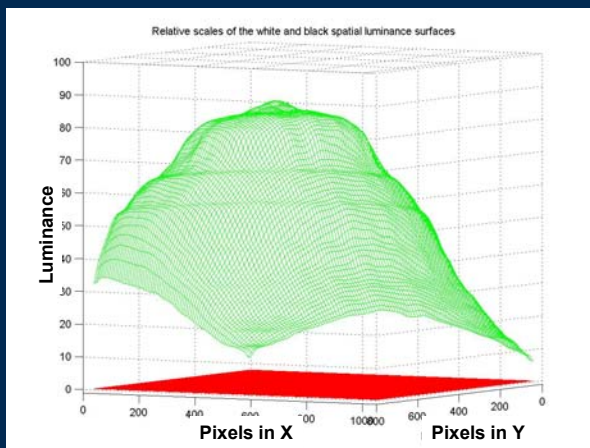


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Intra-Projector Variations

- Luminance response

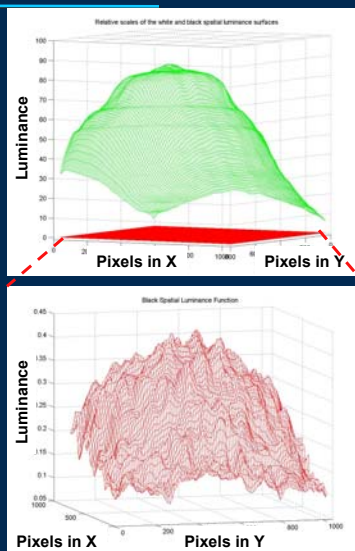


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Intra-Projector Variations

- Luminance response
- Black offset
 - Always present



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Limitations of Previous Methods

- No algorithm addresses intra projector variation
- No algorithm addresses more than one class of problems
- Each class of problems treated as a special case
- *Strict uniformity mindset*
 - *Identical color response at every display coordinate*

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Desiderata

- Comprehensive and general framework
 - Addresses intra, inter and overlap variations
 - Design general solutions
 - » No special cases
 - » Automated
 - » Scalable
 - Explain and compare existing methods

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Organization

- Previous Work
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- Definition of Color Seamlessness
- Achieving Photometric Seamlessness
- Results

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Achieving Color Seamlessness

- To correct, first capture
- Complexity of capture
 - Input color space : 24 bit color
 - Need 2^{24} images
- Reduce complexity by modeling projector color variations

Emineoptic Function

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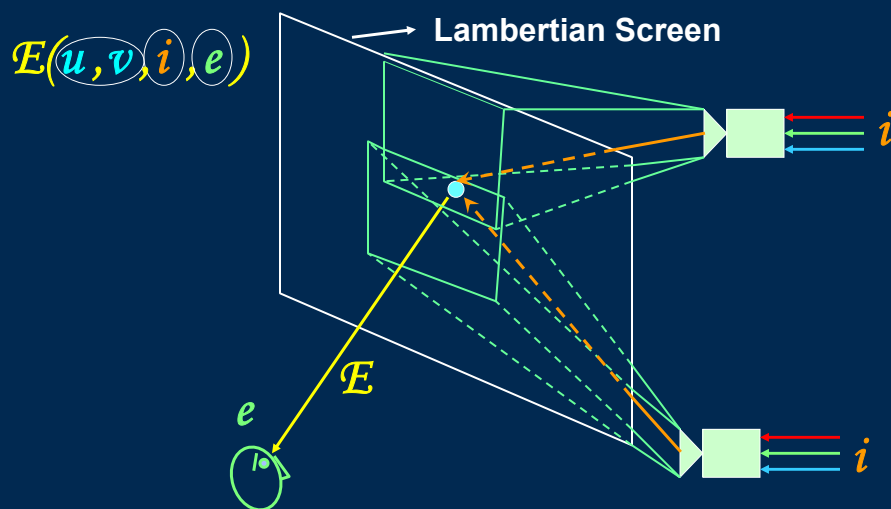
Thesis Statement

- *The color variation in multi-projector displays can be modeled by the **emineoptic function**.*
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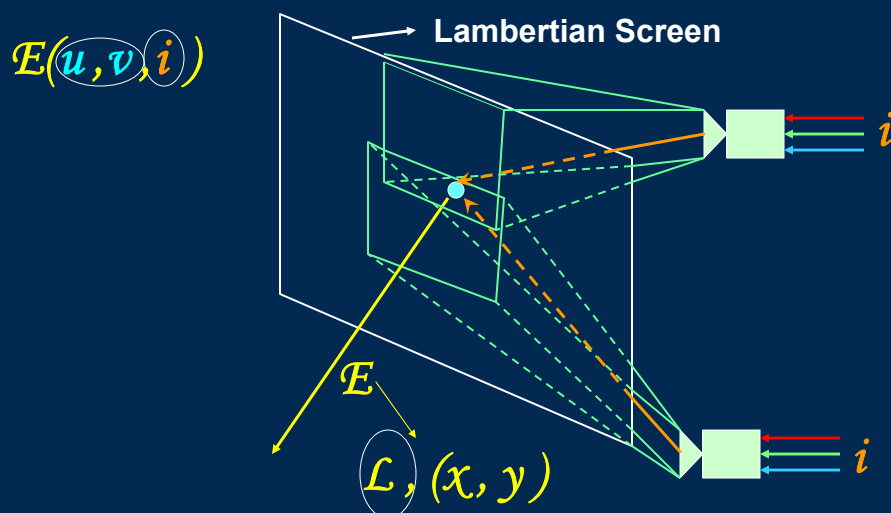
The Emineoptic Function



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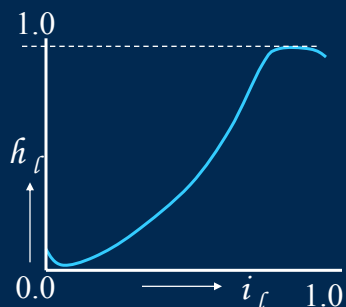
The Emineoptic Function



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Single Pixel, Single Channel Input



