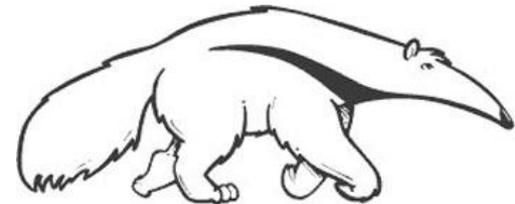


# Machine Learning and Data Mining

## Collaborative Filtering & Recommender Systems

Kalev Kask



# Recommender systems

- Automated recommendations
- Inputs
  - User information
    - Situation context, demographics, preferences, past ratings
  - Items
    - Item characteristics, or nothing at all
- Output
  - Relevance score, predicted rating, or ranking

# Recommender systems: examples

Your Amazon.com   Your Browsing History   Recommended For You   Amazon Betterizer   Improve Your Recommendations   Your

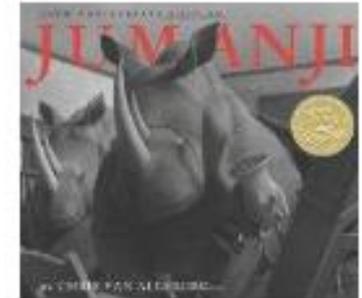
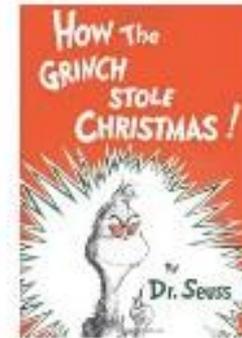
The screenshot shows the Netflix website with a navigation bar at the top. Below the navigation bar, there are several tabs: 'Browse DVDs', 'Watch Instantly', 'Your Queue', 'Movies You'll Love', 'Friends & Community', and 'DVD Sale \$5.99'. The 'Movies You'll Love' section is highlighted, showing 'Suggestions based on your ratings'. Below this, there are instructions: '1. Rate your genres.' and '2. Rate the movies you've seen.' with a star rating icon. The bottom part of the screenshot shows a Google search for 'restaurants' with results for 'California Fish Grill Inc', 'Bistango', 'Ruth's Chris Steak House', and 'Stonefire Grill'.

by telling us which things you like. This helps us provide

Show different items



Show my new re



[California Fish Grill Inc](#)

[cafishgrill.com/](#)

Score: **24** / 30 · 117 Google reviews

A 3988 Barranca Pkwy  
Irvine  
(949) 654-3838

[Bistango](#)

[www.bistango.com/](#)

Zagat: **25** / 30 · 247 Google reviews

B 19100 Von Karman Ave  
Irvine  
(949) 752-5222

[Ruth's Chris Steak House](#)

[www.ruthschris.com/](#)

Zagat: **27** / 30 · 75 Google reviews

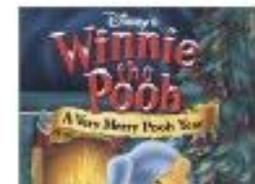
C 2961 Michelson Dr  
Irvine  
(949) 252-8848

[Stonefire Grill](#)

[www.stonefiregrill.com/](#)

Zagat: **23** / 30 · 47 Google reviews

D 3966 Barranca Pkwy  
Irvine  
(949) 777-1177



# Paradigms of recommender systems

Recommender systems reduce information overload by estimating relevance



**Recommendation  
system**



Item	score
I1	0.9
I2	1
I3	0.3
...	...

