



CS 112 - Polygon Scan Conversion

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Polygon Classification

- Convex
 - All interior angles are less than 180 degrees
- Concave
 - Interior angles can be greater than 180 degrees
- Degenerate polygons
 - If all vertices are collinear

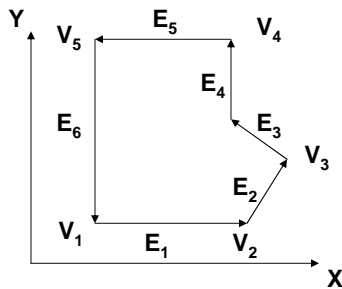
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Identifying Concave Polygons

- Using direction of cross products of adjacent edges
 - If all same sign, then convex, else concave



$$\begin{aligned}
 E_1 \times E_2 &> 0 \\
 E_2 \times E_3 &> 0 \\
 E_3 \times E_4 &< 0 \\
 E_4 \times E_5 &> 0 \\
 E_5 \times E_6 &> 0
 \end{aligned}$$

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Splitting Concave Polygons

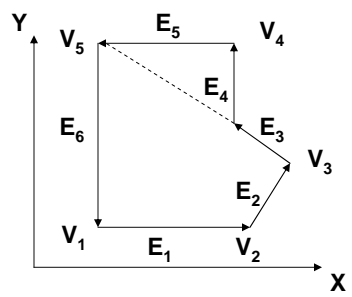
- Assume that the polygon is on XY plane
- Find the cross products of adjacent edges
- If it has a negative z component
 - Split the polygon along the line of the first edge vector of the cross product

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Identifying Concave Polygons

- Using direction of cross products of adjacent edges
 - If all same sign, then convex, else concave

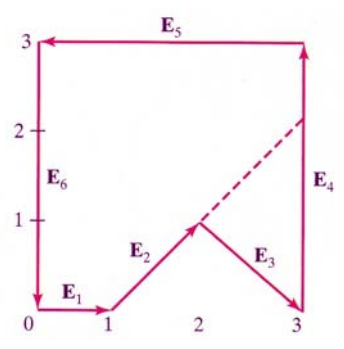


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 \end{aligned}$$

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Example



$$\begin{aligned}
 E_1 &= (1, 0, 0) & E_2 &= (1, 1, 0) \\
 E_3 &= (1, -1, 0) & E_4 &= (0, 2, 0) \\
 E_5 &= (-3, 0, 0) & E_6 &= (0, -2, 0)
 \end{aligned}$$

$$\begin{aligned}
 E_1 \times E_2 &= (0, 0, 1) & E_2 \times E_3 &= (0, 0, -2) \\
 E_3 \times E_4 &= (0, 0, 2) & E_4 \times E_5 &= (0, 0, 6) \\
 E_5 \times E_6 &= (0, 0, 6) & E_6 \times E_1 &= (0, 0, 2)
 \end{aligned}$$

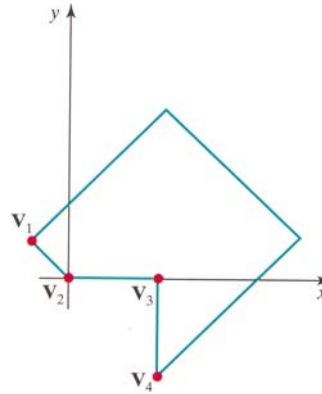
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Rotational Method

- For each vertex V_k
 - Translate so that V_k coincides with origin
 - Rotate clockwise so that V_{k+1} lies on the x-axis
 - If V_{k+2} is below the x-axis, then concave
 - Split along x-axis to get two polygons
 - Apply inverse transformations

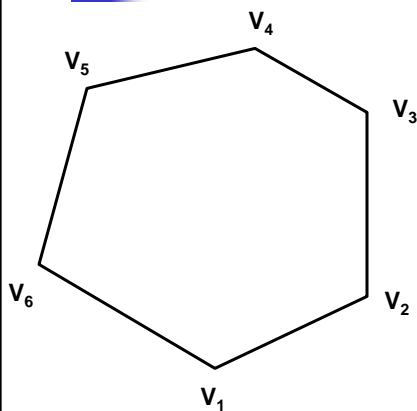


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Triangulating a Convex Polygon