- Maximum channel luminance ($\mathcal{M}_l$)
- Variation in luminance with channel input
 - » Channel transfer function ($\hat{h}_l(i_l)$)

$$C_l(i_l) = \hat{h}_l(i_l) \mathcal{M}_l$$

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Single Pixel, Three Channel Input

At one pixel for one channel:

$$C_l(i_l) = \hat{h}_l(i_l) \mathcal{M}_l$$

For any input $\mathbf{i} = (i_r, i_g, i_b)$:

$$\mathcal{P}(\mathbf{i}) = C_r(i_r) + C_g(i_g) + C_b(i_b)$$

With black Offset $\mathcal{B}$:

$$\begin{aligned} \mathcal{P}(\mathbf{i}) = & C_r(i_r) \\ & + C_g(i_g) \\ & + C_b(i_b) \\ & + \mathcal{B} \end{aligned}$$

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Single Projector Display

At one pixel for one channel:

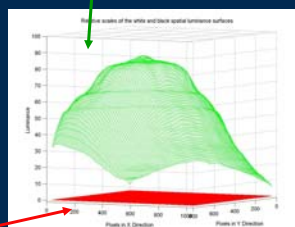
$$C_{\ell}(i_{\ell}, u, v) = \boxed{h_{\ell}(i_{\ell}, u, v)} \boxed{\mathcal{M}_{\ell}(u, v)}$$

For any input $i = (i_r, i_g, i_b)$:

$$\mathcal{P}(i, u, v) = C_r(i_r, u, v) + C_g(i_g, u, v) + C_b(i_b, u, v)$$

With black Offset $\mathcal{B}$:

$$\begin{aligned} \mathcal{P}(i, u, v) = & C_r(i_r, u, v) \\ & + C_g(i_g, u, v) \\ & + C_b(i_b, u, v) \\ & + \boxed{\mathcal{B}(u, v)} \end{aligned}$$



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Single Projector Display

At one pixel for one channel:

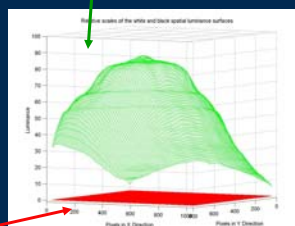
$$C_{\ell}(i_{\ell}, u, v) = \boxed{h_{\ell}(i_{\ell})} \boxed{\mathcal{M}_{\ell}(u, v)}$$

For any input $i = (i_r, i_g, i_b)$:

$$\mathcal{P}(i, u, v) = C_r(i_r, u, v) + C_g(i_g, u, v) + C_b(i_b, u, v)$$

With black Offset $\mathcal{B}$:

$$\begin{aligned} \mathcal{P}(i, u, v) = & C_r(i_r, u, v) \\ & + C_g(i_g, u, v) \\ & + C_b(i_b, u, v) \\ & + \boxed{\mathcal{B}(u, v)} \end{aligned}$$



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Single Projector Display

At one pixel for one channel:

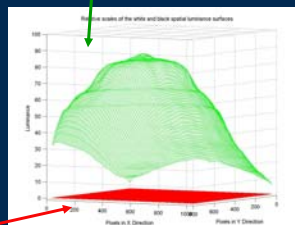
$$C_c(i_c, u, v) = \boxed{h_c(i_c)} \boxed{M_c(u, v)}$$

For any input $\mathbf{i} = (i_r, i_g, i_b)$:

$$\mathcal{P}(\mathbf{i}, u, v) = C_r(i_r, u, v) + C_g(i_g, u, v) + C_b(i_b, u, v)$$

With black Offset $\mathcal{B}$:

$$\begin{aligned} \mathcal{P}(\mathbf{i}, u, v) = & h_r(i_r) M_r(u, v) \\ & + h_g(i_g) M_g(u, v) \\ & + h_b(i_b) M_b(u, v) \\ & + \boxed{\mathcal{B}(u, v)} \end{aligned}$$



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Single Projector Display

$$\begin{aligned} \mathcal{P}(\mathbf{i}, u, v) = & \boxed{h_r(i_r)} \boxed{M_r(u, v)} \\ & + \boxed{h_g(i_g)} \boxed{M_g(u, v)} \\ & + \boxed{h_b(i_b)} \boxed{M_b(u, v)} \\ & + \boxed{\mathcal{B}(u, v)} \end{aligned}$$

Transfer Functions

Luminance Functions

Black Offset

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Multi-Projector Display

$ \mathcal{N} =1$	2	$ \mathcal{N} =1$
$ \mathcal{N} =2$	4	$ \mathcal{N} =2$
$ \mathcal{N} =1$	2	$ \mathcal{N} =1$

$$\mathcal{E}(u, v, i) = \sum_{j \in \mathcal{N}(u, v)} \mathcal{P}_j(u, v, i)$$

$$\begin{aligned} \mathcal{E}(i, u, v) = & \sum \mathcal{h}_r(i_r) \mathcal{M}_r(u, v) \\ & + \sum \mathcal{h}_g(i_g) \mathcal{M}_g(u, v) \\ & + \sum \mathcal{h}_b(i_b) \mathcal{M}_b(u, v) \\ & + \sum \mathcal{B}(u, v) \\ & j \in \mathcal{N}(u, v) \end{aligned}$$

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Multi-Projector Display

- Intra projector luminance variation
 - $\mathcal{M}_r(u, v)$ and $\mathcal{B}(u, v)$ are not flat
- Inter projector luminance variation
 - $\mathcal{h}_r(i_r)$ is different
 - $\mathcal{M}_r(u, v)$ and $\mathcal{B}(u, v)$ have different shapes
- Overlap luminance variation
 - $\mathcal{N}$ is different

$$\begin{aligned} \mathcal{E}(i, u, v) = & \sum \mathcal{h}_r(i_r) \mathcal{M}_r(u, v) \\ & + \sum \mathcal{h}_g(i_g) \mathcal{M}_g(u, v) \\ & + \sum \mathcal{h}_b(i_b) \mathcal{M}_b(u, v) \\ & + \sum \mathcal{B}(u, v) \\ & j \in \mathcal{N}(u, v) \end{aligned}$$