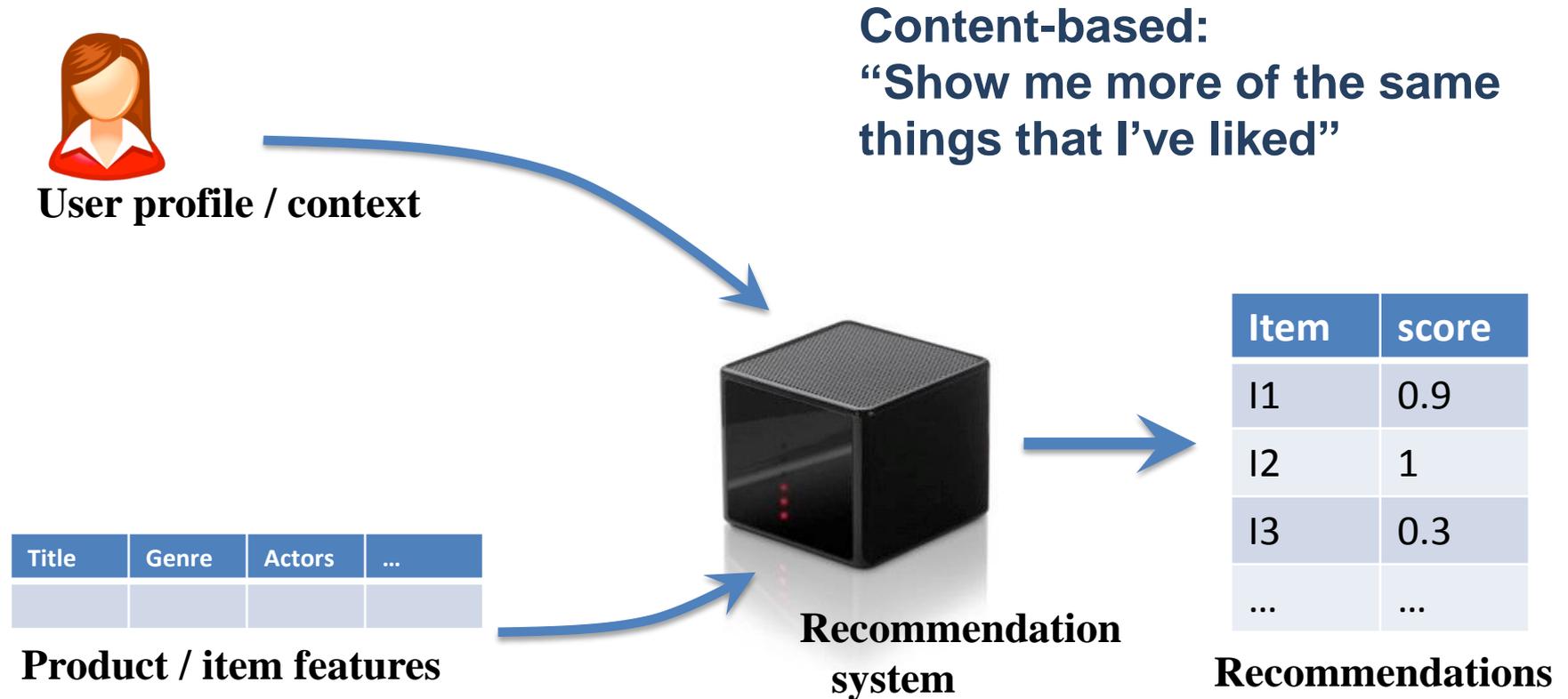
**Recommendations**

# Paradigms of recommender systems

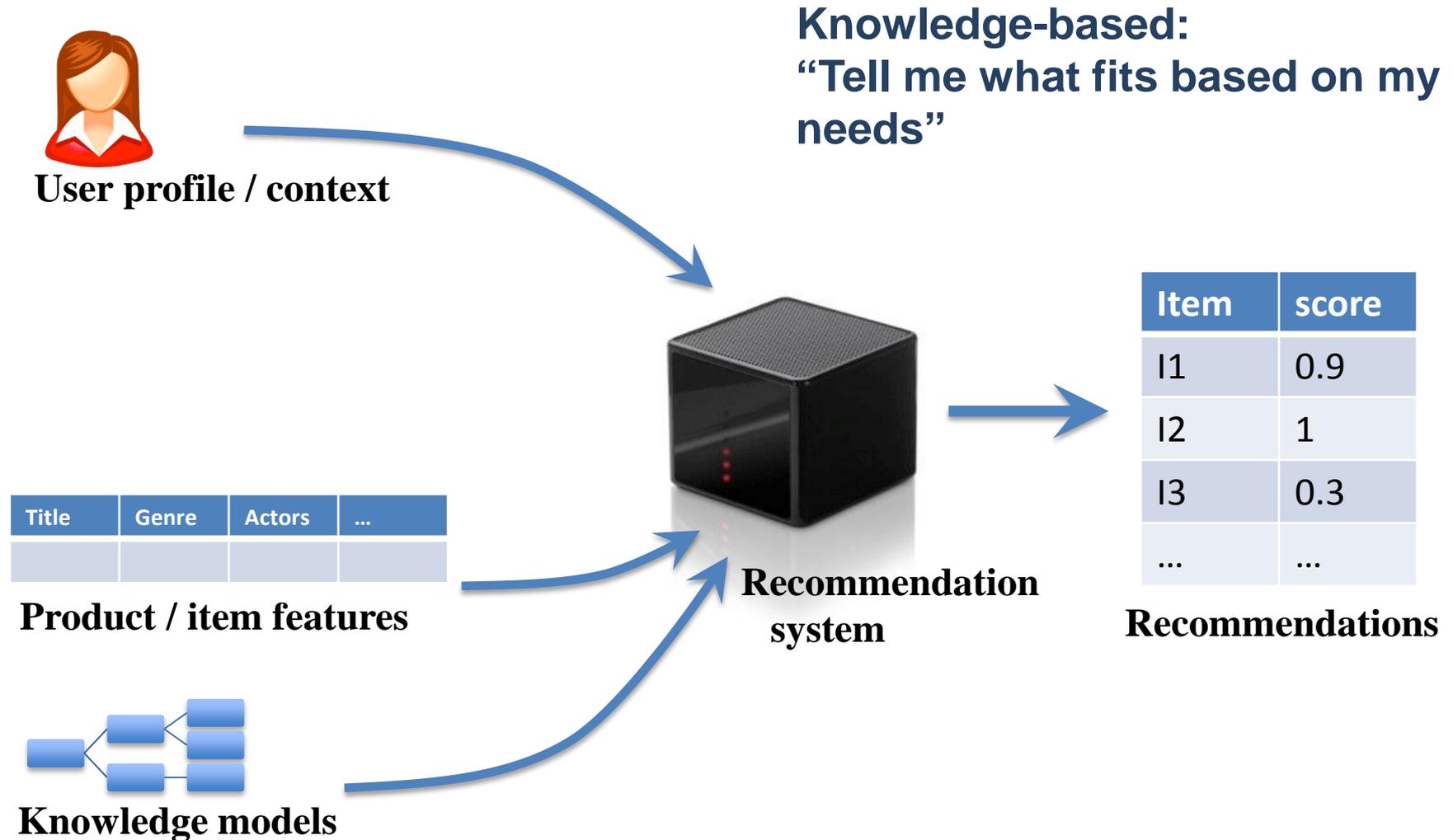
## Personalized recommendations



# Paradigms of recommender systems



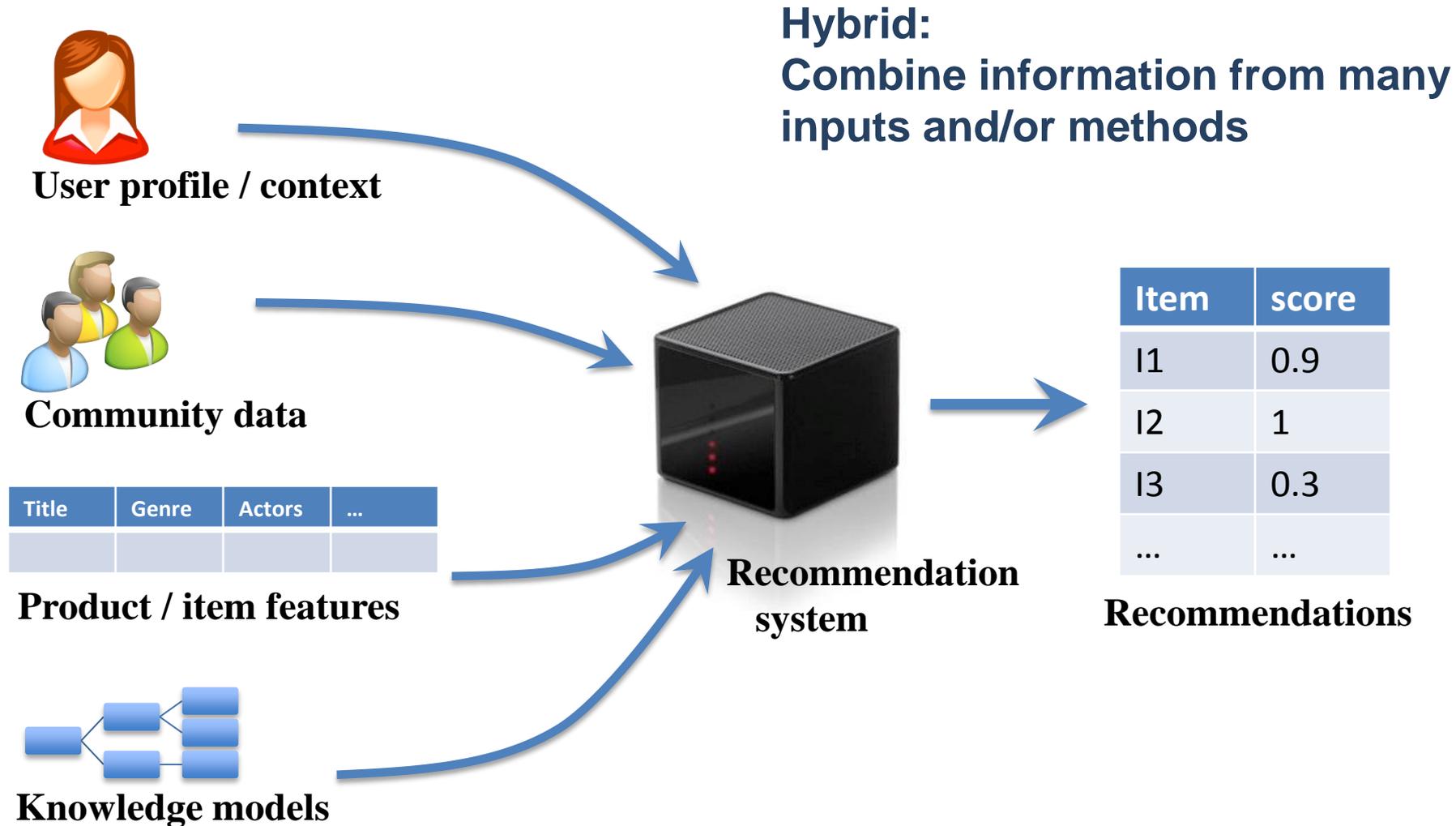
# Paradigms of recommender systems



# Paradigms of recommender systems



# Paradigms of recommender systems



# Measuring success

- **Prediction** perspective
  - Predict to what degree users like the item
  - Most common evaluation for research
  - Regression vs. “top-K” ranking, etc.
- **Interaction** perspective
  - Promote positive “feeling” in users (“satisfaction”)
  - Educate about the products