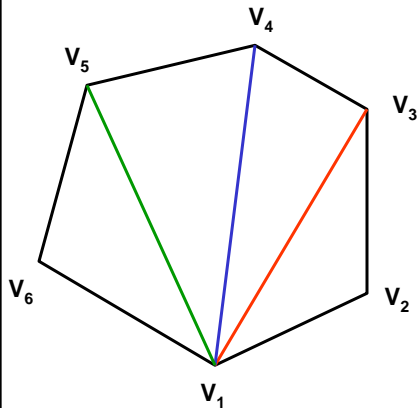


- Take any three vertices in order
- Throw away the middle vertex from the list
- Apply to the same procedure
- Until only three vertices remain

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Triangulating a Convex Polygon



- $V_1, V_2, V_3, V_4, V_5, V_6$
- V_1, V_2, V_3 – tri 1
- V_1, V_3, V_4, V_5, V_6
- V_1, V_3, V_4 – tri 2
- V_1, V_4, V_5, V_6
- V_1, V_4, V_5 – tri 3
- V_1, V_5, V_6 – tri 4

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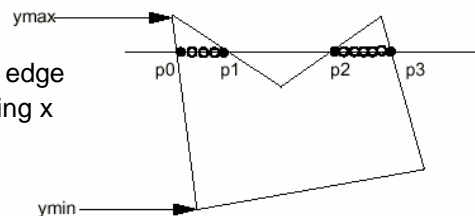
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Polygon Rasterization

- Works for both convex and concave polygons
- Basic Idea: Intersect scanline with polygon edges and fill between pairs of intersections

For $y = y_{min}$ to y_{max}

- 1) intersect scanline y with each edge
- 2) sort intersections by increasing x
[p_0, p_1, p_2, p_3]
- 3) fill pairwise ($p_0 - p_1, p_2 - p_3$)



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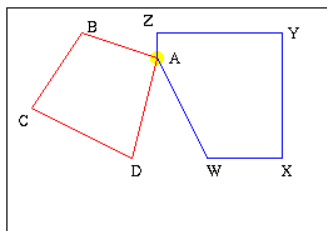
Filling in – Odd Parity Rule

- Sort the intersections
- Start with even parity, and traverse scanline from left to right
- Whenever an intersection is encountered, flip parity
- If parity is odd, draw the pixel
- Continue till the end of the scanline

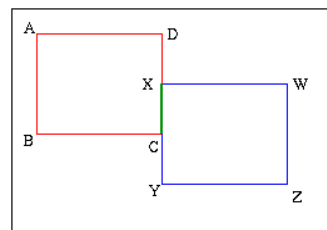
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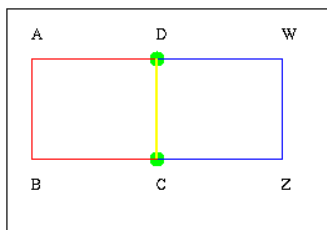
Problem: Shared Boundaries



Case 1: Shared vertices



Case 2: Shared edges



Case 3: Shared vertices and edges

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How to solve this?

- Let the pixel be colored in the order the polygons are scan converted
- Rightmost polygon is the dominant one
- Problems
 - Coloring same pixel multiple times
 - Can cause coloring problems depending on what exactly the coloring function does
 - Can create an amalgam of colors

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How to solve this?

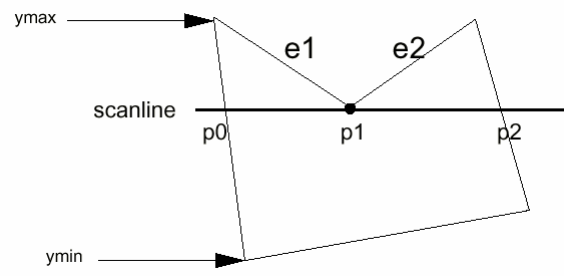
- Define interior: For a given pair of intersection points (X_i, Y) , (X_j, Y)
- Fill ceiling(X_i) to floor(X_j)
 - Will resolve shared boundary problems
- Intersection has an integer X coordinate
 - if X_i is integer, we define it to be interior (fill)
 - if X_j is integer, we define it to be exterior (don't fill)

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Problem: Edge endpoint

- Intersection is an edge endpoint, say: (p_0, p_1, p_2) ??
- (p_0, p_1, p_1, p_2) , so we can still fill pairwise
- In fact, if we compute the intersection of the scanline with edge e_1 and e_2 separately, we will get the intersection point p_1 twice. Keep both of the p_1 .