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Including Chrominance

$$\begin{aligned}\mathcal{E}(i, u, v) = & \sum \hat{h}_r(i_r) \mathcal{M}_r(u, v) \\ & + \sum \hat{h}_g(i_g) \mathcal{M}_g(u, v) \\ & + \sum \hat{h}_b(i_b) \mathcal{M}_b(u, v) \\ & + \sum \mathcal{B}(u, v) \\ & j \in \mathcal{N}(u, v)\end{aligned}$$

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Including Chrominance

$$\begin{aligned}\mathcal{E}(i, u, v) = & \sum \hat{h}_r(i_r) (\mathcal{M}_r(u, v), c_r(u, v)) \\ & + \sum \hat{h}_g(i_g) (\mathcal{M}_g(u, v), c_g(u, v)) \\ & + \sum \hat{h}_b(i_b) (\mathcal{M}_b(u, v), c_b(u, v)) \\ & + \sum (\mathcal{B}(u, v), c_{\mathcal{B}}(u, v)) \\ & j \in \mathcal{N}(u, v)\end{aligned}$$

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Including Chrominance

$$\begin{aligned} \mathcal{E}(i, u, v) = & \sum \hat{h}_r(i_r) \otimes (\mathcal{M}_r(u, v), c_r(u, v)) \\ & + \sum \hat{h}_g(i_g) \otimes (\mathcal{M}_g(u, v), c_g(u, v)) \\ & + \sum \hat{h}_b(i_b) \otimes (\mathcal{M}_b(u, v), c_b(u, v)) \\ & + \sum_{j \in \mathcal{N}(u, v)} (\mathcal{B}(u, v), c_{\mathcal{B}}(u, v)) \end{aligned}$$

$$\hat{k} \otimes (\mathcal{L}_1, c_1) = (\hat{k}\mathcal{L}_1, c_1)$$

Luminance Scaling

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Including Chrominance

$$\begin{aligned} \mathcal{E}(i, u, v) = & \oplus \hat{h}_r(i_r) \otimes (\mathcal{M}_r(u, v), c_r(u, v)) \\ & \oplus \oplus \hat{h}_g(i_g) \otimes (\mathcal{M}_g(u, v), c_g(u, v)) \\ & \oplus \oplus \hat{h}_b(i_b) \otimes (\mathcal{M}_b(u, v), c_b(u, v)) \\ & \oplus \oplus_{j \in \mathcal{N}(u, v)} (\mathcal{B}(u, v), c_{\mathcal{B}}(u, v)) \end{aligned}$$

$$\hat{k} \otimes (\mathcal{L}_1, c_1) = (\hat{k}\mathcal{L}_1, c_1)$$

Luminance Scaling

$$(\mathcal{L}_1, c_1) \oplus (\mathcal{L}_2, c_2) = \left(\mathcal{L}_1 + \mathcal{L}_2, \frac{c_1\mathcal{L}_1}{\mathcal{L}_1 + \mathcal{L}_2} + \frac{c_2\mathcal{L}_2}{\mathcal{L}_1 + \mathcal{L}_2} \right)$$

Optical Superposition

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Including Chrominance

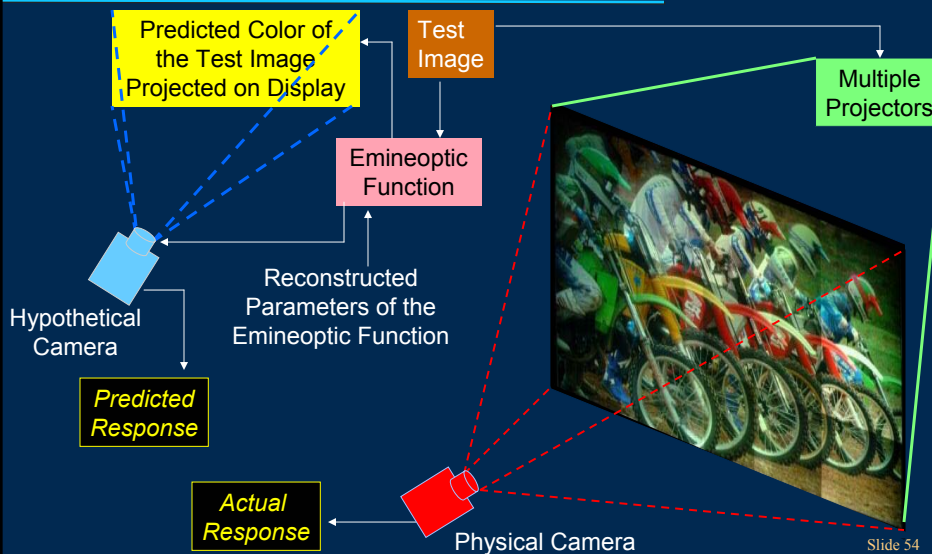
$$\begin{aligned} \mathcal{E}(i, u, v) = & \bigoplus \hat{h}_r(i_r) \bigotimes (\mathcal{M}_r(u, v), c_r(u, v)) \\ & \bigoplus \bigoplus \hat{h}_g(i_g) \bigotimes (\mathcal{M}_g(u, v), c_g(u, v)) \\ & \bigoplus \bigoplus \hat{h}_b(i_b) \bigotimes (\mathcal{M}_b(u, v), c_b(u, v)) \\ & \bigoplus \bigoplus (\mathcal{B}(u, v), c_{\mathcal{B}}(u, v)) \\ & j \in \mathcal{N}(u, v) \end{aligned}$$

- Intra projector chrominance variation
 - $c_r(u, v)$ and $c_b(u, v)$ are not flat
 - $\mathcal{M}_r$, $\mathcal{M}_g$, and $\mathcal{M}_b$ differ in shape
- Inter projector and overlap chrominance variation
 - c_r and c_b differ
 - The relative proportions of $\max(\mathcal{M}_r(u, v))$ across channels

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Model Verification



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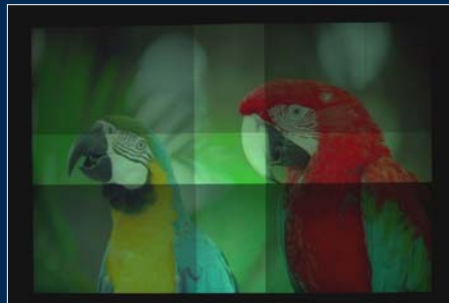
Modeled vs Actual (Both luminance and chrominance)



