



# CS 175: Project in Artificial Intelligence

Slides 4: Collaborative Filtering

# Topic 6: Collaborative Filtering

Some slides taken from Prof. Smyth  
(with slight modifications)

# Outline

- General aspects of recommender systems
- Nearest neighbor methods
- Matrix decomposition and singular value decomposition (SVD)

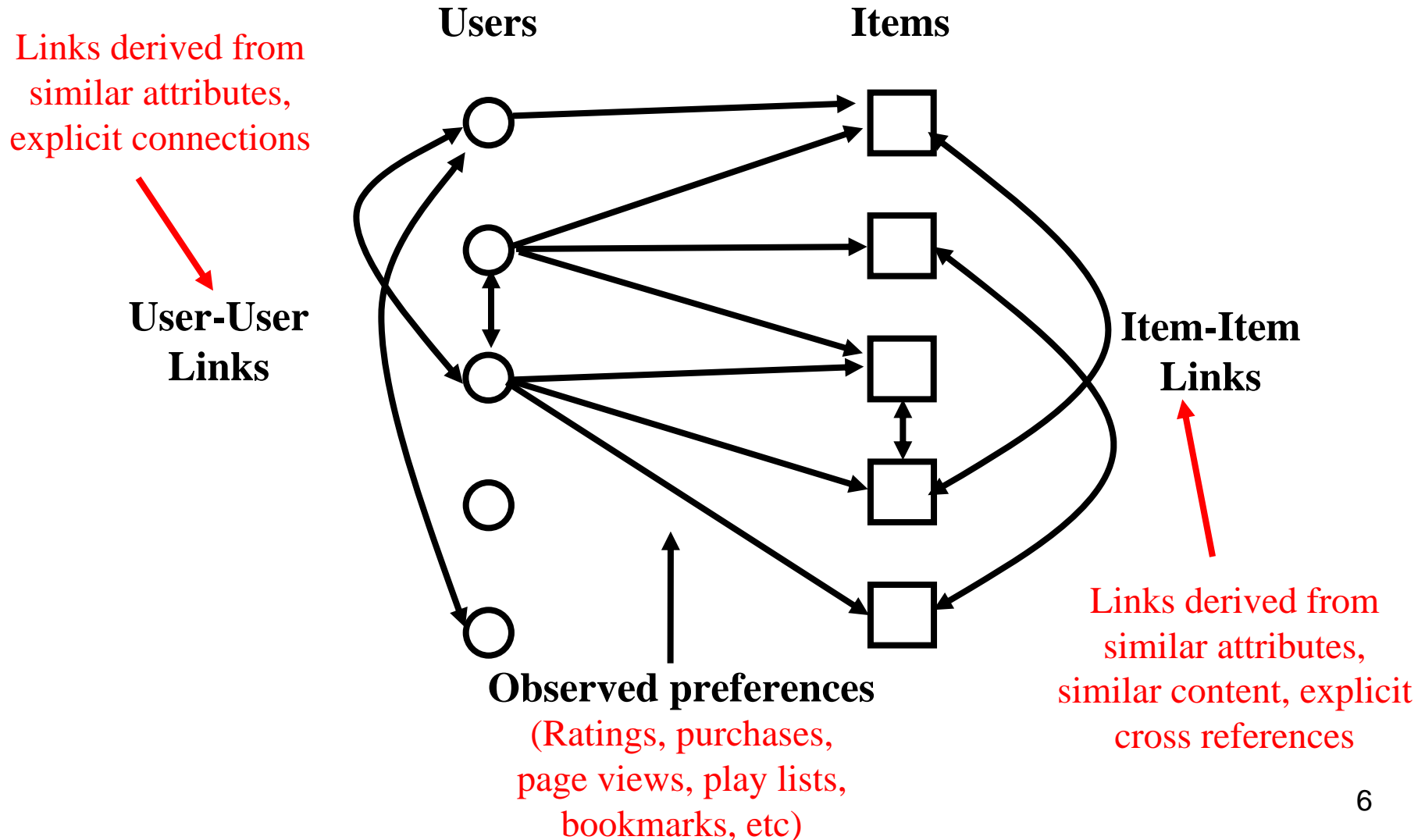
# Recommender Systems

- Ratings or Vote data =  $m \times n$  sparse binary matrix
  - $n$  columns = “products”, e.g., books for purchase or movies for viewing
  - $m$  rows = users
  - Interpretation:
    - Ratings:  $v(i,j)$  = user  $i$ ’s rating of product  $j$  (e.g. on a scale of 1 to 5)
    - Purchases:  $v(i,j) = 1$  if user  $i$  purchased product  $j$
    - entry = 0 if no purchase or rating
- Automated recommender systems
  - Given ratings or votes by a user on a subset of items, recommend other items that the user may be interested in

# Examples of Recommender Systems

- Shopping
  - Amazon.com etc
- Movie and music recommendations:
  - Netflix
  - Last.fm
- Digital library recommendations
  - CiteSeer (Popescul et al, 2001):
    - $m = 177,000$  documents
    - $N = 33,000$  users
    - Each user accessed 18 documents on average (0.01% of the database -> very sparse!)
- Web page recommendations

# The Recommender Space as a Bipartite Graph



# Different types of recommender algorithms

- Nearest-neighbor/collaborative filtering algorithms
  - Widely used – simple and intuitive
- Matrix factorization (e.g., SVD)
  - Has gained popularity recent due to Netflix competition
- Less used
  - Neural networks
  - Cluster-based algorithms
  - Probabilistic models

# Nearest-Neighbor Algorithms for Collaborative Filtering

$r_{i,k}$  = rating of user  $i$  on item  $k$

$I_i$  = items for which user  $i$  has generated a rating

Mean rating for user  $i$  is 
$$\mu_i = \frac{1}{|I_i|} \sum_{j \in I_i} r_{i,j}$$

Predicted vote for user  $i$  on item  $j$  is a weighted sum

$$r_{i,j} = \mu_i + C \sum_{k=1}^K w_{i,k} (r_{k,j} - \mu_k)$$

Normalization constant  
(e.g., total sum of weights)

weights of  $K$  similar users

Value of  $K$  can be optimized on a validation data set

# Nearest-Neighbor Weighting

- K-nearest neighbor

$$w_{i,k} = 1 \text{ if } k \in \text{neighbors}(i) \quad 0 \text{ otherwise}$$

- Pearson correlation coefficient (Resnick '94, Grouplens):

$$w_{i,k} = \rho_{i,k} = \frac{\sum_j (r_{k,j} - \mu_k)(r_{i,j} - \mu_i)}{\sqrt{\sum_j (r_{k,j} - \mu_k)^2 \sum_j (r_{i,j} - \mu_i)^2}}$$

Sums are over items rated by both users

- Can also scale weights by number of items in common

$$w'_{i,k} = \frac{n_{i,k}}{n_{i,k} + n_s} w_{i,k}$$

Smoothing constant, e.g., 10 or 100

# Comments on Neighbor-based Methods

- Here we emphasized user-user similarity
  - Can also do this with item-item similarity, i.e.,
  - Find similar items (across users) to the item we need a rating for
- Simple and intuitive
  - Easy to provide the user with explanations of recommendations
- Computational Issues
  - In theory we need to calculate all  $n^2$  pairwise weights
  - So scalability is an issue (e.g., real-time)
  - Significant engineering involved, many tricks
- For recent advances in neighbor-based approaches see  
Y. Koren, Factor in the neighbors: scalable and accurate collaborative filtering, ACM Transactions on Knowledge Discovery in Data, 2010

# NOTES ON MATRIX DECOMPOSITION AND SVD

# Matrix Decomposition

- Matrix  $D = m \times n$ 
  - e.g., Ratings matrix with  $m$  customers,  $n$  items
  - assume for simplicity that  $m > n$
- Typically
  - $R$  is sparse, e.g., less than 1% of entries have ratings
  - $n$  is large, e.g., 18000 movies
  - So finding matches to less popular items will be difficult