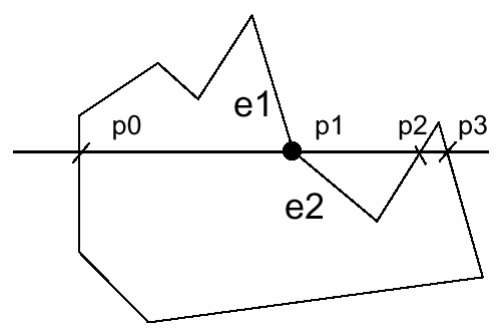


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Problem: Edge endpoint

- But what about this case: still (p_0, p_1, p_1, p_2)

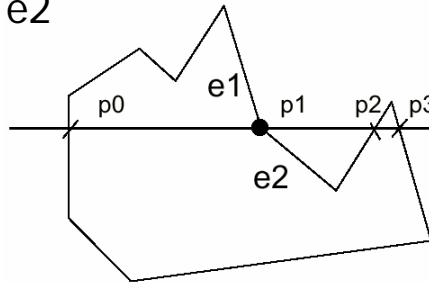


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Rule

- Rule:
 - If the intersection is the ymin of the edge's endpoint, count it. Otherwise, don't.
- Don't count p1 for e2

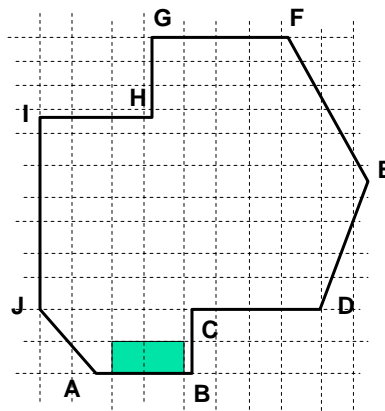


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Horizontal edges

- Need not be considered
- AB
 - A – intersection of JA
 - Parity becomes odd at A
 - B – intersection of BC
 - Parity becomes even at B
 - Hence AB is drawn

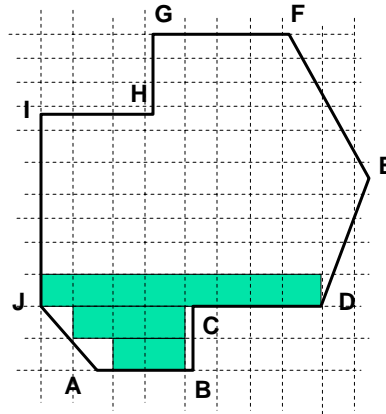


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Horizontal edges

- CD
 - J – intersection of IJ
 - Not of JA
 - Parity becomes odd at J
 - C – no change seen
 - Parity remains odd
 - D – intersection of ED
 - Parity changes to even
 - CD is drawn

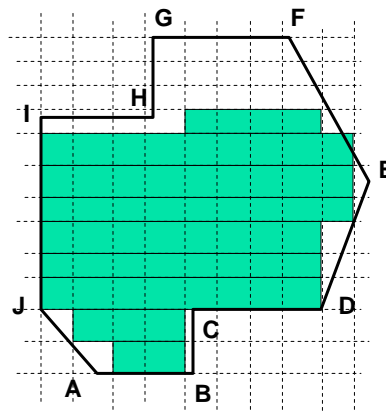


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Horizontal edges

- IH
 - I – no intersection of IJ
 - Parity remains even
 - H – intersection of GH
 - Parity becomes odd
 - IH is not drawn
 - But right span of IH is drawn

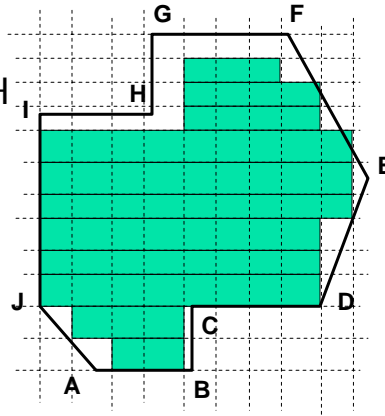


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Horizontal edges

- GF
 - G – no intersection of GH
 - Parity remains even
 - F – no intersection of FE
 - Parity becomes even
 - GF is not drawn