Test Image



Predicted Response



Actual Response

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Organization

- Previous Work
- The Emineoptic Function
- Definition of Color Seamlessness
- Achieving Photometric Seamlessness
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Thesis Statement

- *The color variation in multi-projector displays can be modeled by the emineoptic function.*
- *Achieving color seamlessness is an **optimization problem** that can be defined using the emineoptic function.*
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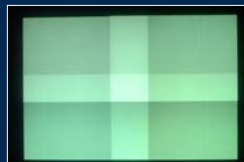
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Properties of Color Variation

Based on extensive empirical analysis of real projectors

- Intra-projector
 - Within a single projector
- Inter-projector
 - Across different projectors
- Overlaps



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Properties of Color Variation

Based on extensive empirical analysis of real projectors

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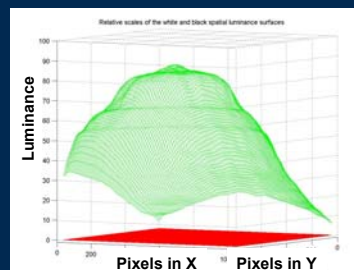
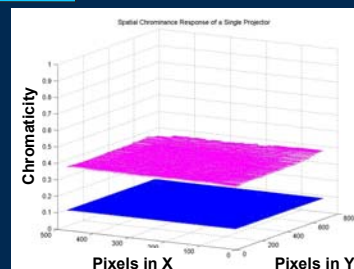
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Intra-Projector Variations

- Chrominance is almost constant
- Luminance is not

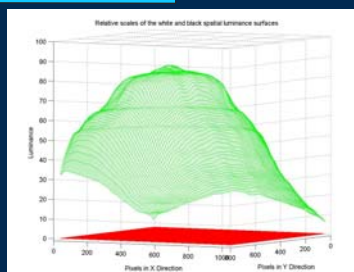
Luminance variation is more significant than chrominance variation





Intra-Projector Variations

- Chrominance is constant
- Luminance is not



$$\begin{aligned}
 E(i, u, v) = & \oplus h_r(i_r) \otimes (\mathcal{M}_r(u, v), c_r(u, v)) \\
 & \oplus \oplus h_g(i_g) \otimes (\mathcal{M}_g(u, v), c_g(u, v)) \\
 & \oplus \oplus h_b(i_b) \otimes (\mathcal{M}_b(u, v), c_b(u, v)) \\
 & \oplus \oplus (B(u, v), c_B(u, v)) \\
 & \quad j \in \mathcal{N}(u, v)
 \end{aligned}$$

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Properties of Color Variation

Based on extensive empirical analysis of real projectors

- Intra-projector
 - Within a single projector
- Inter-projector
 - Across different projectors
- Overlaps

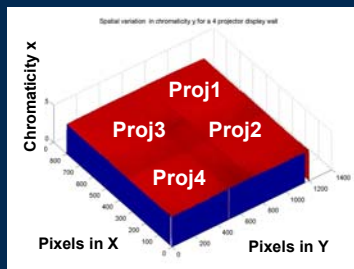


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Inter-Projector Variations

- Projectors of same model
 - Chrominance variation is **negligible**
 - Luminance variation is **significant**
- Projectors of different models
 - Chrominance variation is **relatively very small**
 - Luminance variation is **significant**



Chrominance (χ) of a four projector display

Luminance variation is more significant than chrominance variation

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Inter-Projector Variations

$$E(i, u, v) = \bigoplus_{j \in \mathcal{N}(u, v)} \bigoplus_{r \in \{r, g, b\}} \bigoplus_{h_r(i_r)} \bigotimes (\mathcal{M}_r(u, v), c_r(u, v))$$

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Properties of Color Variation

Based on extensive empirical analysis of real projectors

- Intra-projector
 - Within a single projector
- Inter-projector
 - Across different projectors
- Overlaps



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Overlaps

- For displays made of same model projectors, at overlap regions
 - Chrominance remains almost constant
 - Luminance almost gets multiplied by the number of overlapping projectors



Luminance variation is more significant than chrominance variation

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Addresses only Luminance

- Most display walls made of same model projectors
 - Spatial variation in chrominance is insignificant compared to luminance
- Humans are more sensitive to spatial luminance variation than to spatial chrominance variation

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Achieving Photometric Seamlessness

- Reconstruction
 - Reconstruct $\mathcal{E}$
- Modification
 - Modify $\mathcal{E}$ to $\mathcal{E}'$
- Reprojection
 - Reproject $\mathcal{E}'$

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Achieving Photometric Seamlessness

- Reconstruction
 - Reconstruct $\mathcal{E}$
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 - Modify $\mathcal{E}$ to $\mathcal{E}'$
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 - Reproject $\mathcal{E}'$

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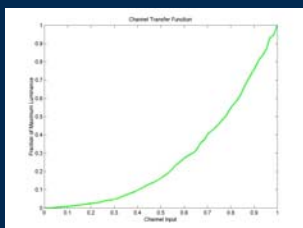


Reconstruction

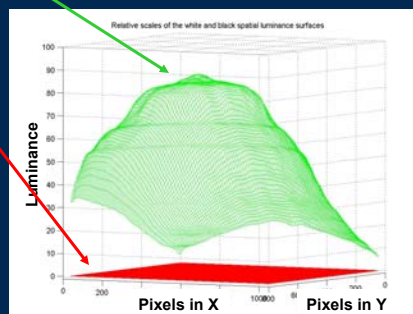
$$\mathcal{E}(i, u, v) = \sum_{r \in \mathcal{R}} h_r(i_r) \mathcal{M}_r(u, v) + \sum_{g \in \mathcal{G}} h_g(i_g) \mathcal{M}_g(u, v) + \sum_{b \in \mathcal{B}} h_b(i_b) \mathcal{M}_b(u, v) + \sum_{j \in \mathcal{N}(u, v)} \mathcal{B}(u, v)$$