Idea:

compress the columns (items) into a lower-dimensional representation

# Singular Value Decomposition (SVD)

$$\begin{array}{ccccccc} \mathbf{D} & = & \mathbf{U} & \Sigma & \mathbf{V}^t \\ m \times n & & m \times n & n \times n & n \times n \end{array}$$

where:

- rows of  $\mathbf{V}^t$  are eigenvectors of  $\mathbf{D}^t\mathbf{D}$  = basis functions
- $\Sigma$  is diagonal, with  $\delta_{ii} = \text{sqrt}(\lambda_i)$  (ith eigenvalue)
- rows of  $\mathbf{U}$  are coefficients for basis functions in  $\mathbf{V}$
- (here we assumed that  $m > n$ , and  $\text{rank } \mathbf{D} = n$ )

# SVD Example

- Data [

10	20	10
2	5	2
8	17	7
9	20	10
12	22	11

# SVD Example

- Data [

10	20	10
2	5	2
8	17	7
9	20	10
12	22	11

Note the pattern in the data above: the center column values are typically about twice the 1<sup>st</sup> and 3<sup>rd</sup> column values:

⇒ So there is redundancy in the columns, i.e., the column values are correlated

# SVD Example

- Data [

10	20	10
2	5	2
8	17	7
9	20	10
12	22	11

$$D = U \Sigma V^t$$

where  $U =$ 

0.50	0.14	-0.19
0.12	-0.35	0.07
0.41	-0.54	0.66
0.49	-0.35	-0.67
0.56	0.66	0.27

where  $\Sigma =$ 

48.6	0	0
0	1.5	0
0	0	1.2

and  $V^t =$ 

0.41	0.82	0.40
0.73	-0.56	0.41
0.55	0.12	-0.82

# SVD Example

• Data [ 10 20 10  
2 5 2  
8 17 7  
9 20 10  
12 22 11

$$D = U \Sigma V^t$$

where  $U =$ 

0.50	0.14	-0.19
0.12	-0.35	0.07
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0	0	1.2

Note that first singular value is much larger than the others

and  $V^t =$ 

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0.73	-0.56	0.41
0.55	0.12	-0.82

# SVD Example

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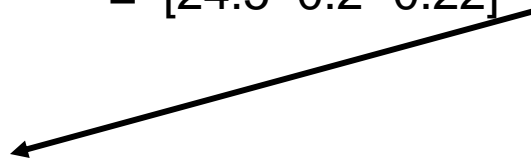
First basis function (or eigenvector) carries most of the information and it “discovers” the pattern of column dependence

# Rows in D = weighted sums of basis vectors

1<sup>st</sup> row of D = [10 20 10]

$$\begin{aligned}\text{Since } D = U S V^t, \quad \text{then } D(1,:) &= U(1,:) * \Sigma * V^t \\ &= [24.5 \quad 0.2 \quad -0.22] * V^t\end{aligned}$$

$$V^t = \begin{bmatrix} 0.41 & 0.82 & 0.40 \\ 0.73 & -0.56 & 0.41 \\ 0.55 & 0.12 & -0.82 \end{bmatrix}$$



$$\Rightarrow D(1,:) = 24.5 v_1 + 0.2 v_2 + -0.22 v_3$$

where  $v_1$ ,  $v_2$ ,  $v_3$  are rows of  $V^t$  and are our basis vectors

Thus, [24.5, 0.2, 0.22] are the weights that characterize row 1 in D

In general, the  $i$ th row of  $U^* \Sigma$  is the set of weights for the  $i$ th row in D

# Summary of SVD Representation

$$\mathbf{D} = \mathbf{U} \mathbf{\Sigma} \mathbf{V}^t$$

**Data matrix:**  
Rows = data vectors



```
graph TD; DM["Data matrix:  
Rows = data vectors"] --> D["D = U Σ V^t"]; US["U*Σ matrix:  
Rows = weights  
for the rows of D"] --> D; VT["V^t matrix:  
Rows = our basis  
functions"] --> D;
```

**$\mathbf{U} \mathbf{\Sigma}$  matrix:**  
Rows = weights  
for the rows of  $\mathbf{D}$

**$\mathbf{V}^t$  matrix:**  
Rows = our basis  
functions

# How do we compute $U$ , $\Sigma$ , and $V$ ?

- SVD decomposition is a standard eigenvector/value problem
  - The eigenvectors of  $D' D$  = the rows of  $V$
  - The eigenvectors of  $D D'$  = the columns of  $U$
  - The diagonal matrix elements in  $\Sigma$  are square roots of the eigenvalues of  $D' D$
- => finding  $U, \Sigma, V$  is equivalent to finding eigenvectors of  $D' D$ 
  - Solving eigenvalue problems is equivalent to solving a set of linear equations – time complexity is  $O(m n^2 + n^3)$

In MATLAB, we can calculate this using the `svd.m` function, i.e.,

`[u, s, v] = svd(D);`

If matrix  $D$  is non-square, we can use `svd(D,0)`

# Approximating the matrix D

- Example: we could approximate any row D just using a single weight
- Row 1:
  - Can be approximated by
$$\begin{aligned} D' &= w_1 * v_1 = 24.5 * [0.41 \ 0.82 \ 0.40] \\ &= [10.05 \ 20.09 \ 9.80] \end{aligned}$$
  - $D(1,:) = 10 \ 20 \ 10$
  - Note that this is a close approximation of the exact  $D(1,:)$   
(Similarly for any other row)
- Basis for data compression:
  - Sender and receiver agree on basis functions in advance
  - Sender then sends the receiver a small number of weights
  - Receiver then reconstructs the signal using the weights + the basis function
  - Results in far fewer bits being sent on average – trade-off is that there is some loss in the quality of the original signal

# Matrix Approximation with SVD

$$\begin{array}{ccccccc} \mathbf{D} & \approx & \mathbf{U} & \mathbf{\Sigma} & \mathbf{V}^t \\ m \times n & & m \times f & f \times f & f \times n \end{array}$$

where:

columns of  $\mathbf{V}$  are first  $f$  eigenvectors of  $\mathbf{R}^t\mathbf{R}$

$\mathbf{\Sigma}$  is diagonal with  $f$  largest eigenvalues

rows of  $\mathbf{U}$  are coefficients in reduced dimension  $\mathbf{V}$ -space

This approximation gives the best rank- $f$  approximation to matrix  $\mathbf{R}$  in a least squares sense (this is also known as principal components analysis)

# Singular Value Decomposition

- A matrix  $D$  can be decomposed:  $D = USV'$

$$\begin{array}{c} N \\ \boxed{D} \\ M \end{array} = \begin{array}{c} M \\ \boxed{U} \\ M \end{array} \begin{array}{c} N \\ \boxed{S} \\ M \end{array} \begin{array}{c} N \\ \boxed{V'} \\ N \end{array}$$

- Rank- $f$  approximation:

$$\begin{array}{c} N \\ \boxed{D} \\ M \end{array} = \begin{array}{c} F \\ \boxed{U} \\ M \end{array} \begin{array}{c} F \\ \boxed{S} \\ F \end{array} \begin{array}{c} N \\ \boxed{V'} \\ F \end{array}$$

$$\begin{array}{c} N \\ \boxed{D} \\ M \end{array} = \begin{array}{c} F \\ \boxed{A} \\ M \end{array} \begin{array}{c} N \\ \boxed{B} \\ F \end{array}$$

# Why do SVD?

- SVD provides the best f-rank approximation under the Frobenius Norm<sup>\*</sup>:

$$F(D - AB) = \sum_{m=1}^M \sum_{n=1}^N (D_{mn} - (AB)_{mn})^2.$$

- We often want to minimize (root) mean squared error for our ratings

<sup>\*</sup> Benjamin Marlin. *Collaborative Filtering: A Machine Learning Perspective*. 2004.

