

GAISE Workshop

Session 3

Nov. 8, 2005

3:30 – 5:30 pm

Brian Smith

**Using technology for developing concepts
and analyzing data**

Uses of Technology

➤ **Super calculator/Number cruncher**

- In this mode the use of technology allows the student to move from solving problems with small samples to analyzing large, realistic data sets.
- Low level of conceptual understanding.

➤ **Grapher**

- Assists in visualization of data, exploration of concepts of central tendency and variability, shape of distribution (symmetric? unimodal? normal?)
- Medium level of conceptual understanding

➤ **Interactive Explorer**

- Integrates numerical measures and graphs into an interactive package that permits exploration, visualization, and active learning.
- High level of conceptual understanding

In this session we will investigate five technologies:

- 1) Excel
- 2) Minitab
- 3) Fathom
- 4) TI-83/84
- 5) Java Applets

A brief word about the advantages and limitations of each technology:

Excel is a superb number cruncher but its statistical capabilities are limited. Doubt has been cast on its random number generator for large scale commercial and scientific applications, but it is adequate for educational purposes. Several add-ins that add extra statistical features and improve user interface are available, and are often included with text books. Major disadvantage in the classroom is that many statistical procedures are not supported and it takes time and effort to program one's own applications.

Minitab is a true statistical package with a large number of built-in statistical procedures. Many applications that are very limited in Excel are automatically available in Minitab, and in particular the ability to generate graphs to accompany procedures is useful. Solves large scale problems easily, has an intuitive Windows based user-friendly interface, and a relatively short learning curve. It also has the advantage that it is a serious statistical package that can be used for commercial applications as well as being an effective educational tool.

Fathom is an original and highly effective package for interactive exploration. It is an educational, pedagogical package and encourages independent investigation of the relationships between variables. It includes a superb collection of real data, including U.S. census data, for use by students, and also incorporates a number of useful interactive demonstrations that can be employed by the instructor for illustrating statistical concepts. Fathom's interface is different from the point-and-click environment that we have come to expect from the Window's based applications, but when you get used to it, Fathom is easy to use and requires little time and effort for the instructor who wishes to demonstrate statistical concepts.

The TI-83/84 has the major advantage of being inexpensive and portable – essentially it puts major computing power into the hands of every student. Numerical output and graphical are limited by the screen size and the quality of the graphics, but nevertheless the universality of the calculators makes them a useful and effective tool for both numerical computation and graphical explorations.

Applets are small applications that are intended to demonstrate one concept e.g. Central Limit Theorem. There are many applets online and the user should carefully check them out before using them in class – they are not all of uniform quality. But there are some sites which are highly reliable and have effective applets. It is often useful to pause for a few minutes in a class to pull up an applet to illustrate a particular concept – and then tell students to continue to explore the applet, and the underlying concept, in out-of-class time.

Excel

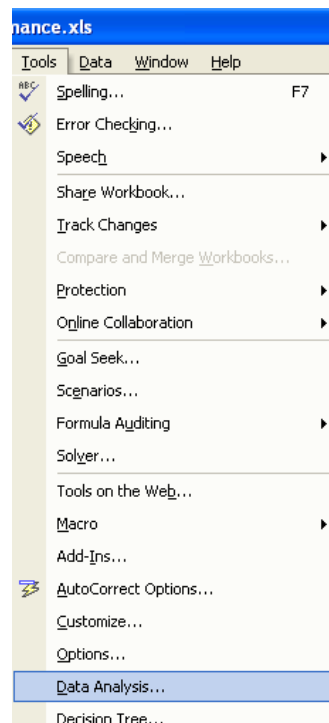
The following data ,obtained from the DASL website, shows long jump records for the Olympic games from 1900 (Year = 0) to 1984 (Year = 84).

Long jump	year
282.88	0
289.00	4
294.50	8
299.25	12
281.50	20
293.13	24
304.75	28
300.75	32
317.31	36
308.00	48
298.00	52
308.25	56
319.75	60
317.75	64
350.50	68
324.50	72
328.50	76
336.25	80
336.25	84

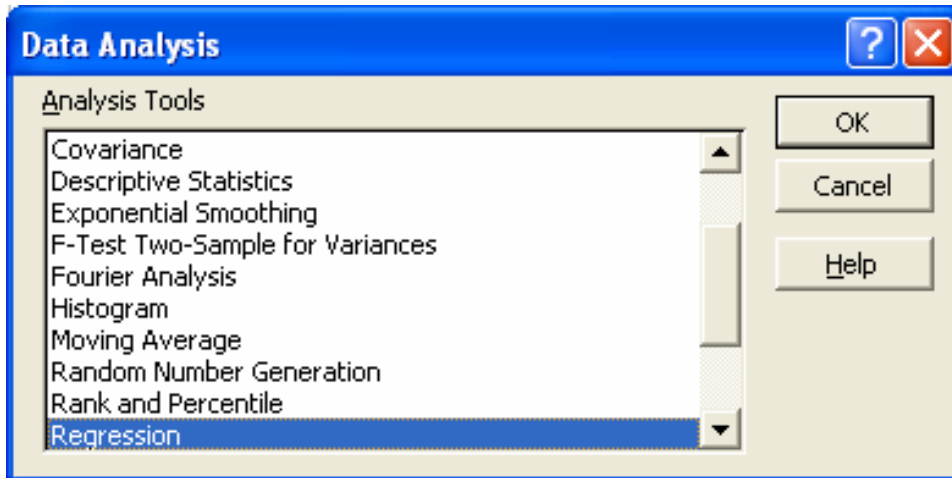
Level 1 use of Excel: supercalculator

To perform a **Simple Linear Regression** in Excel:

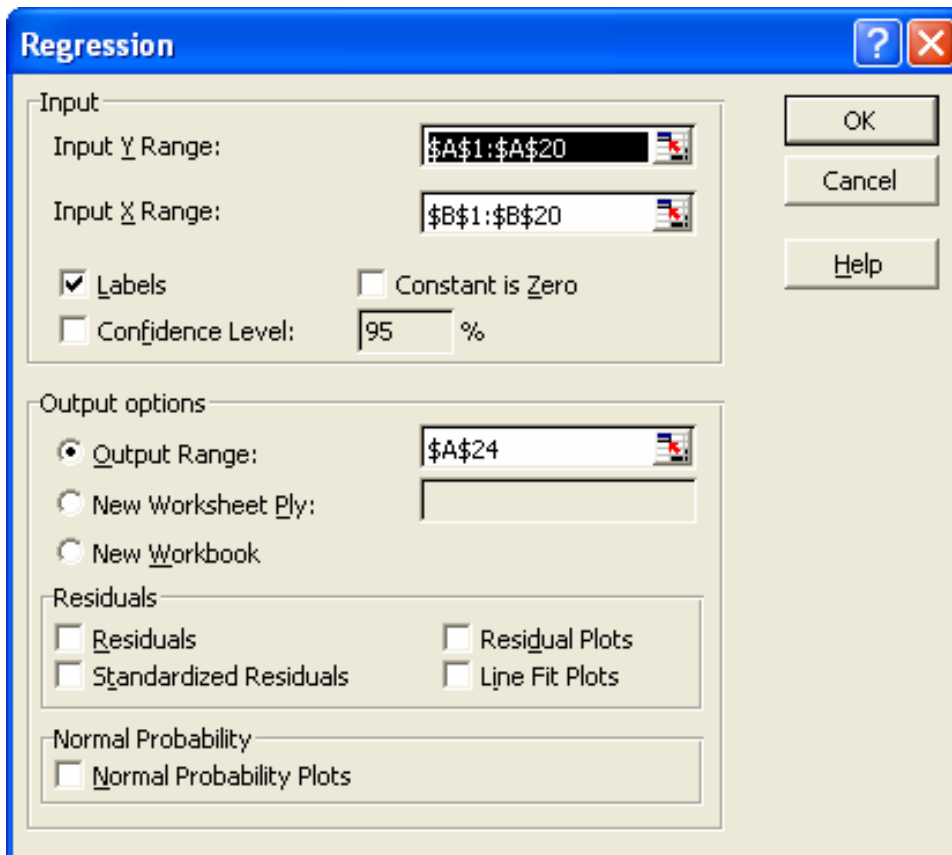
Click on Tools ☐ Data Analysis



Select Regression from the menu



Complete the dialog box (be sure to check the “labels” box!):



Click on OK to obtain the following output:

SUMMARY OUTPUT

<i>Regression Statistics</i>	
Multiple R	0.8703
R Square	0.7575
Adjusted R Square	0.7432
Standard Error	9.7568
Observations	19

ANOVA

	<i>df</i>	<i>SS</i>	<i>MS</i>	<i>F</i>	<i>Significance F</i>
Regression	1	5054.89	5054.89	53.10	1.27001E-06
Residual	17	1618.33	95.20		
Total	18	6673.22			

	<i>Coefficients</i>	<i>Standard Error</i>	<i>t Stat</i>	<i>P-value</i>	<i>Lower 95%</i>	<i>Upper 95%</i>
Intercept	283.45	4.28	66.22	0.00000000	274.42	292.49
Year	0.6131	0.0841	7.2870	1.2700E-06	0.4356	0.7906

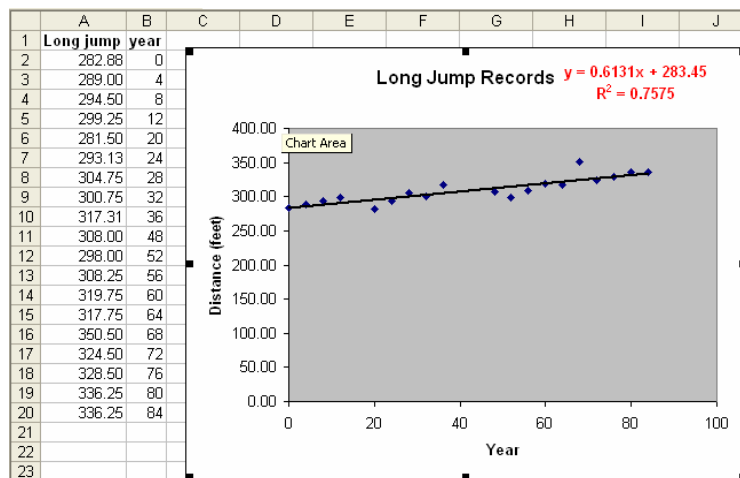
The regression equation is $\hat{Y} = \beta_0 + \beta_1 X = 283.45 + 0.6131X$.