  - Persuade users, provide explanations
- **“Conversion”** perspective
  - Commercial success
  - Increase “hit”, “click-through” rates
  - Optimize sales and profits

# Why are recommenders important?

- The “long tail” of product appeal
  - A few items are very popular
  - Most items are popular only with a few people
- Goal: recommend not-widely known items that the user might like!



# Collaborative filtering

		users											
		1	2	3	4	5	6	7	8	9	1	1	1
movies	1	1		3		?	5			5		4	
	2			5	4			4			2	1	3
	3	2	4		1	2		3		4	3	5	
	4		2	4		5			4			2	
	5			4	3	4	2					2	5
	6	1		3		3			2			4	

# Collaborative filtering

- Simple approach: standard regression
  - Use “user features”  $u_{\sim}$ , “item features”  $i_{\sim}$
  - Train  $f(u_{\sim}, i_{\sim}) \approx r_{iu}$
  - Learn “users with my features like items with these features”
- Extreme case: per-user model / per-item model
- Issues: needs lots of side information!

Features:

*1 0 1 0 0 ...*

*0 0 1 0 0 ...*

*...*

movies

	users											
	1	2	3	4	5	6	7	8	9	10	11	12
1	1		3		?	5			5		4	
2			5	4			4			2	1	3
3	2	4		1	2		3		4	3	5	
4		2	4		5			4			2	
5			4	3	4	2					2	5
6	1		3		3			2			4	

# Collaborative filtering

- Example: nearest neighbor methods
  - Which data are “similar”?
- Nearby items? (based on...)