# Stochastic Gradient Descent

- Sometimes, matrix of ratings is too huge (i.e. Netflix is 480189 x 17770) to do full SVD
- Perform stochastic gradient descent to approximate A and B
  - Repeat until convergence:
    - Select one rating ( $D_{mn}$ ) in our training set, randomly
    - Update row 'm' in A and column 'n' in B, based on update equations

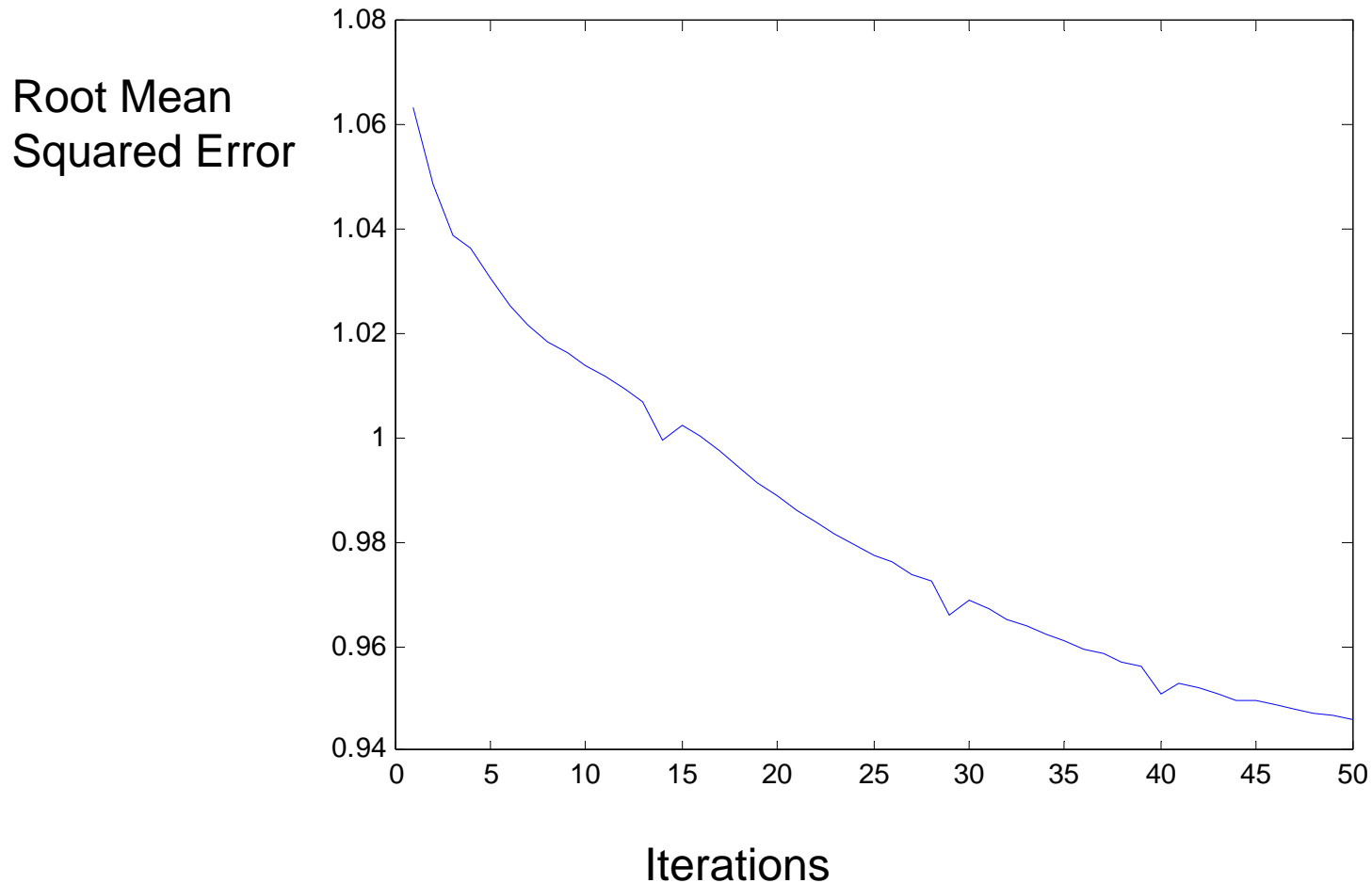
$$\frac{dF}{dA_{mf}} = -2(D_{mn} - (AB)_{mn})B_{fn}$$

$$\frac{dF}{dB_{fn}} = -2(D_{mn} - (AB)_{mn})A_{mf}$$

Exercise:  
Work out these derivatives

- Can be done efficiently in Matlab, via vectorization
  - With  $f = 300$ , can do about 600,000 iterations per minute

# Results of SVD on Netflix (f=600):



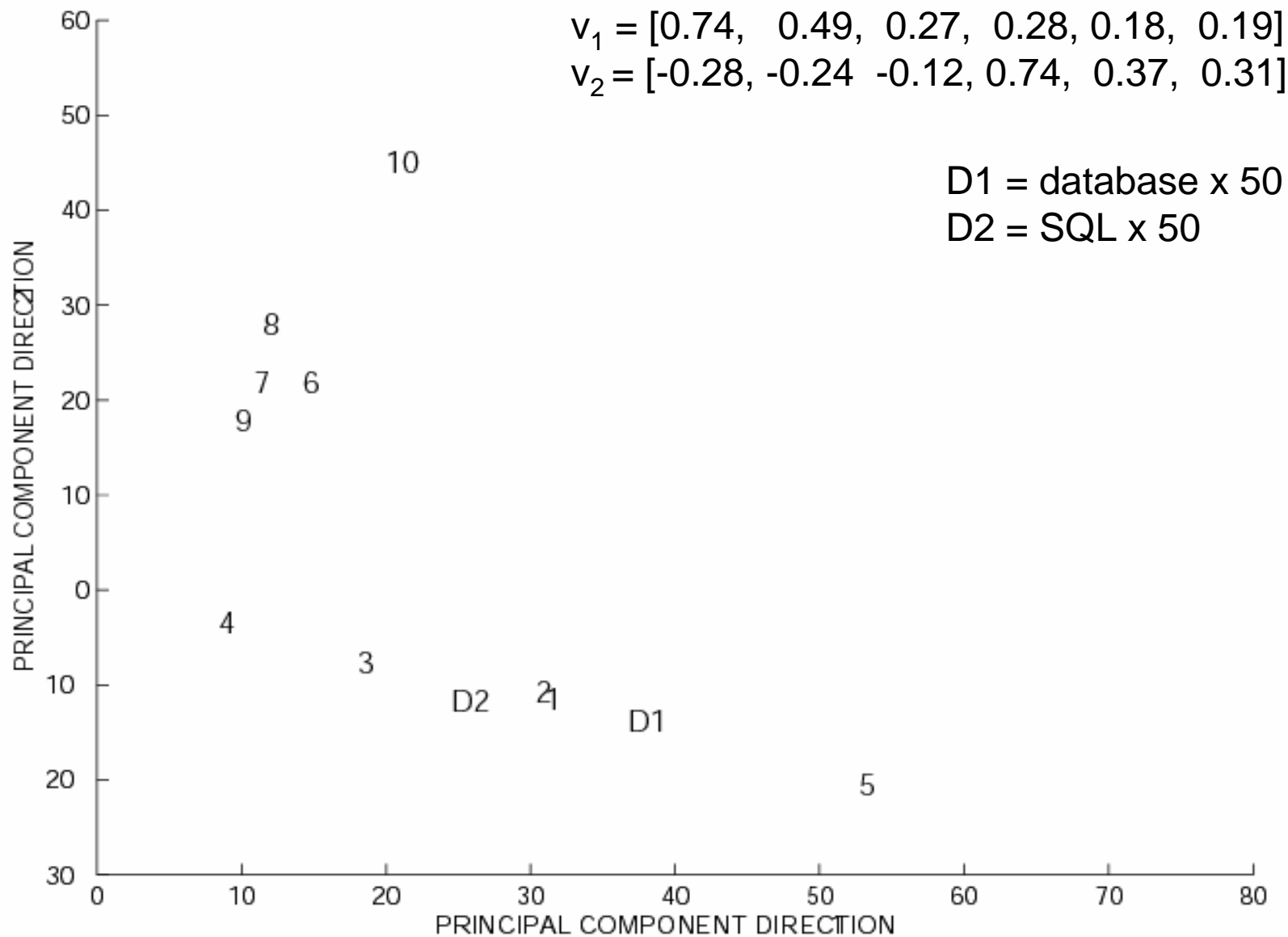
# Example: Applying SVD to a Document-Term Matrix