Transfer Function

Luminance Function



Black Offset



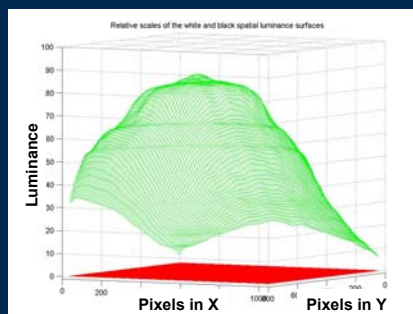
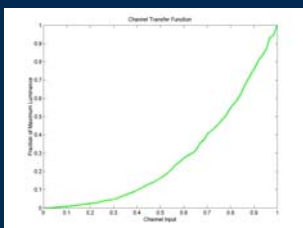


Reconstruction

$$\mathcal{E}(i, u, v) = \sum \left[\begin{array}{l} \hat{h}_r(i_r) \mathcal{M}_r(u, v) \\ + \hat{h}_g(i_g) \mathcal{M}_g(u, v) \\ + \hat{h}_b(i_b) \mathcal{M}_b(u, v) \\ + \mathcal{B}(u, v) \end{array} \right]$$

Photometer Camera

$j \in \mathcal{N}(u, v)$



Achieving Photometric Seamlessness

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Modification 1

$$\begin{aligned}\mathcal{P}(i, u, v) = & \ h_r(i_r) \mathcal{M}_r(u, v) \\ & + h_g(i_g) \mathcal{M}_g(u, v) \\ & + h_b(i_b) \mathcal{M}_b(u, v) \\ & + \mathcal{B}(u, v)\end{aligned}$$

Single Projector

$$\begin{aligned}\mathcal{E}(i, u, v) = & \sum h_r(i_r) \mathcal{M}_r(u, v) \\ & + \sum h_g(i_g) \mathcal{M}_g(u, v) \\ & + \sum h_b(i_b) \mathcal{M}_b(u, v) \\ & + \sum_{j \in \mathcal{N}(u, v)} \mathcal{B}(u, v)\end{aligned}$$

Multi Projector

- Match $h_c(i_c)$ of projectors

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Modification 1

$$\begin{aligned}\mathcal{P}(i, u, v) = & \ h_r(i_r) \mathcal{M}_r(u, v) \\ & + h_g(i_g) \mathcal{M}_g(u, v) \\ & + h_b(i_b) \mathcal{M}_b(u, v) \\ & + \mathcal{B}(u, v)\end{aligned}$$

Single Projector

$$\begin{aligned}\mathcal{E}(i, u, v) = & \sum \mathcal{H}_r(i_r) \mathcal{M}_r(u, v) \\ & + \sum \mathcal{H}_g(i_g) \mathcal{M}_g(u, v) \\ & + \sum \mathcal{H}_b(i_b) \mathcal{M}_b(u, v) \\ & + \sum_{j \in \mathcal{N}(u, v)} \mathcal{B}(u, v)\end{aligned}$$

Multi Projector

- Match $h_c(i_c)$ of projectors

Slide 74



Modification 1

$$\begin{aligned}\mathcal{P}(i, u, v) = & \ h_r(i_r) \ \mathcal{M}_r(u, v) \\ & + \ h_g(i_g) \ \mathcal{M}_g(u, v) \\ & + \ h_b(i_b) \ \mathcal{M}_b(u, v) \\ & + \ \mathcal{B}(u, v)\end{aligned}$$

Single Projector

$$\begin{aligned}\mathcal{E}(i, u, v) = & \ \mathcal{H}_r(i_r) \sum \mathcal{M}_r(u, v) \\ & + \ \mathcal{H}_g(i_g) \sum \mathcal{M}_g(u, v) \\ & + \ \mathcal{H}_b(i_b) \sum \mathcal{M}_b(u, v) \\ & + \ \sum_{j \in \mathcal{N}(u, v)} \mathcal{B}(u, v)\end{aligned}$$

Multi Projector

- Match $h_c(i_c)$ of projectors

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Modification 1

$$\begin{aligned}\mathcal{P}(i, u, v) = & \begin{array}{|l|l|} \hline h_r(i_r) & \mathcal{M}_r(u, v) \\ \hline h_g(i_g) & \mathcal{M}_g(u, v) \\ \hline h_b(i_b) & \mathcal{M}_b(u, v) \\ \hline \mathcal{B}(u, v) & \\ \hline \end{array} \begin{array}{l} \text{Luminance Functions} \\ \text{of one Projector} \\ \\ \text{Black Offset of one Projector} \end{array}\end{aligned}$$

Transfer
Function of
one Projector

$$\begin{aligned}\mathcal{E}(i, u, v) = & \begin{array}{|l|l|} \hline \mathcal{H}_r(i_r) & \sum \mathcal{M}_r(u, v) \\ \hline \mathcal{H}_g(i_g) & \sum \mathcal{M}_g(u, v) \\ \hline \mathcal{H}_b(i_b) & \sum \mathcal{M}_b(u, v) \\ \hline \sum_{j \in \mathcal{N}(u, v)} \mathcal{B}(u, v) & \\ \hline \end{array} \begin{array}{l} \text{Luminance Functions} \\ \text{of the whole Display} \\ \\ \text{Black Offset of the whole Display} \end{array}\end{aligned}$$

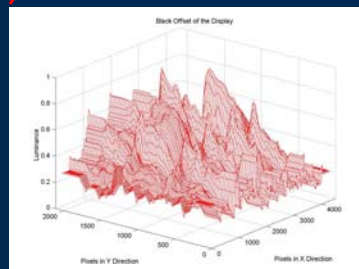
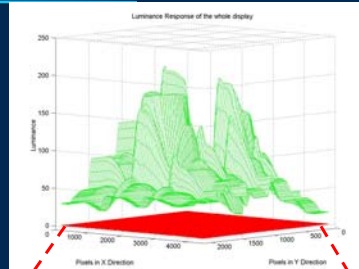
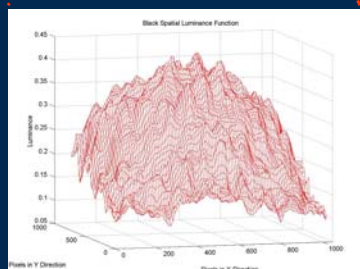
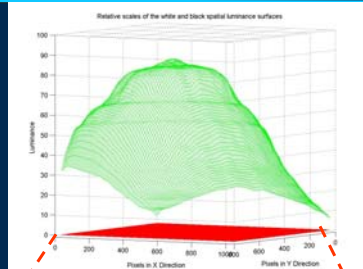
Common
Transfer
Function