We see that in the test of hypothesis $H_0: \beta_1 = 0$ the p -value is 1.2700E-06 (compare with TI-84) and we conclude *Reject H_0* , i.e. conclude that there is a linear relationship between length and year.

Further, we note that a 95% confidence interval for β_1 is $0.4356 \leq \beta_1 \leq 0.7906$.

Level 2 use of Excel: grapher

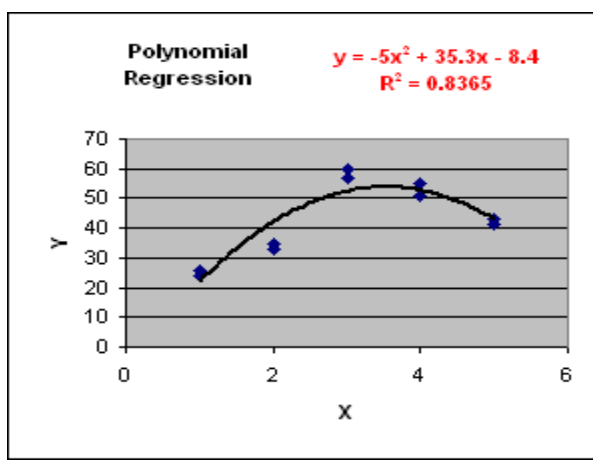
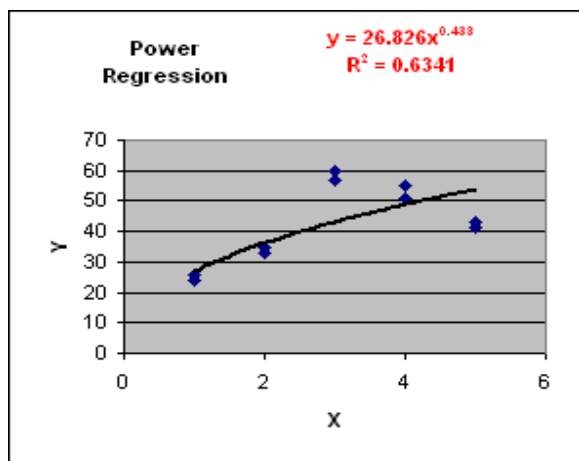
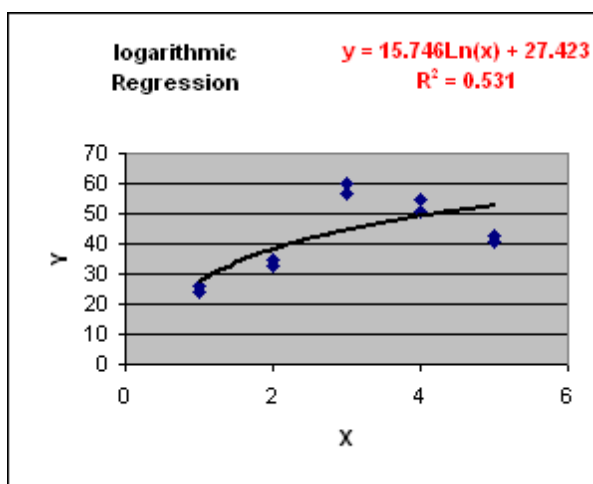
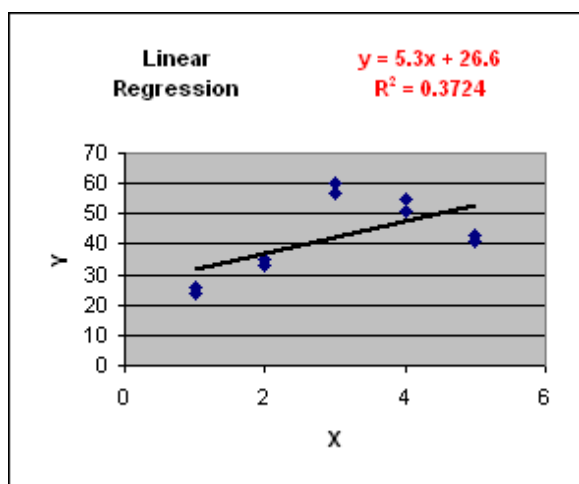
Use the Chart Wizard feature to draw a scatter diagram and superimpose a linear regression on the diagram, specifying the linear regression equation and the R^2 value.



Level 3 use of Excel: Interactive

Explore the relationship between X and Y for the following data

<u>X</u>	<u>Y</u>
1	24
1	26
2	35
2	33
3	57
3	60
4	55
4	51
5	43
5	41

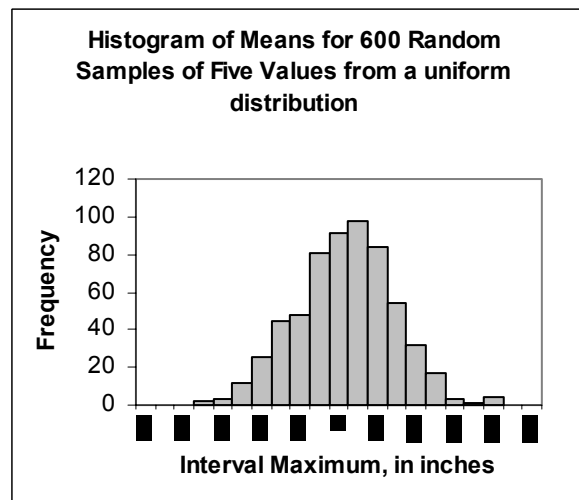
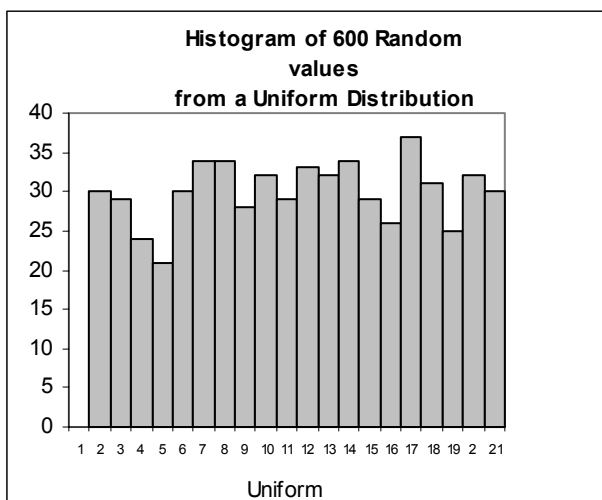


Experiment: Change one of the Y-values in the table and see the effect on the four graphs! For example, change the first Y-value from 24 to 200.
Note: The graph is updated but the regression equations and R^2 values are not! It is necessary to delete these values and recompute

Simulating the Central Limit Theorem in Excel

The Scenario

Consider a production process where the actual lengths of metal pipes produced vary uniformly Between 19.5 and 20.5 cm. At regular intervals a random sample of five pipes is selected and the mean length is recorded. After 600 samples have been selected, the distribution of the sample means is plotted. Even though the population values are uniformly distributed and the sample size is small, we see that the distribution of sample means is approximately normal.

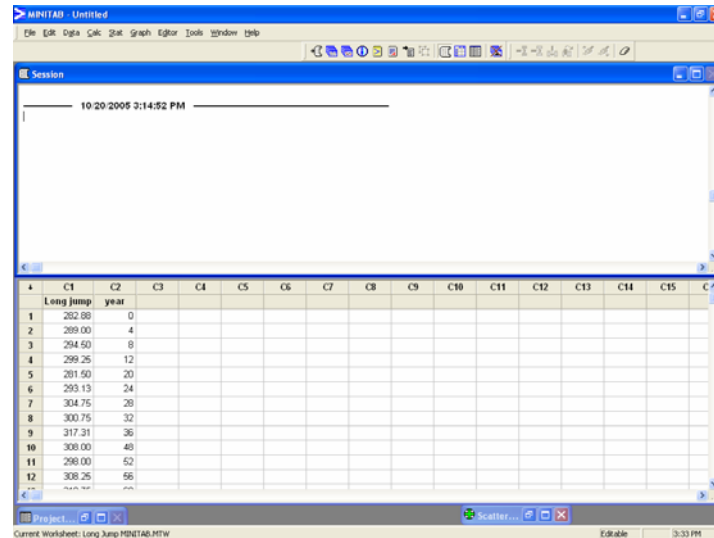


The ability to produce plots and to regenerate them interactively is based on the fact that the `Rand()` function in Excel, which generates a random number from a uniform distribution between 0 and 1, is automatically renewed every time the *recalculate* key (F9) is pressed.

The formula `{=FREQUENCY(G3:G602,H2:H22)}` is used to create the histogram. Every time the F9 function key is pressed the two graphs are regenerated. It is a nice demonstration of the fact that while 600 values of the original variable (length of metal pipe) is uniformly distributed in the range 19.5 to 20.5, the means of 600 samples of 5 metal pipes is approximately normally distributed.