	database	SQL	index	regression	likelihood	linear
d1	24	21	9	0	0	3
d2	32	10	5	0	3	0
d3	12	16	5	0	0	0
d4	6	7	2	0	0	0
d5	43	31	20	0	3	0
d6	2	0	0	18	7	16
d7	0	0	1	32	12	0
d8	3	0	0	22	4	2
d9	1	0	0	34	27	25
d10	6	0	0	17	4	23

# Results of SVD with 2 factors (f=2)

	database	SQL	index	regression	likelihood	linear
d1	24	21	9	0	0	3
d2	32	10	5	0	3	0
d3	12	16	5	0	0	0
d4	6	7	2	0	0	0
d5	43	31	20	0	3	0
d6	2	0	0	18	7	16
d7	0	0	1	32	12	0
d8	3	0	0	22	4	2
d9	1	0	0	34	27	25
d10	6	0	0	17	4	23

	U1	U2
d1	30.9	-11.5
d2	30.3	-10.8
d3	18.0	-7.7
d4	8.4	-3.6
d5	52.7	-20.6
d6	14.2	21.8
d7	10.8	21.9
d8	11.5	28.0
d9	9.5	17.8
d10	19.9	45.0



# Latent Semantic Indexing

- LSI = application of SVD to document-term data
- Querying
  - Project documents into  $f$ -dimensional space
  - Project each query  $q$  into  $f$ -dimensional space
  - Find documents closest to query  $q$  in  $f$ -dimensional space
  - Often works better than matching in original high-dimensional space
- Why is this useful?
  - Query contains “automobile”, document contains “vehicle”
  - can still match  $Q$  to the document since the 2 terms will be close in  $k$ -space (but not in original space), i.e., addresses synonymy problem

# Related Ideas

- Topic Modeling
  - Can also be viewed as matrix factorization
    - Basis functions = topics
  - Topics tend to be more interpretable than LSI vectors (better suited to non-negative matrices)
  - May also perform better for document retrieval
- Non-negative Matrix Factorization

# NETFLIX: CASE STUDY

# Netflix

- Movie rentals by DVD (mail) and online (streaming)
- 100k movies, 10 million customers
- Ships 1.9 million disks to customers each day
  - 50 warehouses in the US
  - Complex logistics problem
- Employees: 2000
  - But relatively few in engineering/software
  - And only a few people working on recommender systems
- Moving towards online delivery of content
- Significant interaction of customers with Web site

# The \$1 Million Question



The screenshot shows the Netflix Prize website interface. At the top, the Netflix logo is on the left, and a yellow banner with the text "Netflix Prize" is on the right. Below the banner is a navigation bar with links: Home, Rules, Leaderboard, Register, Update, Submit, and Download. The main content area is divided into sections. On the left, there's a "Movies For You" section with a recommendation for "Randy, the following movies were chosen based on your interest in: Bowling for Columbine, Carnival: Season 1, Fahrenheit 9/11". In the center, there's a "You really liked it..." section with a "Shop as low as \$5.99" offer. On the right, there's a "Welcome!" section with a large blue text. Below the "Welcome!" section, there's a paragraph explaining the Netflix Prize: "The Netflix Prize seeks to substantially improve the accuracy of predictions about how much someone is going to love a movie based on their movie preferences. Improve it enough and you win one (or more) Prizes. Winning the Netflix Prize improves our ability to connect people to the movies they love." Below this, there's a paragraph about the rules: "Read the Rules to see what is required to win the Prizes. If you are interested in joining the quest, you should register a team." Below that, there's a paragraph about frequently asked questions: "You should also read the frequently asked questions about the Prize. And check out how various teams are doing on the Leaderboard." At the bottom of the "Welcome!" section, there's a "Good luck and thanks for helping!" message. The background of the website is a red curtain with silhouettes of two people looking at the screen. The bottom of the page has a footer with links: FAQ, Forum, and Netflix Home.

**NETFLIX**

## Netflix Prize

Home Rules Leaderboard Register Update Submit Download

**NETFLIX**

Browse Recommendations Friends Queue Buy DVDs

Home Genres New Releases Previews Netflix Top 100 Crit

### Movies For You

Randy, the following movies were chosen based on your interest in:  
[Bowling for Columbine](#)  
[Carnival: Season 1](#)  
[Fahrenheit 9/11](#)

**The Big One**  
★★★★★  
A riveting, subversive series from the mind of Michael

**Carnival: Season 2**  
★★★★★  
Disc Series

**Daniel Knapp**  
★★★★★  
A riveting, subversive series from the mind of Michael

**Read More**

**Roger & Me**  
★★★★★  
In this biographical

**You really liked it...**  
Now own it for just \$5.99  
Shop as low as \$5.99

**OT**

## Welcome!

The Netflix Prize seeks to substantially improve the accuracy of predictions about how much someone is going to love a movie based on their movie preferences. Improve it enough and you win one (or more) Prizes. Winning the Netflix Prize improves our ability to connect people to the movies they love.

Read the [Rules](#) to see what is required to win the Prizes. If you are interested in joining the quest, you should [register a team](#).

You should also read the [frequently asked questions](#) about the Prize. And check out how various teams are doing on the [Leaderboard](#).