Display is like a single large projector



Display Luminance Functions

One Projector Display



15 Projector Display

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Display Luminance Functions

Reconstructing Display Luminance Response

4 Projector Display

15 Projector Display

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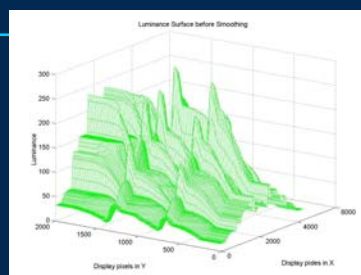
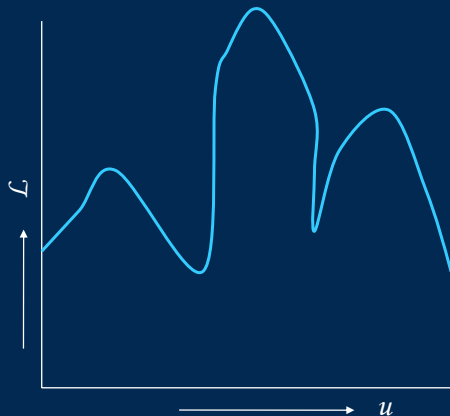
Modification 2

- Sharp discontinuities are the cause of photometric seams
- Remove the sharp discontinuities

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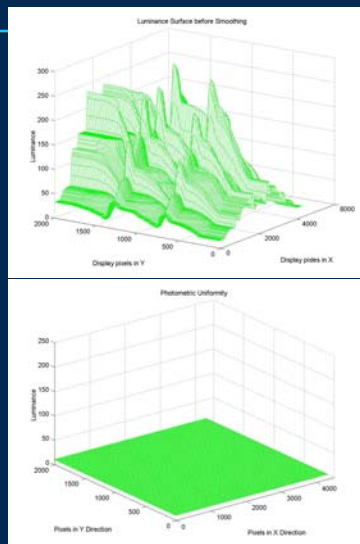
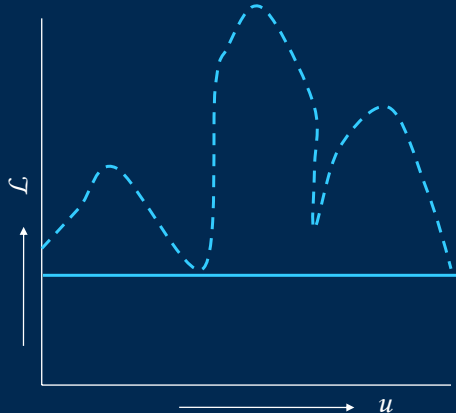
The Problem



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Strict Photometric Uniformity



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Strict Photometric Uniformity

$$|lum(E'(u_1, v_1, i, e)) - lum(E'(u_2, v_2, i, e))| = 0$$

The luminance of the light reaching the viewer from any two coordinates is identical

Strict Color Uniformity

$$|E'(u_1, v_1, i, e) - E'(u_2, v_2, i, e)| = 0$$

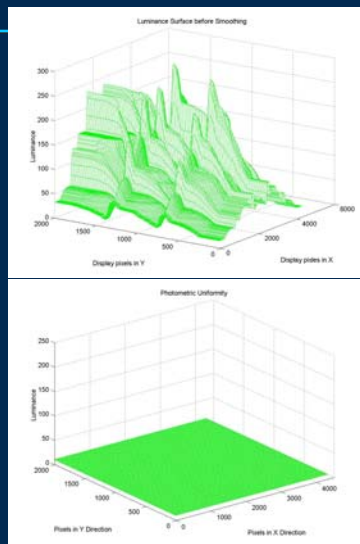
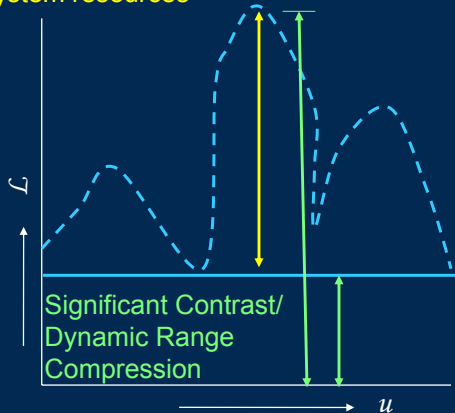
The color of the light reaching the viewer from any two coordinates is identical

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Strict Photometric Uniformity

Suboptimal use of
system resources



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Display Quality



Before

Which one is better?

After Strict Photometric Uniformity

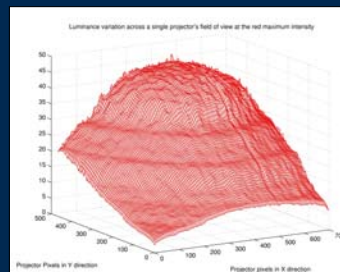
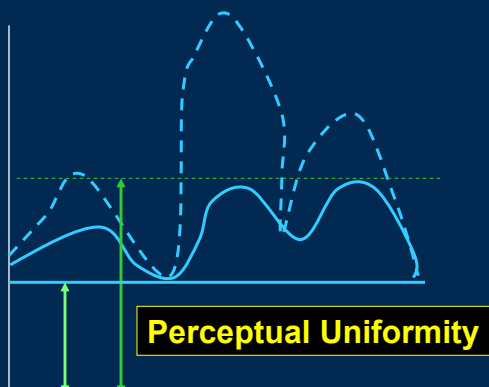


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Is Strict Photometric Uniformity Required?