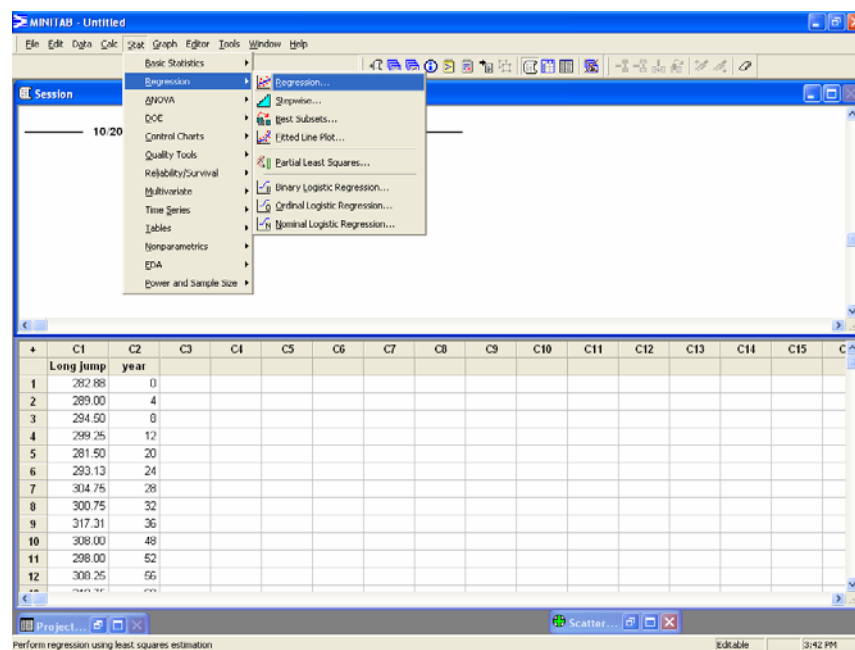
Minitab

We will show how Minitab can be used to analyze the long jump data:

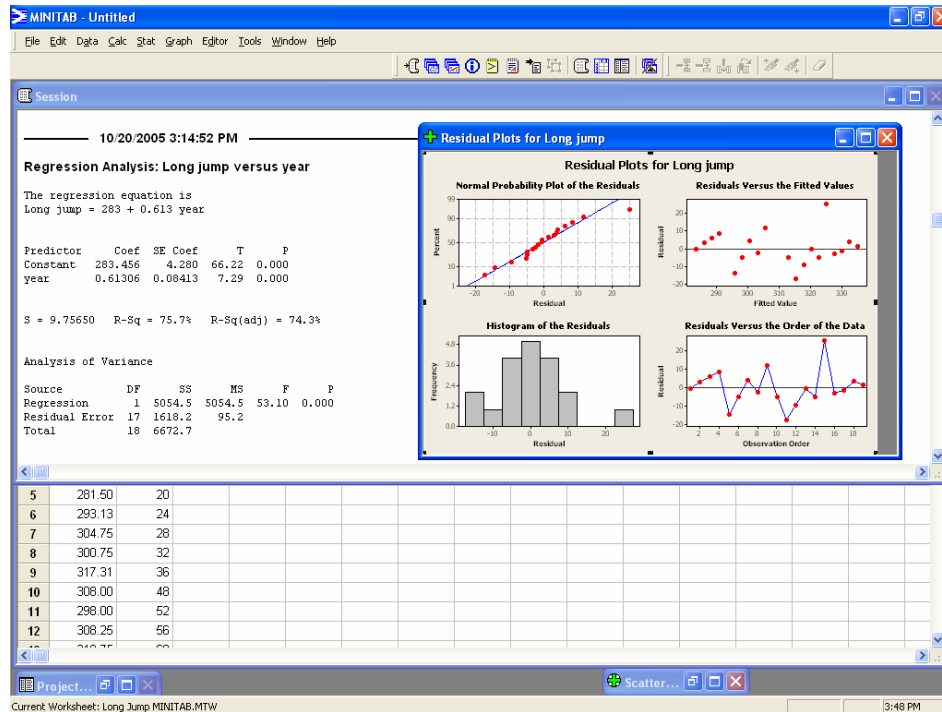


Notice that the Minitab screen is divided into a *session window* (top half) and the *data window* (lower half). The data window is basically a spreadsheet and data can be exchanged with Excel by cutting and pasting. The long jump data is already stored in the data window.

To perform a regression analysis select *Stat > Regression > Regression* as shown below:

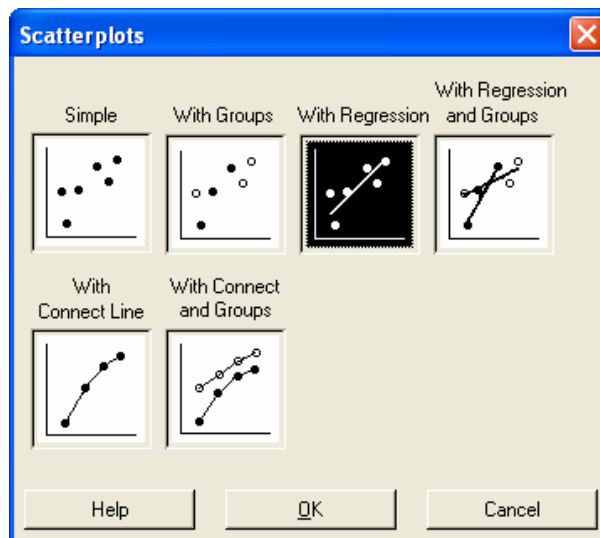


Running the regression analysis and selecting the “*Four in One*” option from the *Graphs* menu, we get the following results:

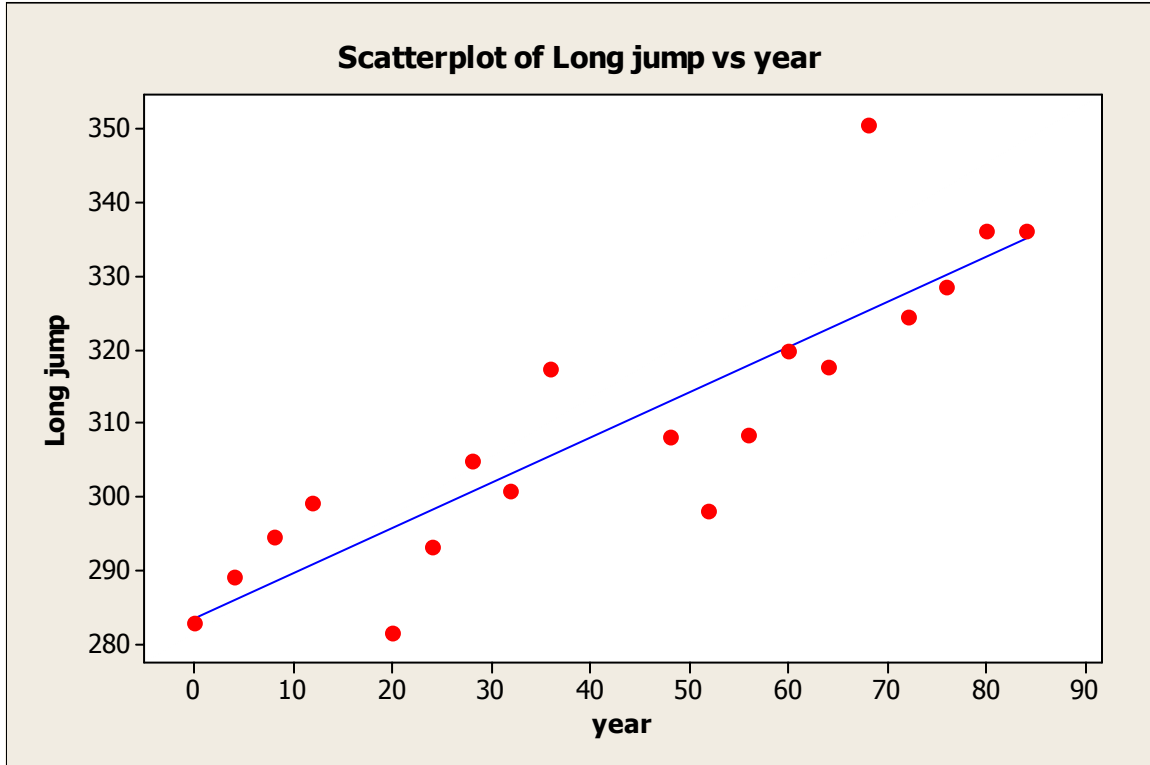


Notice that this output includes not only the regression equation and the ANOVA table for the regression, but also four graphs which can be useful for testing regression assumptions (e.g. normal distribution of residuals, equal variances, etc.)