Features:

*1 0 1 0 0 ...*

*0 0 1 0 0 ...*

*...*

movies

	users											
	1	2	3	4	5	6	7	8	9	10	11	12
1	1		3		?	5			5		4	
2			5	4			4			2	1	3
3	2	4		1	2		3		4	3	5	
4		2	4		5			4			2	
5			4	3	4	2					2	5
6	1		3		3			2			4	

# Collaborative filtering

- Example: nearest neighbor methods
  - Which data are “similar”?
- Nearby items? (based on...)

Based on ratings alone?

Find other items that are rated similarly...

**Good match on observed ratings**

		users												
		1	2	3	4	5	6	7	8	9	10	11	12	
movies	1	1		3		?	5			5		4		
	2			5	4			4			2	1	3	
	3	2	4		1	2		3		4	3	5		
	4		2	4		5			4			2		
	5			4	3	4	2					2	5	
	6	1		3		3			2				4	

# Collaborative filtering

- Which data are “similar”?
- Nearby items?
- Nearby users?
  - Based on user features?
  - Based on ratings?

		users												
		1	2	3	4	5	6	7	8	9	10	11	12	
movies	1	1		3		?	5			5		4		
	2			5	4			4			2	1	3	
	3	2	4		1	2		3		4	3	5		
	4		2	4		5			4			2		
	5			4	3	4	2					2	5	
	6	1		3		3			2			4		

# Collaborative filtering

- Some **very simple** examples
  - All users similar, items not similar?
  - All items similar, users not similar?
  - All users and items are equally similar?

		users												
		1	2	3	4	5	6	7	8	9	10	11	12	
movies	1	1		3		?	5			5		4		
	2			5	4			4			2	1	3	
	3	2	4		1	2		3		4	3	5		
	4		2	4		5			4			2		
	5			4	3	4	2					2	5	
	6	1		3		3			2			4		

# Measuring similarity

- Nearest neighbors depends significantly on distance function
  - “Default”: Euclidean distance
- Collaborative filtering:
  - Cosine similarity:  $\frac{x^{(i)} \cdot x^{(j)}}{\|x^{(i)}\| \|x^{(j)}\|}$  (measures angle between  $x^{(i)}$ ,  $x^{(j)}$ )
  - Pearson correlation: measure correlation coefficient between  $x^{(i)}$ ,  $x^{(j)}$
  - Often perform better in recommender tasks
- Variant: weighted nearest neighbors
  - Average over neighbors is weighted by their similarity
- Note: with ratings, need to deal with missing data!

# Nearest-Neighbor methods

		users											
		1	2	3	4	5	6	7	8	9	10	11	12
movies	1	1		3		?	5			5		4	
	2			5	4			4			2	1	3
	<u>3</u>	2	4		1	2		3		4	3	5	
	4		2	4		5			4			2	
	5			4	3	4	2					2	5
	<u>6</u>	1		3		3			2			4	

**Neighbor selection:**  
**Identify movies similar to 1, rated by user 5**

# Nearest-Neighbor methods

		users											
		1	2	3	4	5	6	7	8	9	10	11	12
movies	1	1		3		?	5			5		4	
	2			5	4			4			2	1	3
	<u>3</u>	2	4		1	2		3		4	3	5	
	4		2	4		5			4			2	
	5			4	3	4	2					2	5
	<u>6</u>	1		3		3			2			4	

Compute similarity weights:

$$s_{13}=0.2, s_{16}=0.3$$

# Nearest-Neighbor methods

		users											
		1	2	3	4	5	6	7	8	9	10	11	12
movies	1	1		3		2.6	5			5		4	
	2			5	4			4			2	1	3
	<u>3</u>	2	4		1	2		3		4	3	5	
	4		2	4		5			4			2	
	5			4	3	4	2					2	5
	<u>6</u>	1		3		3			2			4	