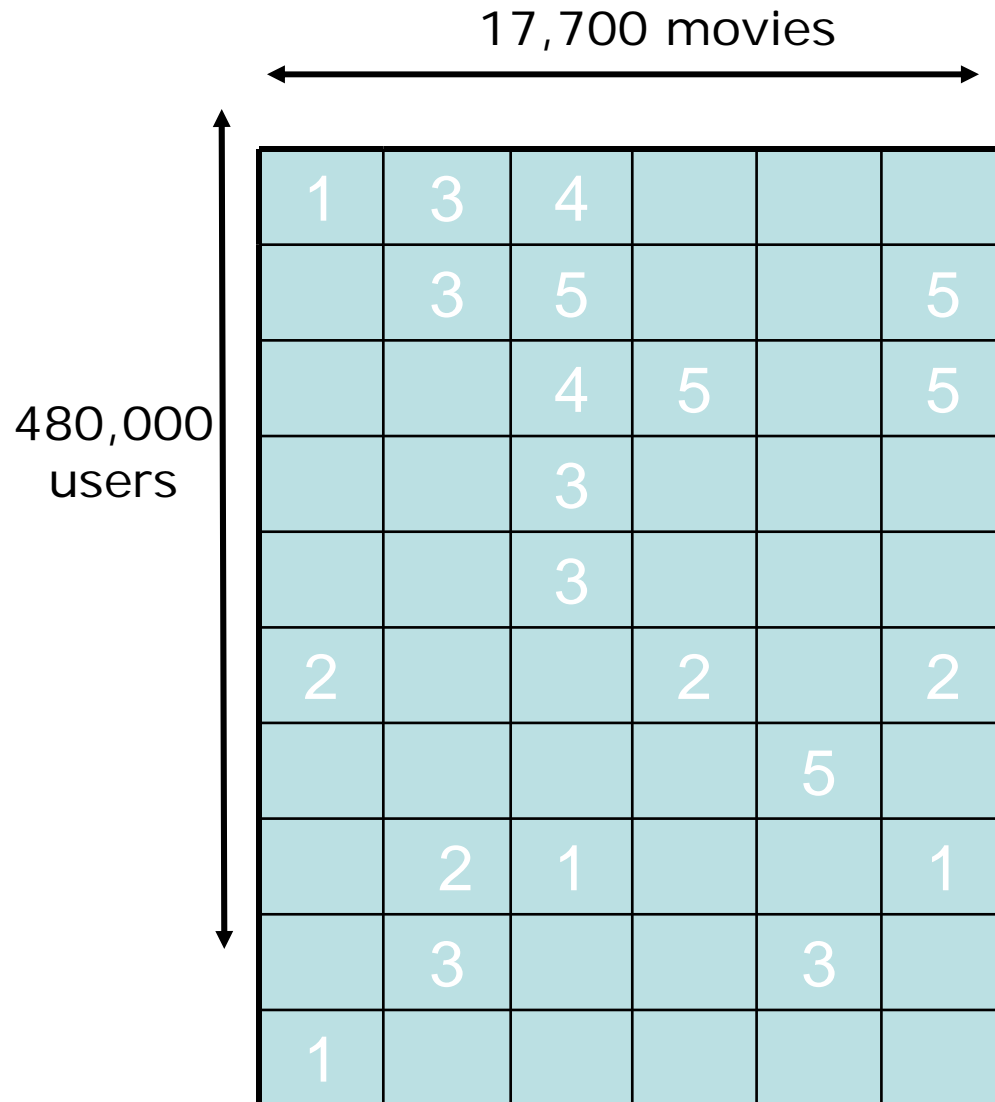
Good luck and thanks for helping!

**FAQ | Forum | Netflix Home**

# Million Dollars Awarded Sept 21<sup>st</sup> 2009



# Ratings Data



# Scoring

Minimize root mean square error (RMSE)

$$\text{Mean square error} = 1/|R| \sum_{(u,i) \in R} (r_{ui} - \hat{r}_{ui})^2$$

Does not necessarily correlate well with user satisfaction

But is a widely-used well-understood quantitative measure

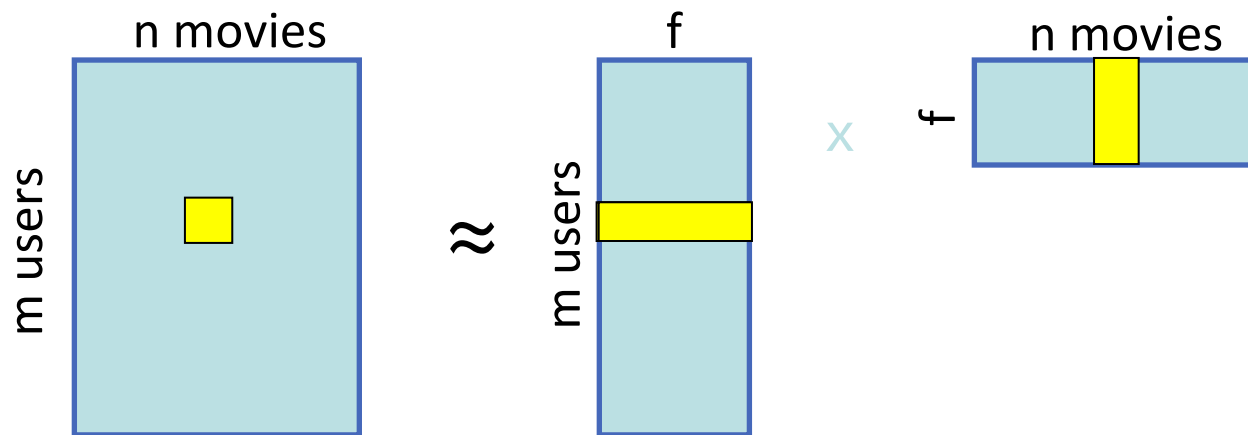
# RMSE Baseline Scores on Test Data

- 1.054 - just predict the mean user rating for each movie
- 0.953 - Netflix's own system (Cinematch) as of 2006
- 0.941 - nearest-neighbor method using correlation
- 0.857 - required 10% reduction to win \$1 million

# Why did Netflix do this?

- Customer satisfaction/retention is key to Netflix – they would really like to improve their recommender systems
- Progress with internal system (Cinematch) was slow
- Initial prize idea from CEO Reed Hastings
- \$1 million would likely easily pay for itself
- Potential downsides
  - Negative publicity (e.g., privacy)
  - No-one wins the prize (conspiracy theory)
  - The prize is won within a day or 2
  - Person-hours at Netflix to run the competition
  - Algorithmic solutions are not useful operationally