Humans cannot detect smooth luminance variations



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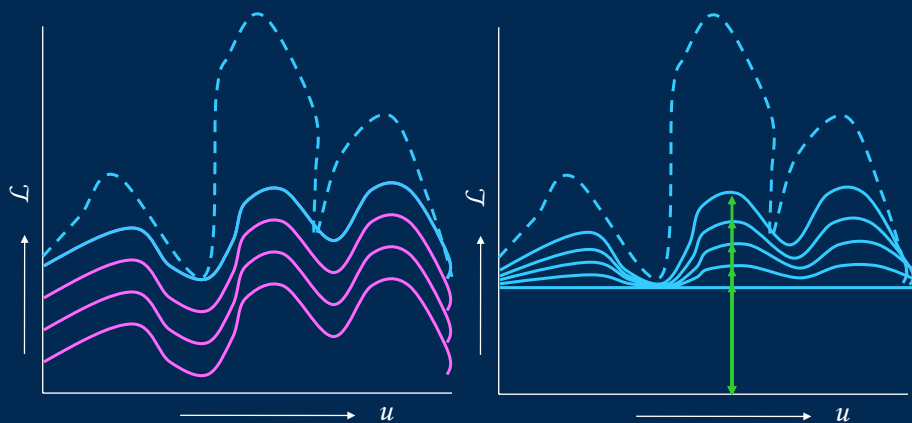
Achieving Photometric Seamlessness

- Optimization Problem
 - Perceptual Uniformity
 - » Creates the *perception* of uniformity
 - Display Quality
 - » Maintains *high* display quality

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Optimization Problem



Strict photometric uniformity is a special case of perceptual uniformity

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Photometric Seamlessness

- Perceptual Uniformity

$$|lum(E'(u_1, v_1, i, e)) - lum(E'(u_2, v_2, i, e))| \leq \Delta$$

- Display Quality

Minimize

$$Distance(lum(E(u, v, i, e)), lum(E'(u, v, i, e)))$$

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Color Seamlessness

- Perceptual Uniformity

$$| E'(u_1, v_1, i, e) - E'(u_2, v_2, i, e) | \leq \Delta$$

- Display Quality
Minimize

$$Distance(E(u, v, i, e), E'(u, v, i, e))$$

Perceptually uniform high quality displays can be achieved by realizing a *desired emineoptic function* that *differs minimally* from the original function and has *imperceptible* color variation.

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Strict Photometric Uniformity



Before

After Strict Photometric Uniformity





Photometric Seamlessness



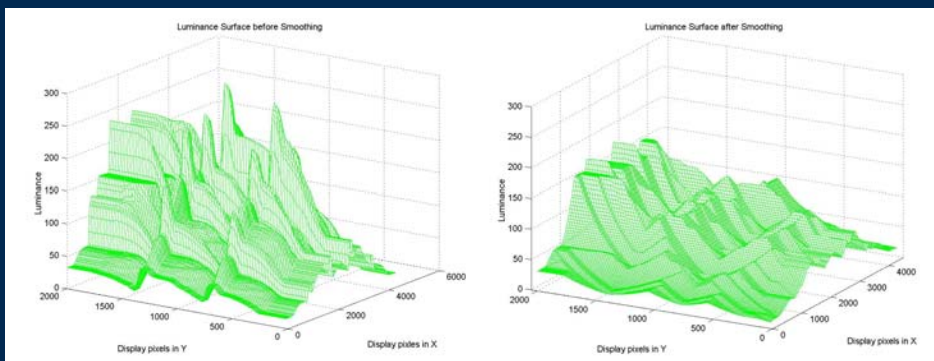
Before

After Photometric Seamlessness



Smooth Luminance Functions

5 x 3 array of fifteen projectors

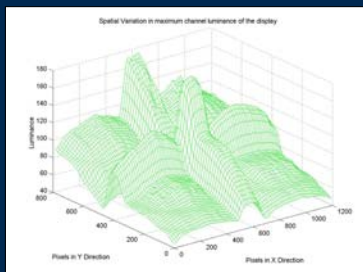


Before smoothing

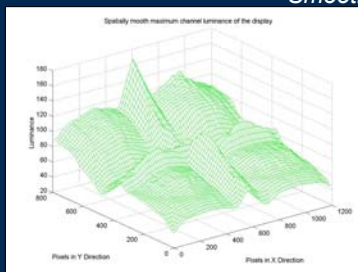
After smoothing



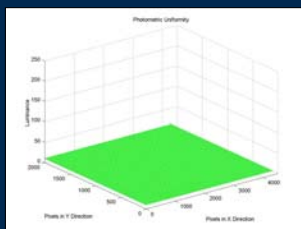
Different Smoothing Parameter (2x2 array of four projectors)



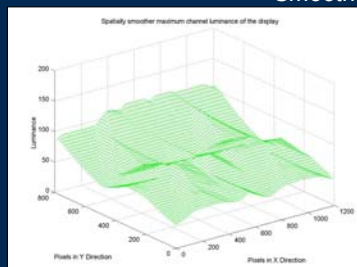
Original



Smooth



Flat



Smoother

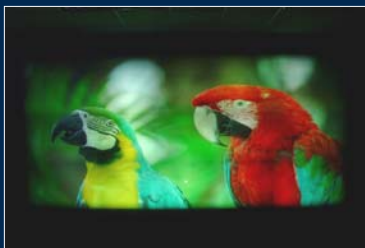
side 93



Using different smoothing parameters (3x5 array of 15 projectors)