Predict by taking weighted average:

$$(0.2*2+0.3*3)/(0.2+0.3)=2.6$$

# Latent space methods

From Y. Koren  
of BellKor team

		users											
		1	2	3	4	5	6	7	8	9	10	11	12
movies	1	1		3		?	5			5		4	
	2			5	4			4			2	1	3
	3	2	4		1	2		3		4	3	5	
	4		2	4		5			4			2	
	5			4	3	4	2					2	5
	6	1		3		3			2			4	

$X_{N \times D} \approx U_{N \times K} S_{K \times K} V^T_{K \times D}$

# Latent Space Models

From Y. Koren  
of BellKor team

Model ratings matrix as  
“user” and “movie”  
positions

Infer values from known  
ratings

		users										
items	1		3			5			5		4	
			5	4			4			2	1	3
	2	4		1	2		3		4	3	5	
			2	4		5		4			2	
				4	3	4	2				2	5
1		3		3			2			4		

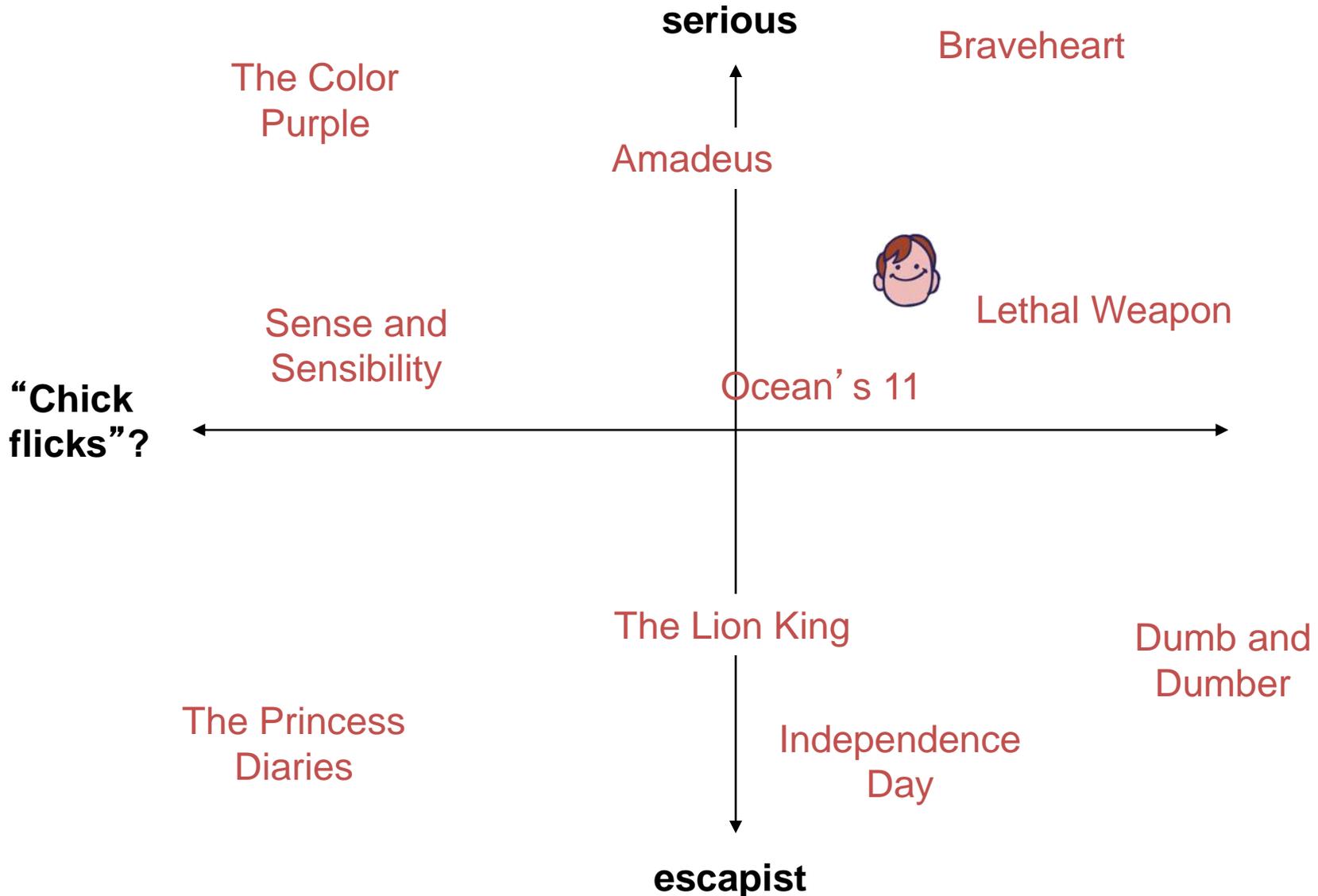
~

Extrapolate to unranked

		users													
items	1	.1	-.4	.2											
		-.5	.6	.5											
	2	-.2	.3	.5											
		1.1	2.1	.3											
		-.7	2.1	-.2											
	1	-.1	.7	.3											
		users													
		1.1	-.2	.3	.5	-.2	-.5	.8	-.4	.3	1.4	2.4	-.9		
		-.8	.7	.5	1.4	.3	-1	1.4	2.9	-.7	1.2	-.1	1.3		
		2.1	-.4	.6	1.7	2.4	.9	-.3	.4	.8	.7	-.6	.1		

# Latent Space Models

From Y. Koren  
of BellKor team



# Some SVD dimensions

See [timelydevelopment.com](http://timelydevelopment.com)

## Dimension 1

Offbeat / Dark-Comedy

Lost in Translation

The Royal Tenenbaums

Dogville

Eternal Sunshine of the Spotless Mind

Punch-Drunk Love

Mass-Market / 'Beniffer' Movies

Pearl Harbor

Armageddon

The Wedding Planner

Coyote Ugly

Miss Congeniality

## Dimension 2

Good

VeggieTales: Bible Heroes: Lions

The Best of Friends: Season 3

Felicity: Season 2

Friends: Season 4

Friends: Season 5

Twisted

The Saddest Music in the World

Wake Up

I Heart Huckabees

Freddy Got Fingered

House of 1

## Dimension 3

What a 10 year old boy would watch

Dragon Ball Z: Vol. 17: Super Saiyan

Battle Athletes Victory: Vol. 4: Spaceward Ho!