# Matrix Factorization of Ratings Data



$$r_{ui} \approx a_u^t b_i$$

$$r_{ui} \approx a_i^t b_u$$

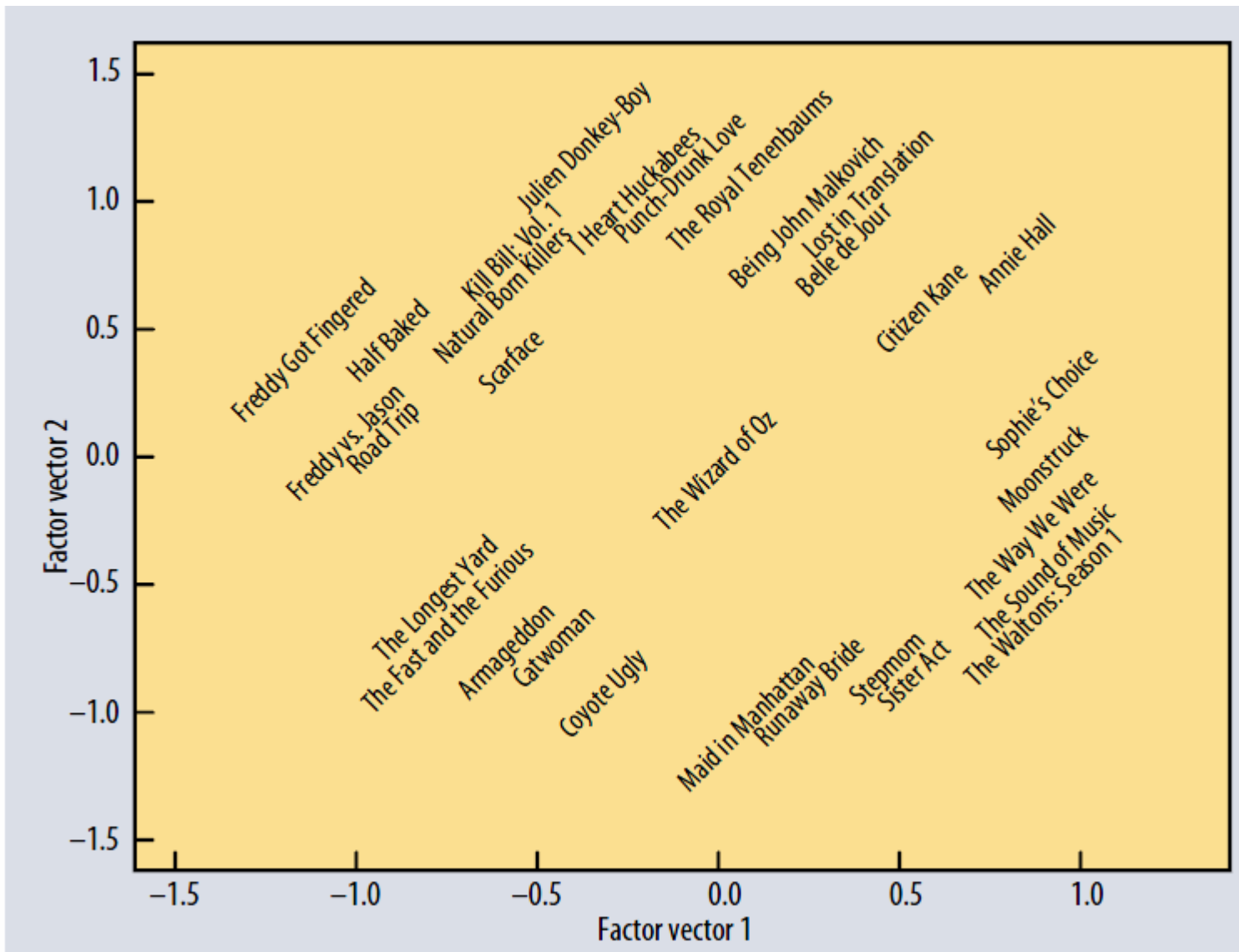


Figure from Koren, Bell, Volinsky, IEEE Computer, 2009

# Dealing with Missing Data

$$r_{ui} \approx \mathbf{a}_i^t \mathbf{b}_u$$

$$\min_{\mathbf{a}, \mathbf{b}} \sum_{(u,i) \in R} (r_{ui} - \mathbf{a}_i^t \mathbf{b}_u)^2$$