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Performance Improvement

- Brute force: intersect all the edges with all scanline
- Goal: compute the intersections more efficiently
 - find the ymin and ymax of each edge and intersect the edge only when it crosses the scanline
 - only calculate the intersection of the edge with the first scan line it intersects
 - calculate dx/dy
 - for each additional scanline, calculate the new intersection as $x = x + dx/dy$

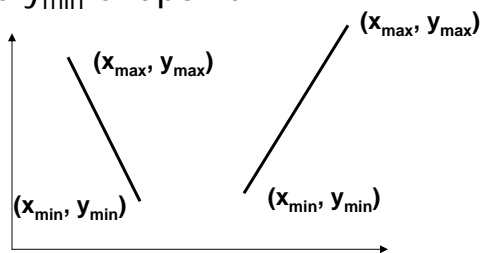
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Data Structure

Edge table: Bucket Sort

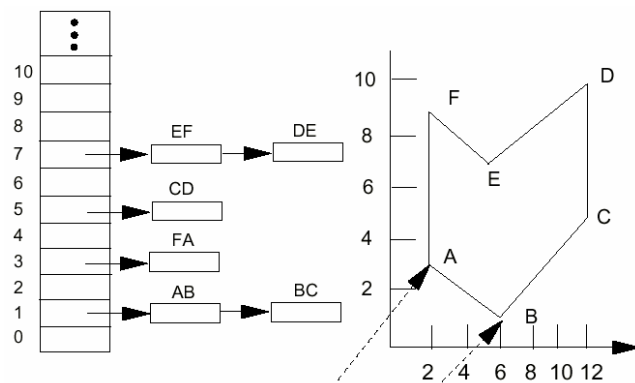
- A separate bucket for each scanline
- Each edge goes to the bucket of its y_{min} scanline
- Within each bucket, edges are sorted by increasing x of the y_{min} endpoint



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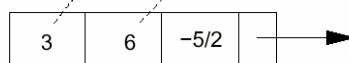
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Edge Table



- Edge structure: y_{max} , x_{min} , dx/dy , next

AB:

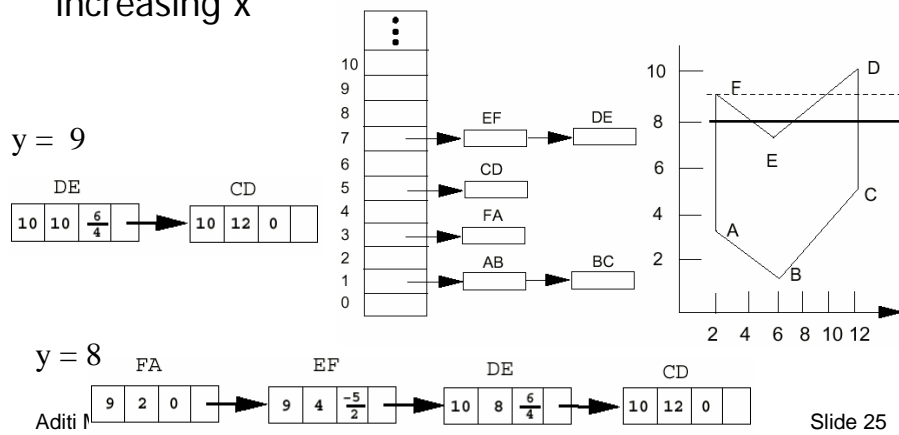


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Active Edge Table (AET)

- A list of edges active for current scanline, sorted in increasing x



Algorithm

```

Construct the Edge Table (ET);
Active Edge Table (AET) = null;
for y = Ymin to Ymax
    Merge-sort ET[y] into AET by x value
    for each edge in AET
        if edge.ymax = y
            remove edge from AET
    Fill between pairs of x in AET
    for each edge in AET
        edge.x = edge.x + dx/dy
    sort AET by x value
end scan_fill
    
```