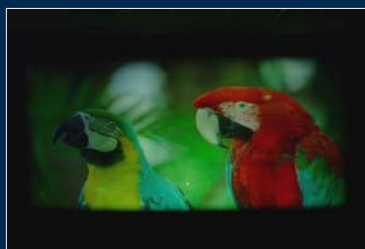
Original



Smooth



Flat



Smoother



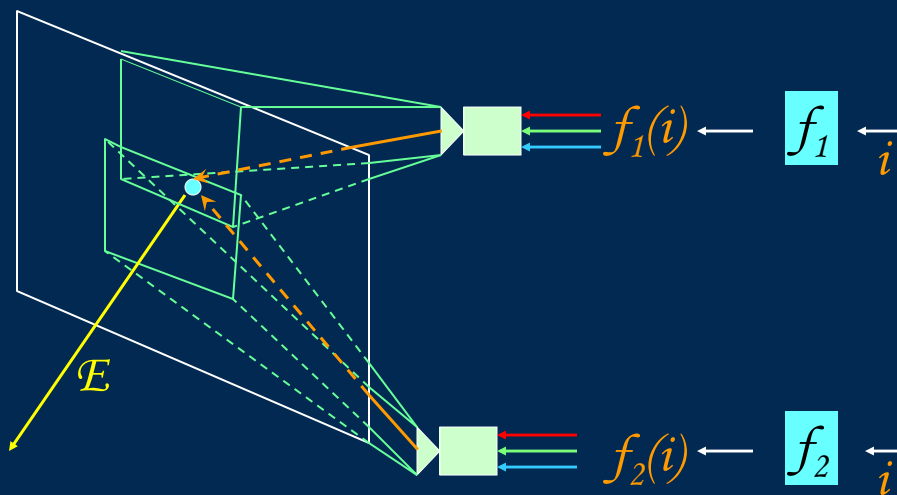
Achieving Photometric Seamlessness

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 - Reproject $\mathcal{E}'$

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Reprojection



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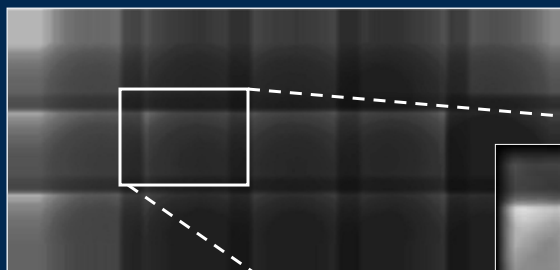
Smoothing Maps

- Attenuation Map
 - Per pixel luminance attenuation to achieve the desired luminance function
- Offset Map
 - Per pixel luminance offset to achieve the desired black offset

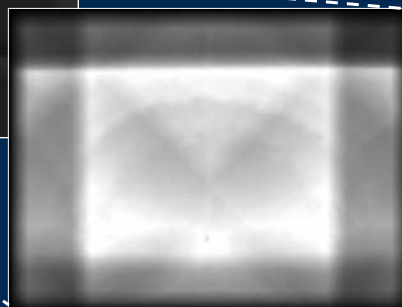
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Attenuation Map

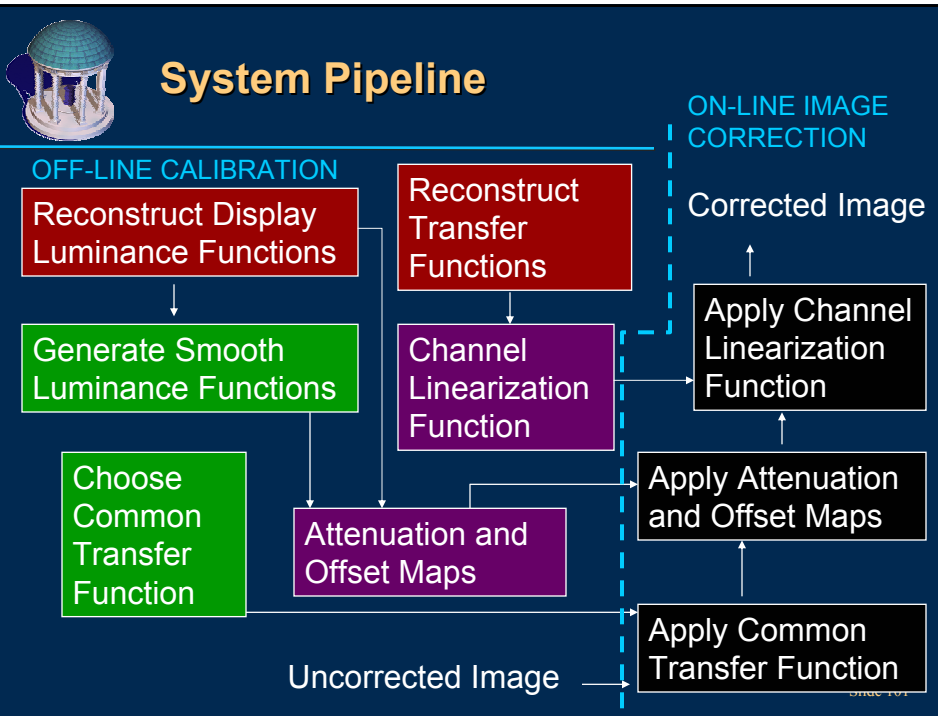


Display Attenuation Map
(15 projector display)



Projector Attenuation Map

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Issues

- Camera
 - Linearity
 - Dynamic Range
 - Sampling Frequency
- Scalability

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Organization

- Previous Work
- The Emineoptic Function
- Definition of Color Seamlessness
- Achieving Photometric Seamlessness
- Results

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Results (After)



Slide 104



Results (Before)



6 Projector Display

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Results (After)



Slide 106



Results (Before)



15 Projector Display

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Chrominance

- Chrominance and luminance are not independent parameters
- 5D nonlinear optimization problem
- No definite perceptual objective metric
- Insights from emineoptic function
 - Luminance variations can be perceived as chrominance variations
- How far can we go with just luminance?

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The Comprehensive Framework

- Validity of the Emineoptic Function
 - Model verification
- Generality
 - Can be used to model color variations of other devices
 - Also a camera
- Unifying Parametric Space
 - Explain and compare different algorithms
 - » Parameters addressed
 - » Formal color correction goal they strive to achieve
 - » Success they can achieve
 - Design new algorithms

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Evaluation Metric

- Comparing the quality of display
 - Brightness
 - Contrast
 - Seamlessness

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Summary

- Modeling color variation comprehensively
- Color Seamlessness
 - Optimization Problem
- Achieving Photometric Seamlessness

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Future Work (Handling Chrominance)



Before

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Future Work (Handling Chrominance)



After

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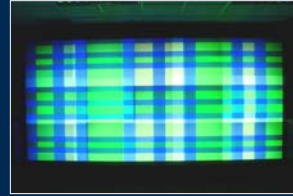
Future Work

- Real time Calibration
- Different kinds of sensors
- Perceptual Image Quality Metric

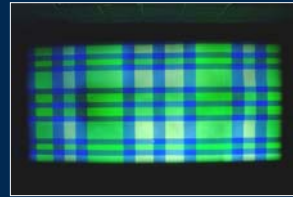
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THE END



Before



After Smoothing