sum is only over known ratings

# Dealing with Missing Data

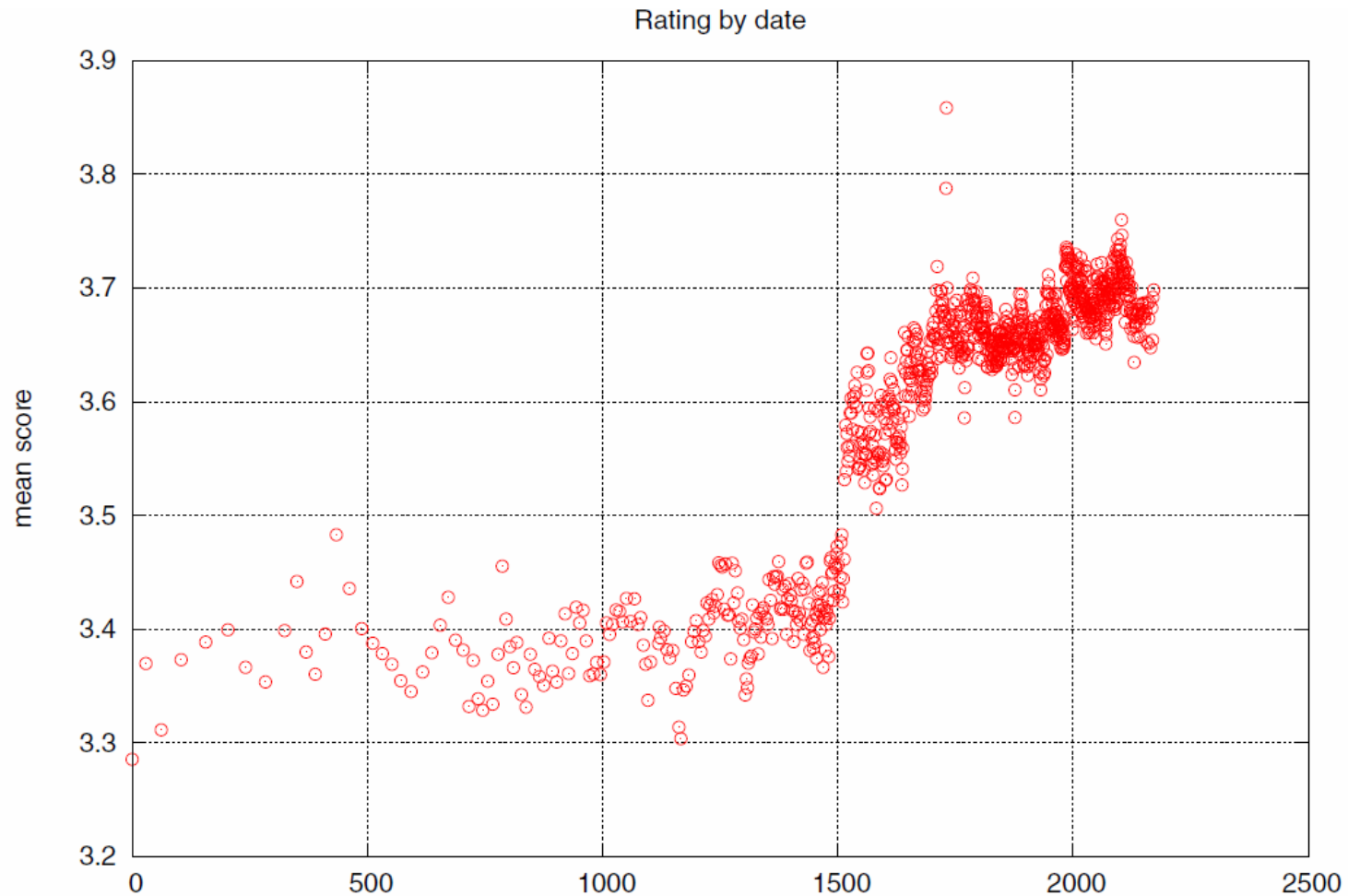
$$r_{ui} \approx a_i^t b_u$$

$$\min_{a,b} \sum_{(u,i) \in R} (r_{ui} - a_i^t b_u)^2$$

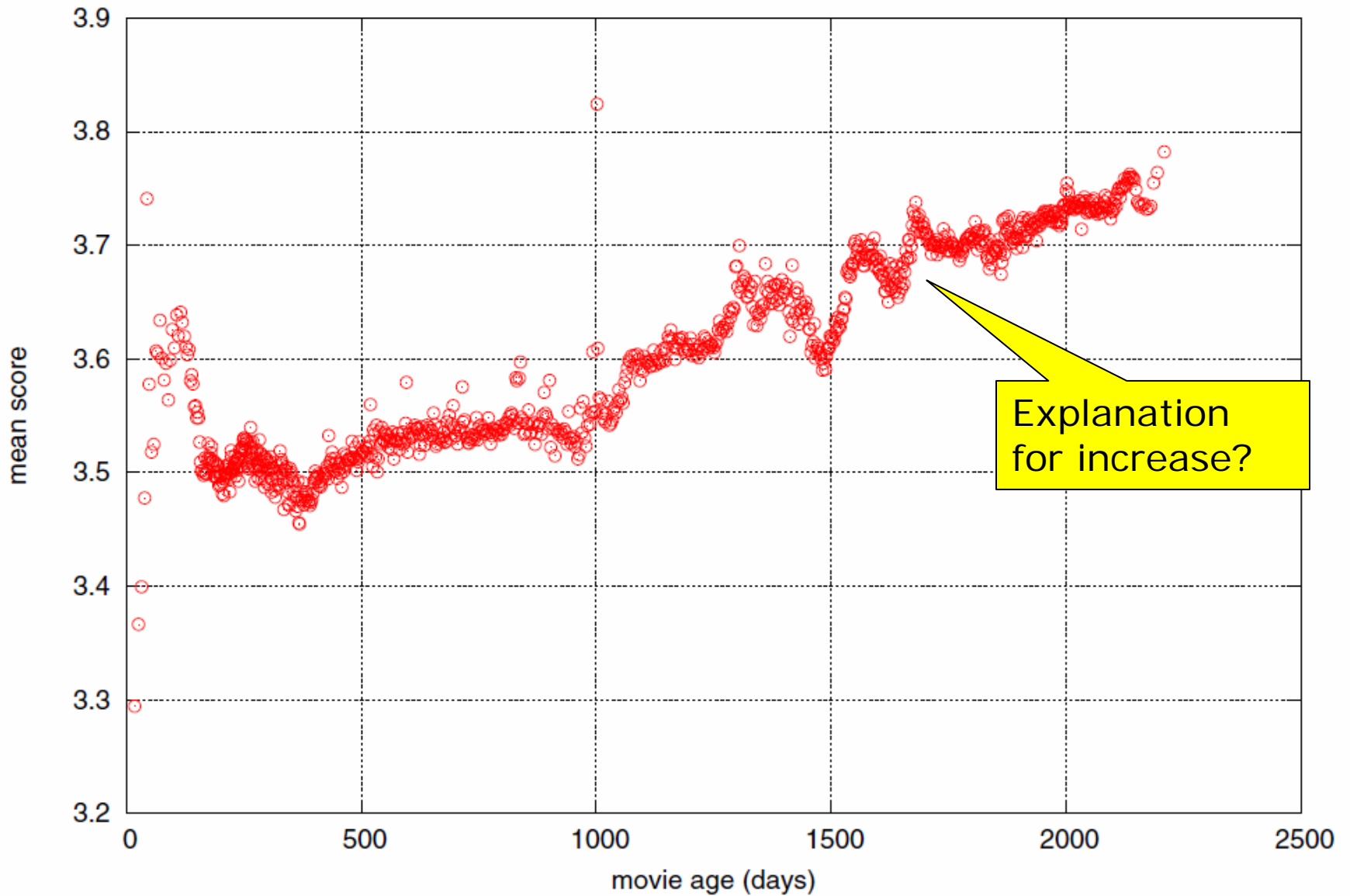
Add regularization

$$\min_{a,b} \sum_{(u,i) \in R} (r_{ui} - a_i^t b_u)^2 + \lambda (|a_i|^2 + |b_u|^2)$$

# Time effects also important



Rating by movie age

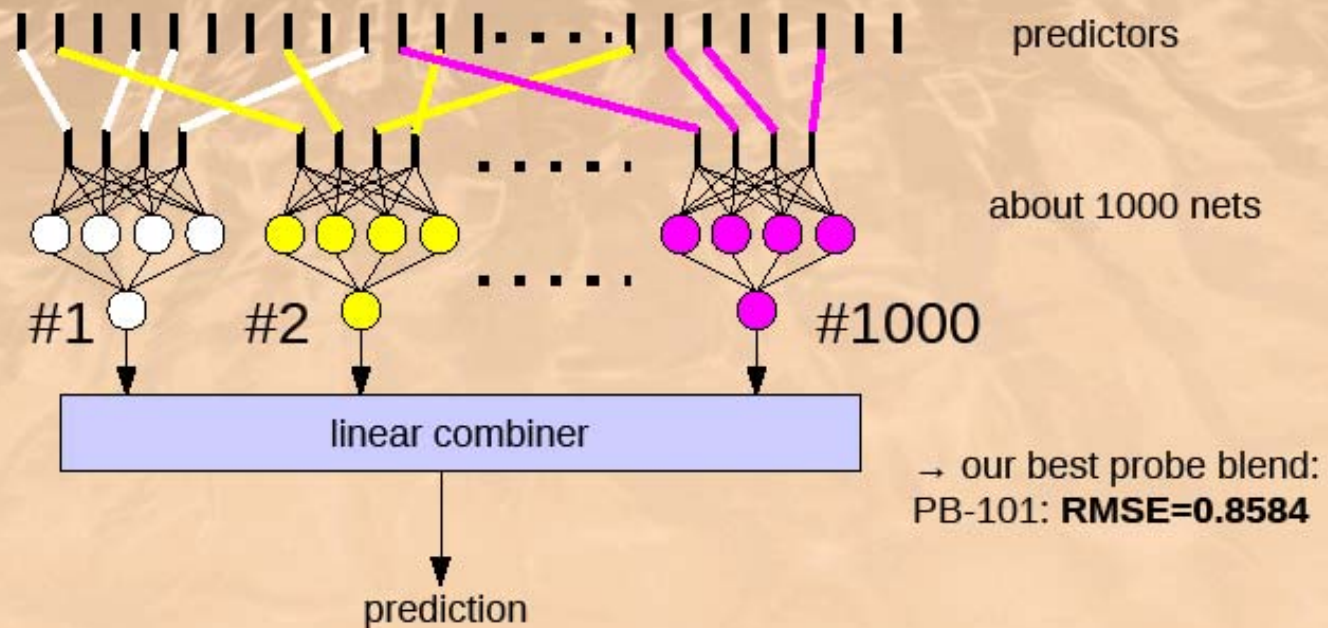


# The Kitchen Sink Approach....

- Many options for modeling
  - Variants of the ideas we have seen so far
    - Different ways to model time
    - Different ways to handle implicit information
    - Different numbers of factors
    - ....
  - Other models
    - Nearest-neighbor models
    - Restricted Boltzmann machines
- Model averaging was useful....
  - Linear model combining
  - Neural network combining
  - Gradient boosted decision tree combining
  - Note: combining weights learned on validation set (“stacking”)

# Ensemble NNBlend

- Train many small NN's (>1000) on a random subset
  - Per net: 20..40 weights
- Combine them linearly



# Other Aspects of Model Building

- Automated parameter tuning
  - Using a validation set, and grid search, various parameters such as learning rates, regularization parameters, etc., can be optimized
- Memory requirements
  - Memory: can fit within roughly 1 Gbyte of RAM
- Training time
  - Order of days: but achievable on commodity hardware rather than a supercomputer
  - Some parallelization used

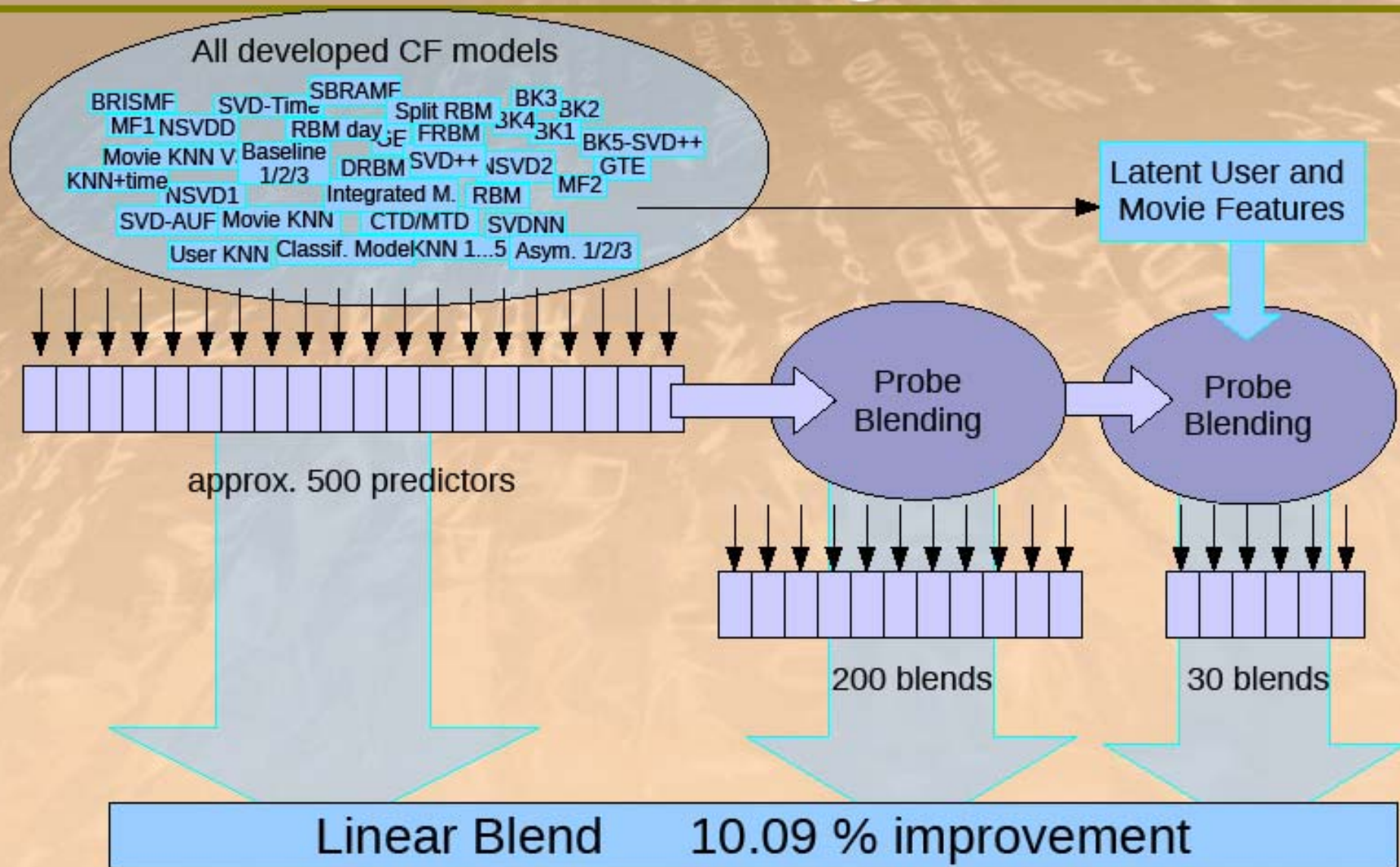
# Matrix factorization vs Near Neighbor?