To generate a scatter diagram select *Graph > Scatterplot*



and choose the “*With Regression*” option from the dialog box above. The scatterplot appears below:



Repeating analysis we have already performed in Excel:

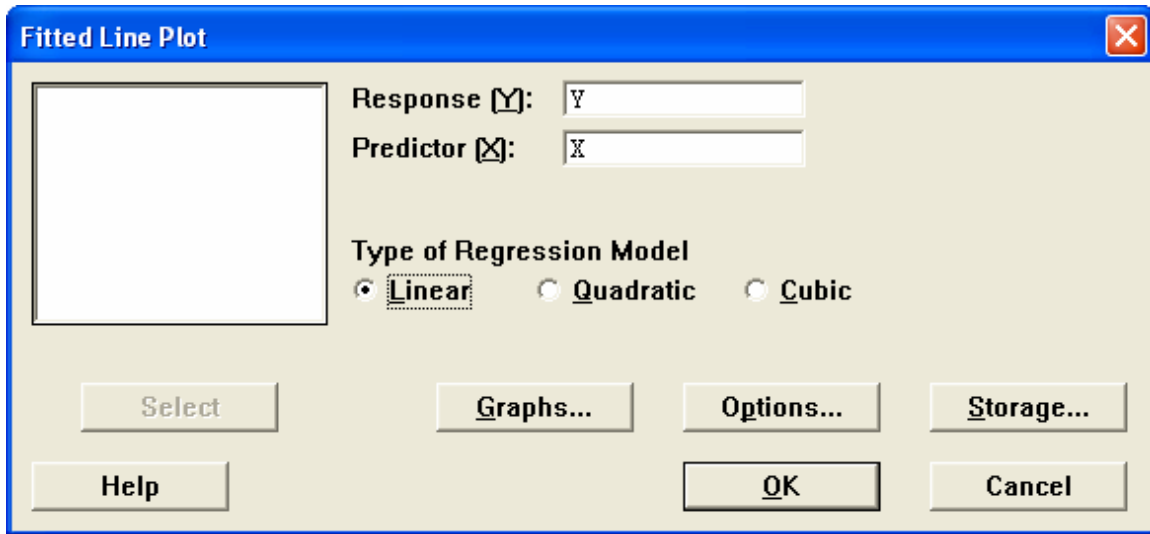
Explore the relationship between X and Y for the following data

<u>X</u>	<u>Y</u>
1	24
1	26
2	35
2	33
3	57
3	60
4	55
4	51
5	43
5	41

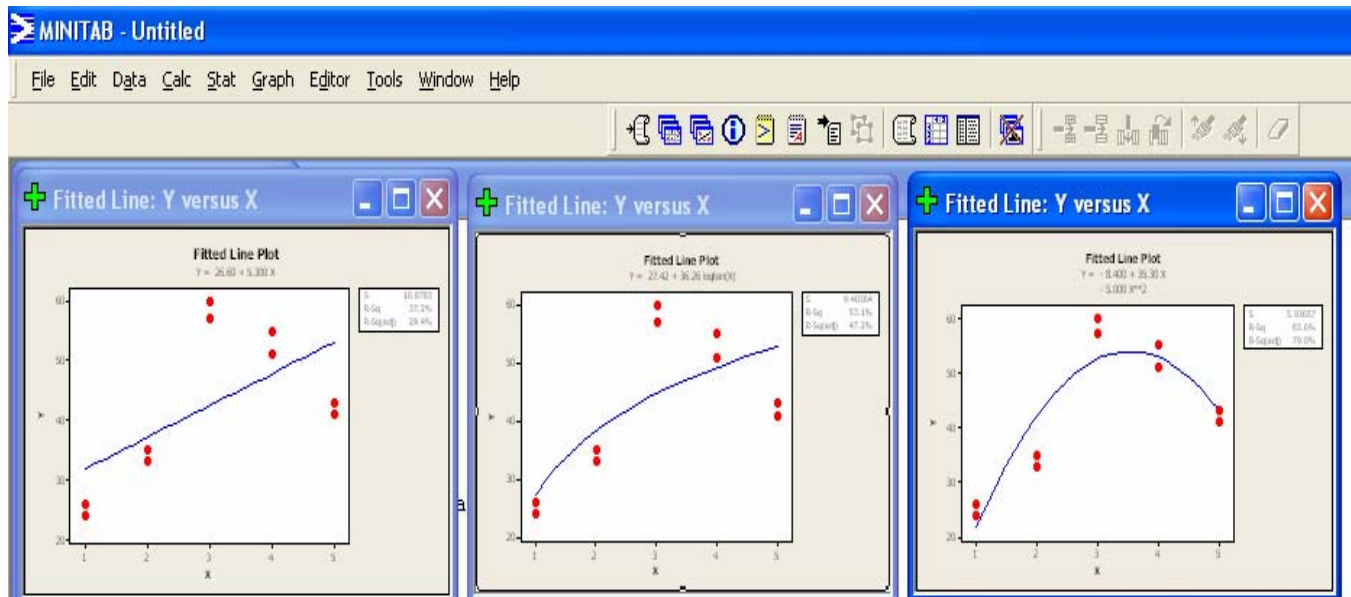


Select *Stat > Regression > Fitted Line Plot*.

Select the Type of Regression Model from the screen below:



We can produce the following graphs:



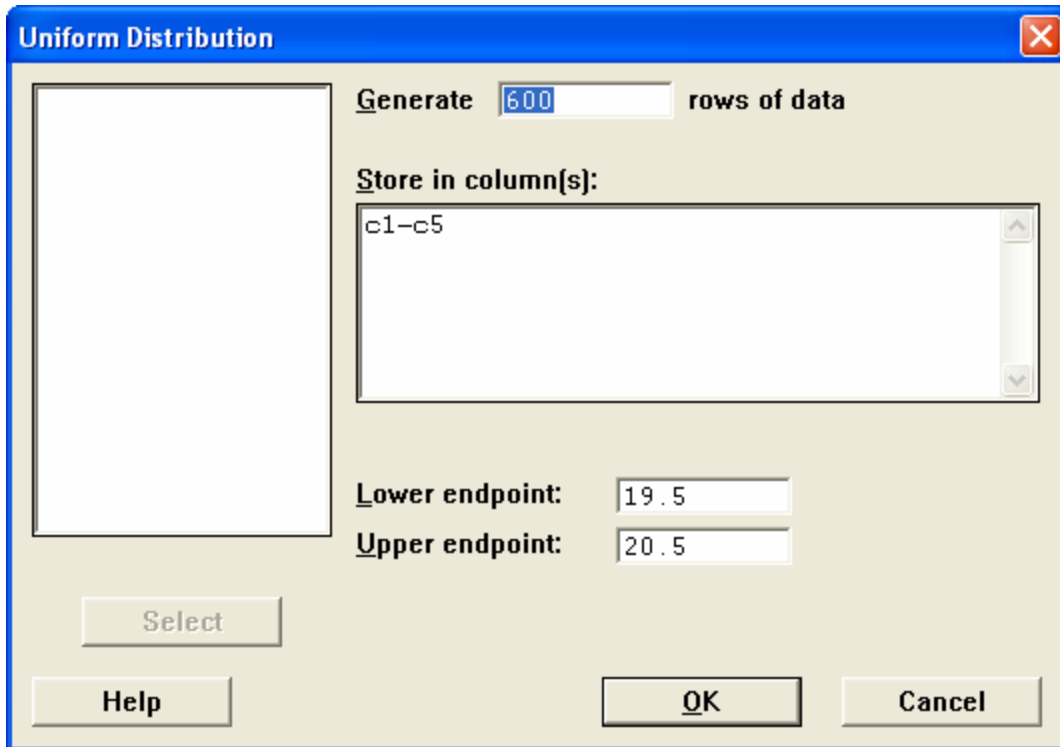
These graphs are the same as the ones produced using Excel.

Central Limit Theorem Simulation in Minitab

Repeat the process of generating 600 samples of 5 random values uniformly distributed between 19.5 and 20.5.

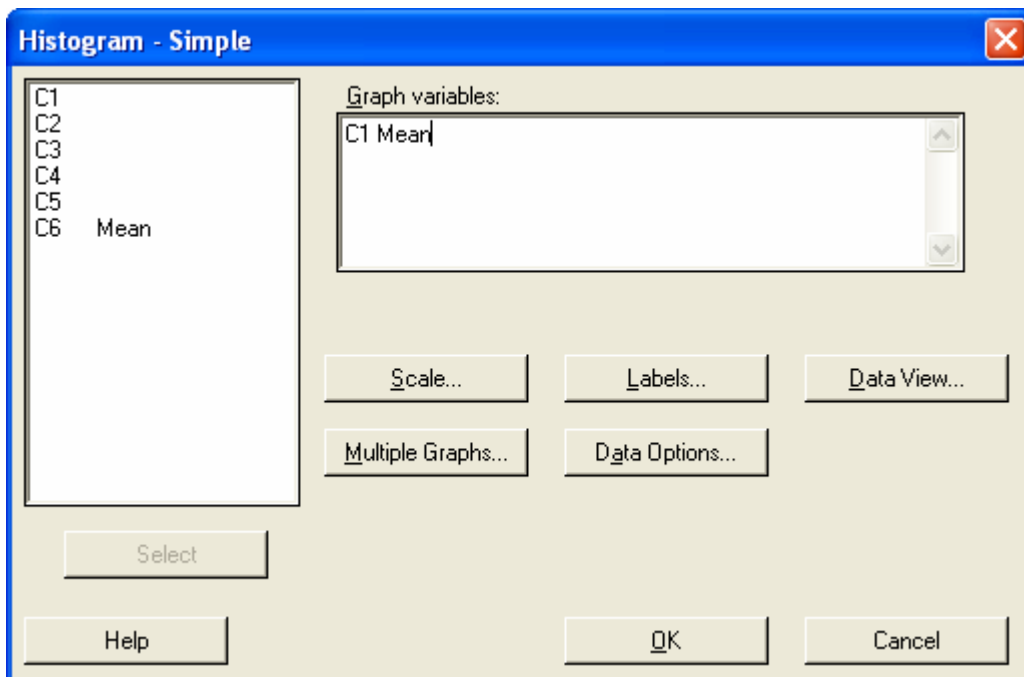
Select *Calc > Random Data > Uniform*

Complete the following screen:

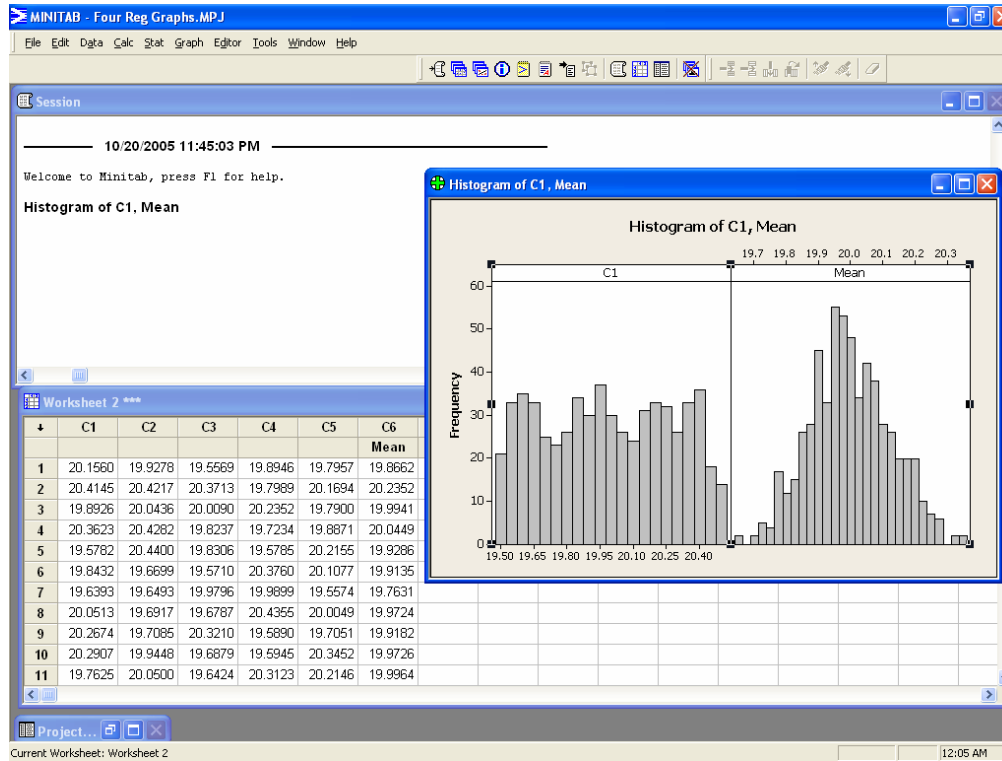


Next, graph one column of 600 values of the uniform distribution, and also graph the 600 values of the means of samples of size 5:

Select *Graph > Histogram* and complete the dialog box:



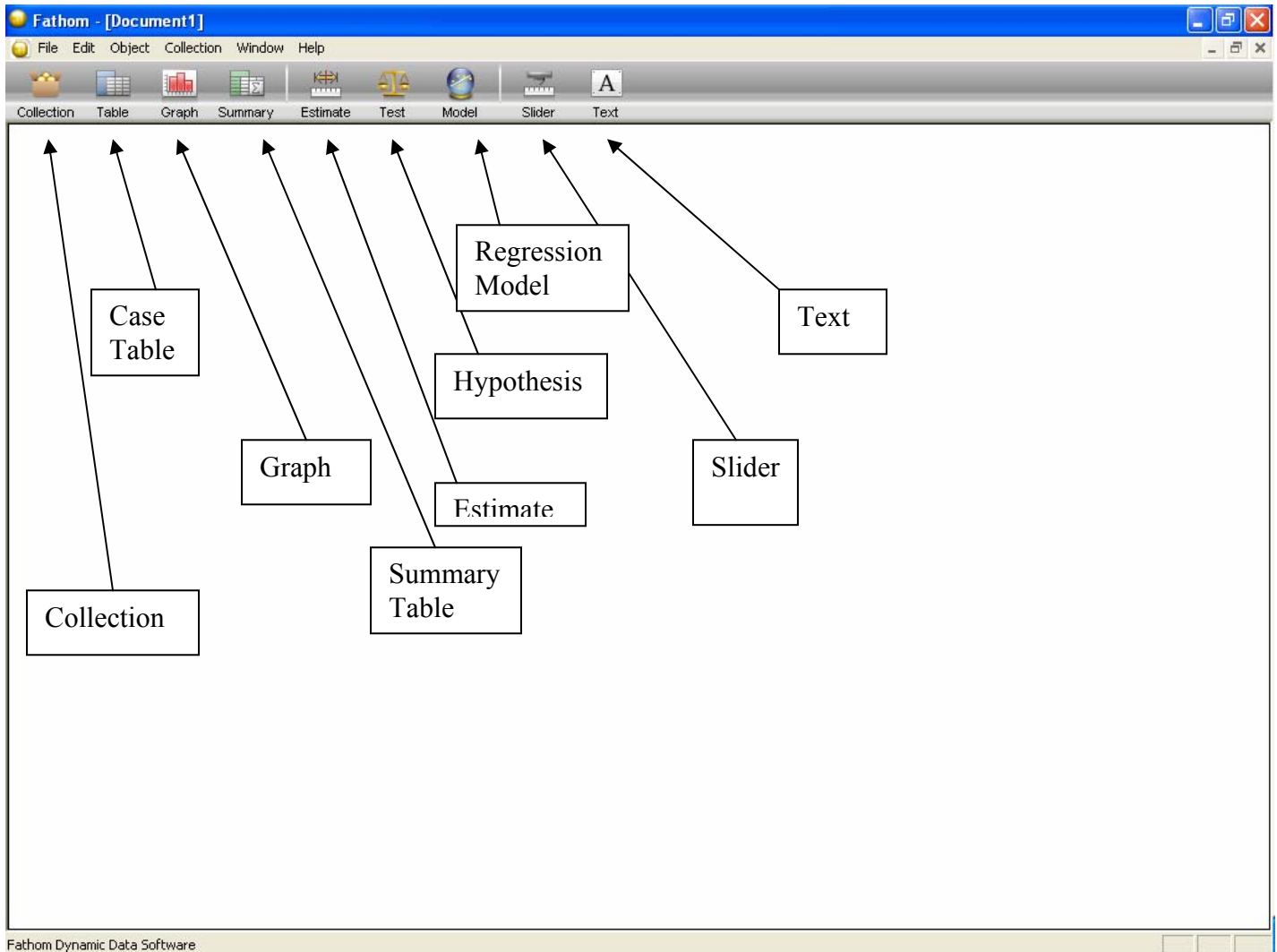
You will see the two graphs below:



Once again we see that the histogram of the original values is uniformly distributed while the mean values are approximately normally distributed.