Battle Athletes Victory: Vol. 5: No Looking Back

Battle Athletes Victory: Vol. 7: The Last Dance

Battle Athletes Victory: Vol. 2: Doubt and Conflic

What a liberal woman would watch

Fahrenheit 9/11

The Hours

Going Upriver: The Long War of John Kerry

Sex and the City: Season 2

Bowling for Columbine

# Latent space models

- Latent representation encodes some “meaning”
- What kind of movie is this? What movies is it similar to?
- Matrix is full of missing data
  - Hard to take SVD directly
  - Typically solve using gradient descent
  - Easy algorithm (see Netflix challenge forum)

$$J(U, V) = \sum_{u,m} (X_{mu} - \sum_k U_{mk} V_{ku})^2$$

# for user u, movie m, find the kth eigenvector & coefficient by iterating:

```
predict_um = U[m,:].dot( V[:,u] )      # predict: vector-vector product
err = ( rating[u,m] - predict_um )     # find error residual
V_ku, U_mk = V[k,u], U[m,k]           # make copies for update
U[m,k] += alpha * err * V_ku           # Update our matrices
V[k,u] += alpha * err * U_mk           # (compare to least-squares gradient)
```

# Latent space models

- Can be a bit more sophisticated:

$$r_{iu} \approx \mu + b_u + b_i + \sum_k W_{ik} V_{ku}$$

- “Overall average rating”
  - “User effect” + “Item effect”
  - Latent space effects (k indexes latent representation)
  - (Saturating non-linearity?)
- Then, just train some loss, e.g. MSE, with SGD
    - Each (user, item, rating) is one data point
    - E.g.  $J = \sum_{iu} (X_{iu} - r_{iu})^2$

# Ensembles for recommenders

---

- Given that we have many possible models:
  - Feature-based regression
  - (Weighted) kNN on items
  - (Weighted) kNN on users
  - Latent space representationperhaps we should combine them?
- Use an ensemble average, or a stacked ensemble
  - “Stacked” : train a weighted combination of model predictions