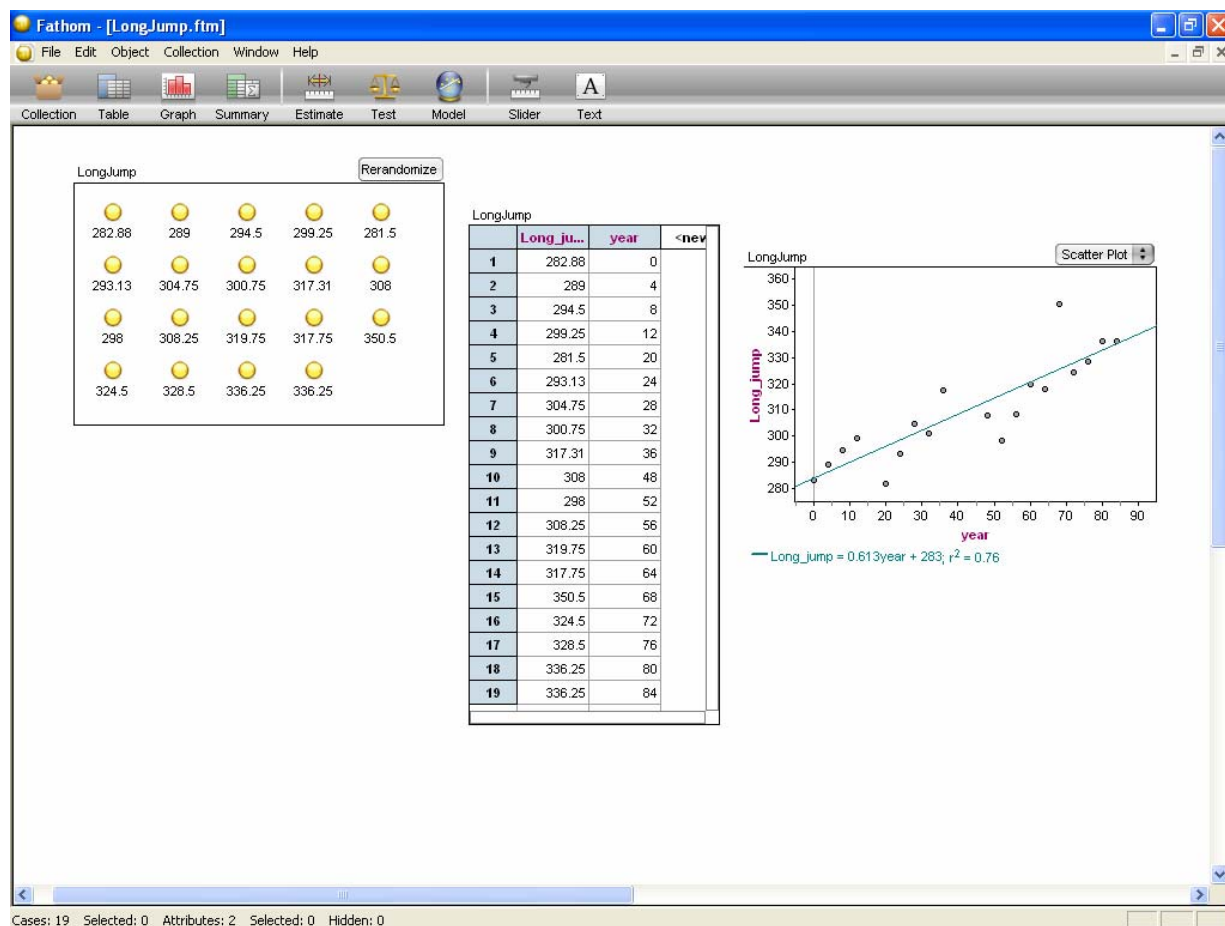
Fathom

Anatomy of a screen in Fathom 2™ Dynamic Data Software



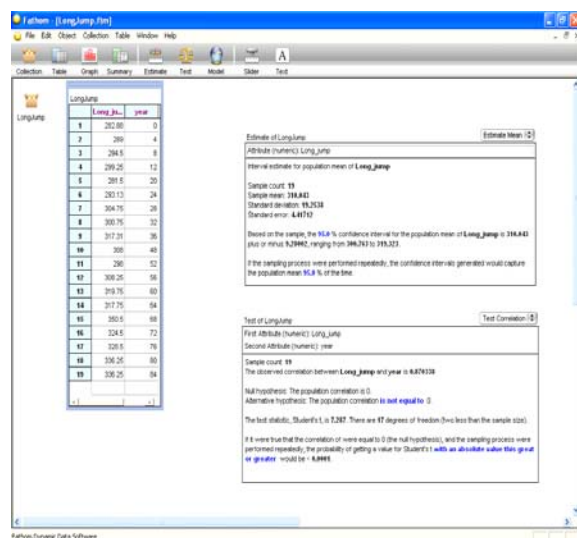
The following screen shows three elements of a Fathom analysis for the long jump data:

- (1) the collection
- (2) the case table
- (3) a graph (scatter plot with least squares regression line).

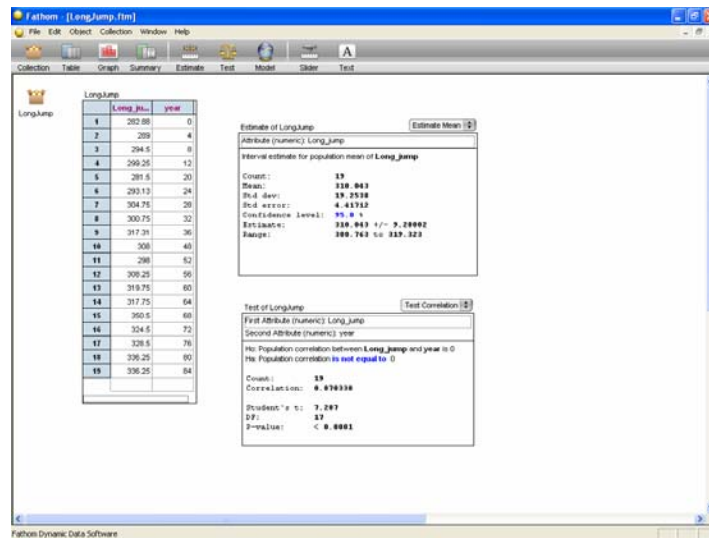


Each of the elements above can be dragged into the document.

The next screen shows (1) a confidence interval for the mean distance jumped and (2) a test of hypothesis for the correlation between distance and year.



Exercise: repeat the confidence interval and test of hypothesis with *Verbose* toggled off.

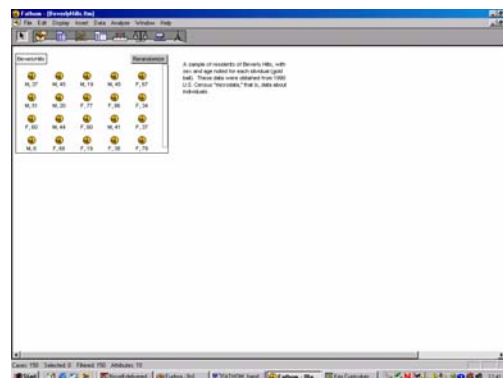


Exercise 1: Exploring Data

We use the file BeverlyHills to explore the data graphically.

- Investigate various graphs and see the impact of selecting an observation on all open graphs and the inspector.
- Investigate a scatter diagram of Income on Age
- Restrict age range (filter) to 18 – 80.
- See impact of the filter on the regression line.
- Then try age range 18 - 55

File → Open → Sample Documents → Learning Starter Guides → BeverlyHills



The screen displays two entities:

1. A “collection”
2. A text box describing the collection

Each gold ball in the collection represents one case.

When the cursor is placed over the collection the status bar in the bottom left-hand corner of the screen indicates that the collection has 150 cases and 10 attributes (variables).

To explore the attributes double click the collection. You will see the Inspector screen as below:

By clicking on a gold ball in the collection you can inspect the attributes for that case in the Inspector. The screen below shows the attributes for the 2nd case in the collection. Note that it is necessary to resize the Inspector to see the full description of some of the attributes.

Inspect BeverlyHills		
Cases	Measures	Comments
Attribute	Value	Formula
sex	M	
age	45	
race	White	
ancestry	Israeli	
marital	Mar	
eduCode	11	
eduText	Some col...	
income	32734	
industry	Machiner...	
job	Electricia...	
<new>		

Inspect BeverlyHills		
Cases	Measures	Comments
Attribute	Value	Formula
sex	M	
age	45	
race	White	
ancestry	Israeli	
marital	Mar	
eduCode	11	
eduText	Some college, but no degree	
income	32734	
industry	Machinery manufacturing, except electrical, n.e.c.	
job	Electrician earning \$13191. Unearned income: \$19543.	
<new>		

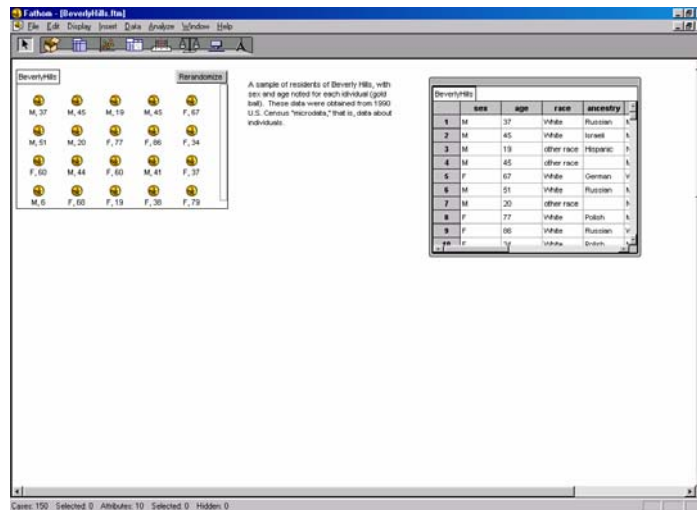
Click on the **Comments** tab and you will see the description of the data set. This is a good place to store documentation and notes about the data.

Close the Inspector by clicking its close box.

For spreadsheet fans!

Click on the collection to select it (you will see a border around it).

To create a **Case Table** (spreadsheet), choose **Case Table** from the **Insert** menu or drag a new **Case Table** into the document.



The **Case Table** can be enlarged by dragging on a bottom corner of the table.

To see the full table we close the text box, shrink the collection until it is “iconized” and enlarge the **Case Table** by dragging on a bottom corner of the table.

	sex	age	race	ancestry	marital	eduCode	eduText	income	industry	job	<ne
1	M	37	White	Russian	Mar	14	Bachelor...	0	Scrap an...	Sales rep...	
2	M	45	White	Israeli	Mar	11	Some coll...	32734	Machiner...	Electricia...	
3	M	19	other race	Hispanic	Nev	9	12th grad...	0	Retail bak...	Baker, bu...	
4	M	45	other race	N	Mar	5	5th, 6th, ...	5000		Unearne...	
5	F	67	White	German	Wid	13	Associat...	7660	Business...	Artist / p...	
6	M	51	White	Russian	Mar	17	Doctorat...	120000	Hospitals	Physician...	
7	M	20	other race	N	Nev	1	No schoo...	11000	Eating an...	Cook ear...	
8	F	77	White	Polish	Mar	5	5th, 6th, ...	2496		Unearne...	
9	F	66	White	Russian	Wid	10	High sch...	8000		Unearne...	
10	F	34	White	Polish	Nev	15	Master's ...	34150	Theaters ...	Editor/rep...	
11	F	60	White	Scottish	Mar	11	Some coll...	0			
12	M	44	White	Italian	Nev	11	Some coll...	30000	Services ...	Pest cont...	
13	F	60	White	German	Wid	10	High sch...	10000	Health se...	Nursing a...	
14	M	41	White	Russian	Nev	11	Some coll...	33001	Air trans...	Transpor...	
15	F	37	White	Israeli	Mar	10	High sch...	7270		Unearne...	
16	M	6	White	Israeli	Nev	4	1st, 2nd, ...	0			
17	F	68	White	Spanish	Div	8	11th grade	4200	Drug stor...	Supervis...	
18	F	19	White	Welsh	Nev	10	High sch...	20000	Personne...	Demonstr...	
19	F	38	White	German	Nev	14	Bachelor...	60000	Radio an...	Technicia...	
20	F	79	White	Russian	Wid	14	Bachelor...	7500		Unearne...	
21	F	32	White	Russian	Nev	9	12th grad...	32983	Theaters ...	Editor/rep...	
22	F	36	White	British	Nev	13	Associat...	60000	Apparel ...	Manager ...	
23	M	26	other race	Salvadoran	Mar	9	12th grad...	11000	Miscellan...	Janitor/cl...	
24	M	5	other race	N	Nev	1	No schoo...	0			
25	M	21	White	Russian	Nev	14	Bachelor...	0			
26	M	53	White	Irish	Nev	14	Bachelor...	42000	Furniture ...	Manager ...	

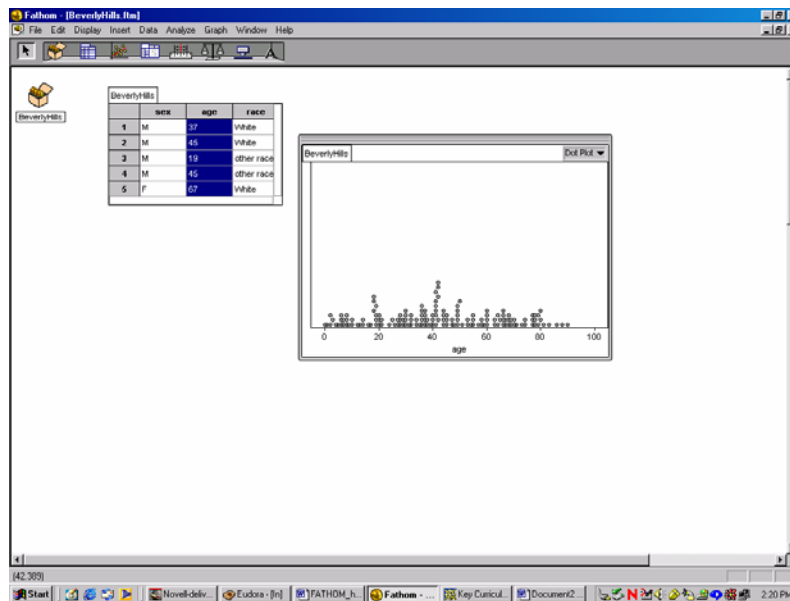
Creating a Graph

Insert a graph into the document by (1) clicking on **Insert** → **Graph** (2) pressing CTRL-G or (3) dragging a new graph into the document

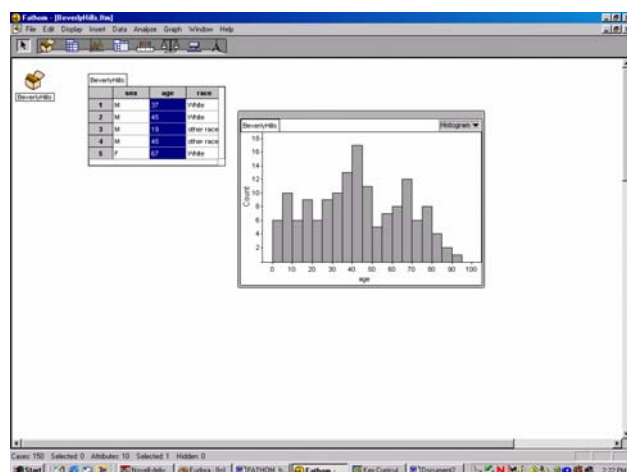
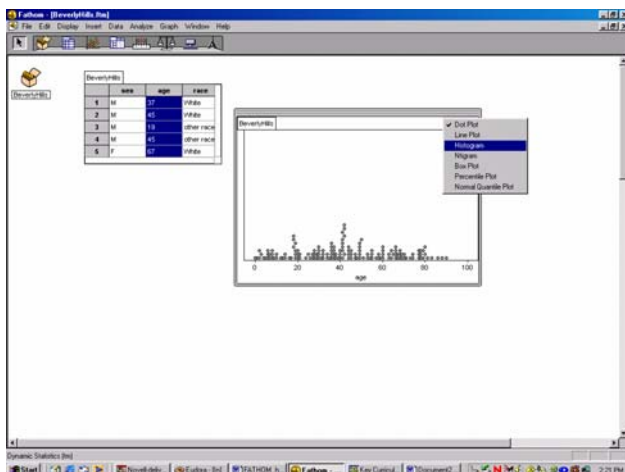
We will make a graph of the attribute **age**.

Drag the **age** attribute from the **Case Table** and drop it onto the horizontal axis of the graph, where you see the message “drop an attribute here”.

A Dot Plot of **age** will now be displayed.



This graph can be changed to a histogram by choosing Histogram from the popup menu as seen below:



Experiment with dragging other variables onto the horizontal axes of the graph e.g. sex (how many of the respondents are male? What percentage is female?), **marital** (what percentage is divorced? Never married?)

Making a Summary Table

Drag a **Summary Table** into the document. Drag the attribute **sex** onto the down-pointing arrow to obtain the first graph below. The second graph is generated by dragging the attribute **marital** onto the down arrow.

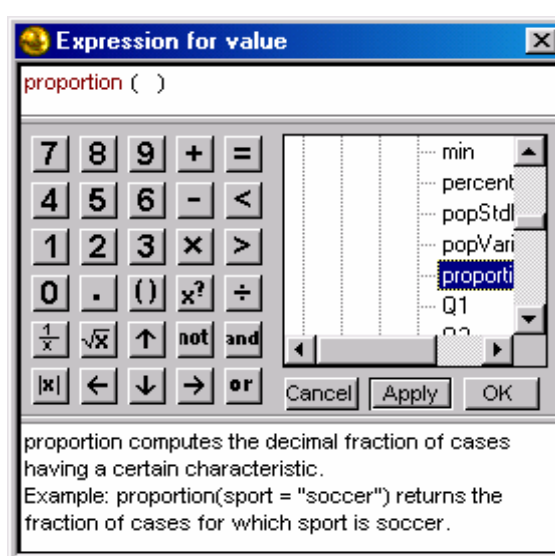
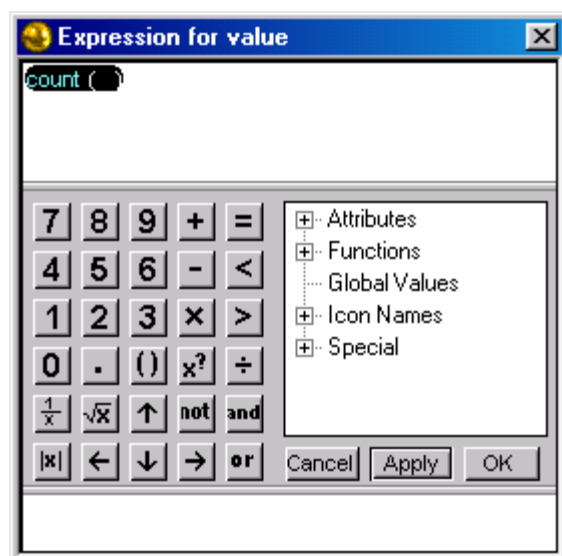
Beverly Hills		Summary Table	
↓		→	
sex	F	79	
	M	71	
Column Summary		150	
S1 = count ()			

Beverly Hills		Summary Table	
↓		→	
marital	Div	15	
	Mar	53	
	Nev	67	
	Sep	2	
	Wid	13	
Column Summary		150	

S1 = count ()

When showing a categorical variable the default display is the number of cases in each group.

Other statistics can be displayed by changing the formula. For example to display the proportion of cases in each category, double-click on the formula `S1 = count ()` to open the formula editing box. You can then edit the formula to display the proportion.



Click on OK to close the formula editor and the following results are displayed:

Beverly Hills		Summary Table	
↓	→		
marital	Div	0.1	
	Mar	0.35333333	
	Nev	0.44666667	
	Sep	0.01333333	
	Wid	0.08666667	
Column Summary 1			
S1 = proportion ()			

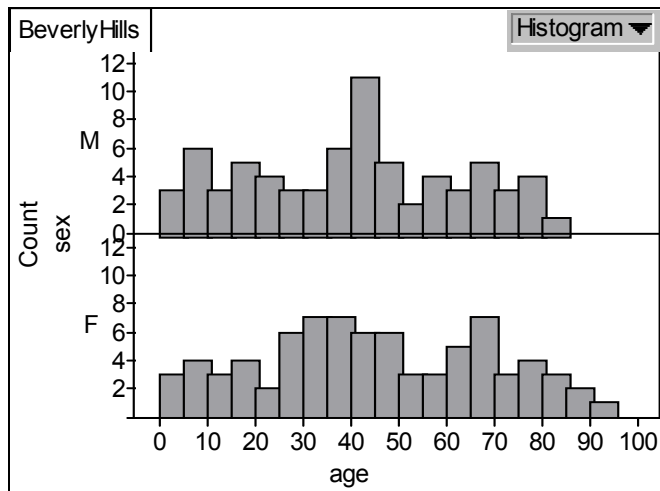
Close the **Summary Table** and open a new one. Drag the attribute **age** to the down arrow to obtain the following table.

BeverlyHills		Summary Table	
↓	⇒		
age		42.106667	
S1 = ()			

Note that for a numerical attribute the default display is the mean. We see that the mean age of the people surveyed is approximately years 42.

Splitting a graph

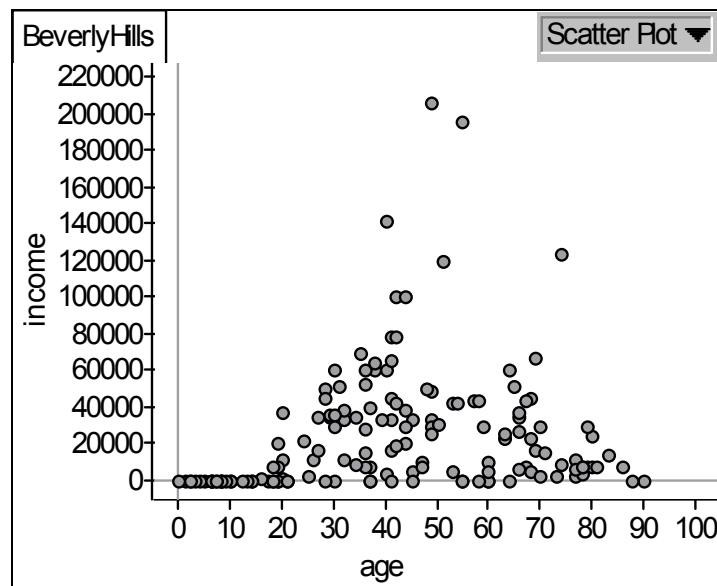
Drag a new graph into the document and drop the **age** attribute onto the horizontal axis. Change the graph to a histogram. Now drag the **sex** attribute onto the vertical axis. You will now see that the histogram of **age** has been split on the attribute **sex**.



We can now compare the distribution of age for male and female respondents.

Graphing Two Continuous Numeric Attributes

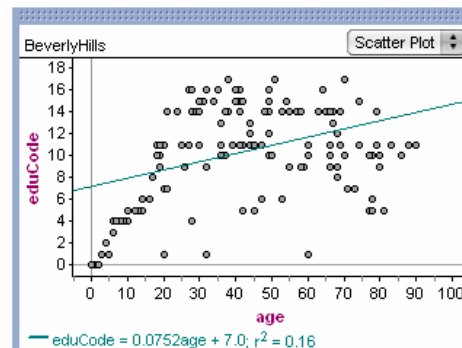
To create a graph of **income** vs **age**, drag the attribute income onto the vertical axes of the graph age is already on the horizontal axis.) The following scatter diagram will be displayed.



We note that the under 20 year olds have almost no income, the highest incomes are earned by people in the 40 – 60 age group, and incomes decrease for older people.

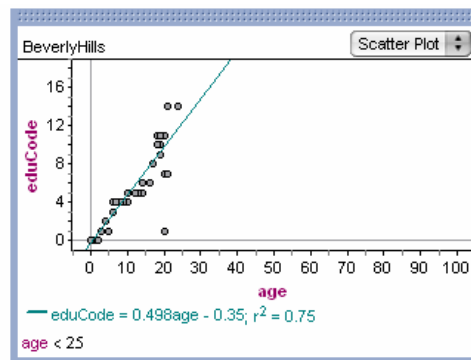
Now replace *income* on the vertical axis with *educode*. We will use the new graph to illustrate the concepts of **Outliers and Influential Observations**. A point which lies far from the line (and thus has a large residual value) is known as an *outlier*. Such points may represent erroneous data, or may indicate a poorly fitting regression line. If a point lies far from the other data in the horizontal direction, it is known as an *influential observation*. The reason for this distinction is that these points may have a significant impact on the slope of the regression line.

The next graph shows a scatter diagram of Educode on Age.



Note that the r^2 value is 0.16, implying that 16% of variation in Educode (Educational level) is explained by Age.

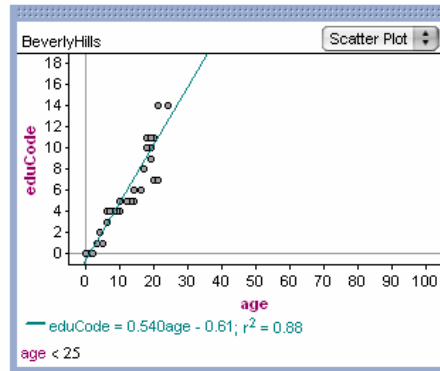
Now apply the filter *Age* < 25 to produce the following graph:



We see that in the age range 0 - 25 the r^2 value increases to $r^2 = 0.75$ (for obvious reasons!).

Notice that there is one “unusual” observation corresponding to a twenty year old male with an Educode of 1 (“no school completed”). He is working as a cook and earning \$11,000. This observation is an outlier.

When this observation is removed we see that the r^2 value increases to 0.88.



Question: How would you write up a report on this data set? Would you include the outlier and report a coefficient of determination of 75%, or analyze the data set with the outlier removed, and include an exception report in your final statement?

Contingency Tables (Cross Tabulation).

To create a contingency table of two categorical variable we drag a **Summary Table** into the document and then drop one of the attributes onto the horizontal axis, and the other onto the vertical axis. For example, the following table shows a cross-tabulation of **marital** status by **sex**.

BeverlyHills		Summary Table					
↓	sex	marital					Row Summary
		Div	Mar	Nev	Sep	Wid	
		9	23	34	0	13	
	F	9	23	34	0	13	79
	M	6	30	33	2	0	71
Column Summary		15	53	67	2	13	150

S1 = count ()

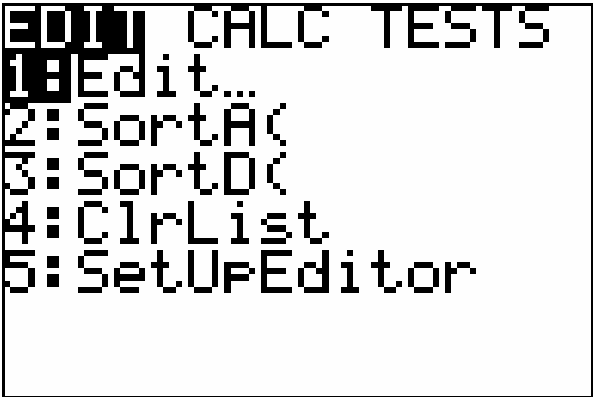
This example has introduced the basics - but there is lots more!! It is worthwhile to linger over this example for a while and experiment with other graphs and tables. For example we may wish to explore box plots and Ntigrams (for which cases are grouped into bins of equal sample size). Remember when you draw graph you can see the number (percentage) of observation in each category by moving the cursor to the specified class and looking at the values in the status bar. Observe the ability to rescale the axes by dragging.

Other things to explore

- Test hypothesis that mean age = 40
 - o Toggle **Verbose** on and off
- Establish A 95% confidence interval for mean age
- Investigate a multiple regression of Income on Age and Educodes
 - o Change order of independent variables and see effect on r^2

TI-84 Plus SE

Press <Stat>



Press <Enter> and scroll to the right.

Long Jump data is stored in L3, Year is stored in L4

L3	L4	L5	5
282.88	0.0000		
289.00	4.0000		
294.50	8.0000		
299.25	12.000		
281.50	20.000		
293.13	24.000		
304.75	28.000		
L5(1)=			

Press <Stat>, Select CALC

```
EDIT  DATA TESTS
1: 1-Var Stats
2: 2-Var Stats
3: Med-Med
4: LinReg(ax+b)
5: QuadReg
6: CubicReg
7: QuartReg
```

Select 4: LinReg(ax+b)

```
LinReg(ax+b) L4,
L3, Y1
```

Press <Enter>

```
LinReg
y=ax+b
a=.6131
b=283.4556
r2=.7575
r=.8703
```

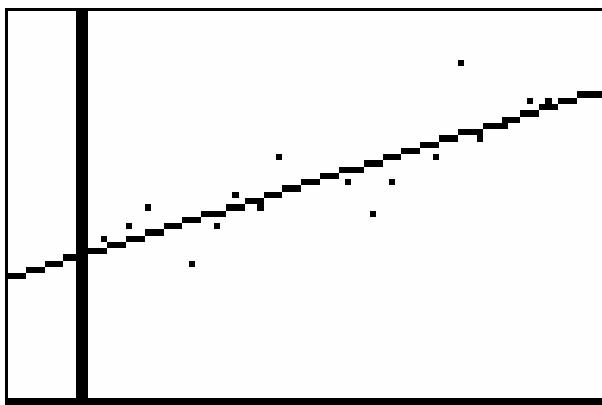
The regression equation is now stored in Var Y_1

```

Plot1 Plot2 Plot3
Y1=.6131X+283.4
556
Y2=
Y3=
Y4=
Y5=
Y6=

```

Press <GRAPH> to see the regression line:



To perform a test of hypothesis:

$H_0 : \square = 0$ vs $H_A : \square \square 0$ or $H_0 : \square = 0$ vs $H_A : \square \square 0$

Press <STAT>, highlight TESTS, and scroll down to F:LinRegTTest...

```

EDIT CALC TESTS
B: 2-PropZInt...
C:  $\chi^2$ -Test...
D:  $\chi^2$ GOF-Test...
E: 2-SampFTest...
F: LinRegTTest...
G: LinRegTInt...
H: ANOVA(

```

Complete the screen as shown below:

```

LinRegTTest
Xlist:L4
Ylist:L3
Freq:1
 $\beta$  &  $\rho$ :  $\neq$  <0 >0
RegEQ:Y2
Calculate

```

Select Calculate and press <ENTER>

```

LinRegTTest
y=a+bx
 $\beta \neq 0$  and  $\rho \neq 0$ 
t=7.2870
P=1.2700E-6
df=17.0000
a=283.4556

```

We see that the computed t-value is 7.2870 and the p-value is 1.2700E^{-6} , therefore we reject H_0 and conclude that there is a significant linear relationship between Y (Distance) and X (Year).

To construct a 95% confidence interval for β we select the test **G:LinRegTInt** and we get the following result:

```
LinRegTInt
y=a+bx
(.4356,.7906)
b=.6131
df=17.0000
s=9.7565
a=283.4556
```

The 95% confidence interval is $0.4356 \leq \beta \leq 0.7906$

Demonstration of Central Limit Theorem

Program clt.83p

(<https://www.ticalc.org/archives/files/fileinfo/99/9919.html>)

```
DEMONSTRATE
CENTRAL LIMIT
THEOREM

SAMPLE SIZE=25
```

\bar{x} is being sampled 99 times
from the uniform distrib.
Sample Size = 25
Men = .5 Variance = .0833