From Koren, ACM Transactions on Knowledge Discovery,  
2010

“Latent factor models such as SVD face real difficulties when needed to explain predictions. ... Thus, we believe that for practical applications neighborhood models are still expected to be a common choice.”

## The big picture

# Solution of BellKor's Pragmatic Chaos



June 26<sup>th</sup> 2009: after 1000 Days and nights...

**NETFLIX**

**Netflix Prize**

Home Rules Leaderboard Register Update Submit Download

**Leaderboard**

Display top 20 leaders.

Rank	Team Name	Best Score	% Improvement	Last Submit Time
1	<a href="#">BellKor's Pragmatic Chaos</a>	0.8558	10.05	2009-06-26 18:42:37
<b>Grand Prize - RMSE <math>\leq</math> 0.8563</b>				
2	<a href="#">PragmaticTheory</a>	0.8582	9.80	2009-06-25 22:15:51
3	<a href="#">BellKor in BigChaos</a>	0.8590	9.71	2009-05-13 08:14:09
4	<a href="#">Grand Prize Team</a>	0.8593	9.68	2009-06-12 08:20:24
5	<a href="#">Dace</a>	0.8604	9.56	2009-04-22 05:57:03
6	<a href="#">BigChaos</a>	0.8613	9.47	2009-06-23 23:06:52
<b>Progress Prize 2008 - RMSE = 0.8616 - Winning Team: BellKor in BigChaos</b>				
7	<a href="#">BellKor</a>	0.8620	9.40	2009-06-24 07:16:02
8	<a href="#">Gravity</a>	0.8634	9.25	2009-04-22 18:31:32
9	<a href="#">Opera Solutions</a>	0.8638	9.21	2009-06-26 23:18:13
10	<a href="#">BruceDengDaoCiYiYou</a>	0.8638	9.21	2009-06-27 00:55:55
11	<a href="#">pengpengzhou</a>	0.8638	9.21	2009-06-27 01:06:43
12	<a href="#">xlvector</a>	0.8639	9.20	2009-06-26 13:49:04
13	<a href="#">xiangliang</a>	0.8639	9.20	2009-06-26 07:47:34
14	<a href="#">Feeds2</a>	0.8641	9.18	2009-06-26 22:51:55
15	<a href="#">Ces</a>	0.8642	9.17	2009-06-24 14:34:14

# The Leading Team

- BellKorPragmaticChaos
  - BellKor:
    - Yehuda Koren (now Yahoo!), Bob Bell, Chris Volinsky, AT&T
  - BigChaos:
    - Michael Jahrer, Andreas Toscher, 2 grad students from Austria
  - Pragmatic Theory
    - Martin Chabert, Martin Pottle, 2 engineers from Montreal (Quebec)
- June 26<sup>th</sup> submission triggers 30-day “last call”
- Submission timed purposely to coincide with vacation schedules

# The Last 30 Days

- Ensemble team formed
  - Group of other teams on leaderboard forms a new team
  - Relies on combining their models
  - Quickly also get a qualifying score over 10%
- BellKor
  - Continue to eke out small improvements in their scores
  - Realize that they are in direct competition with Ensemble
- Strategy
  - Both teams carefully monitoring the leaderboard
  - Only sure way to check for improvement is to submit a set of predictions
    - This alerts the other team of your latest score

# 24 Hours from the Deadline

- Submissions limited to 1 a day
  - So only 1 final submission could be made by either in the last 24 hours
  - team 24 hours before deadline...
  - BellKor team member in Austria notices (by chance) that Ensemble posts a score that is slightly better than BellKor's
  - Leaderboard score disappears after a few minutes (rule loophole)
- Frantic last 24 hours for both teams
  - Much computer time on final optimization
  - run times carefully calibrated to end about an hour before deadline
- Final submissions
  - BellKor submits a little early (on purpose), 40 mins before deadline
  - Ensemble submits their final entry 20 mins later
  - ....and everyone waits....

# Netflix Prize

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## Leaderboard

Display top  leaders.

Rank	Team Name	Best Score	% Improvement	Last Submit Time
1	<a href="#">The Ensemble</a>	0.8553	10.10	2009-07-26 18:38:22
2	<a href="#">BellKor's Pragmatic Chaos</a>	0.8554	10.09	2009-07-26 18:18:28

### Grand Prize - RMSE $\leq$ 0.8563

3	<a href="#">Grand Prize Team</a>	0.8571	9.91	2009-07-24 13:07:49
4	<a href="#">Opera Solutions and Vandelay United</a>	0.8573	9.89	2009-07-25 20:05:52
5	<a href="#">Vandelay Industries I</a>	0.8579	9.83	2009-07-26 02:49:53
6	<a href="#">PragmaticTheory</a>	0.8582	9.80	2009-07-12 15:09:53
7	<a href="#">BellKor in BigChaos</a>	0.8590	9.71	2009-07-26 12:57:25
8	<a href="#">Dace</a>	0.8603	9.58	2009-07-24 17:18:43
9	<a href="#">Opera Solutions</a>	0.8611	9.49	2009-07-26 18:02:08
10	<a href="#">BellKor</a>	0.8612	9.48	2009-07-26 17:19:11
11	<a href="#">BigChaos</a>	0.8613	9.47	2009-06-23 23:06:52
12	<a href="#">Feeds2</a>	0.8613	9.47	2009-07-24 20:06:46

### Progress Prize 2008 - RMSE = 0.8616 - Winning Team: BellKor in BigChaos

13	<a href="#">xiangliang</a>	0.8633	9.26	2009-07-21 02:04:40
14	<a href="#">Gravity</a>	0.8634	9.25	2009-07-26 15:58:34
15	<a href="#">Ces</a>	0.8642	9.17	2009-07-25 17:42:38
16	<a href="#">Invisible Ideas</a>	0.8644	9.14	2009-07-20 03:26:12
17	<a href="#">Just a guy in a garage</a>	0.8650	9.08	2009-07-22 14:10:42
18	<a href="#">Craig Carmichael</a>	0.8656	9.02	2009-07-25 16:00:54
19	<a href="#">J Dennis Su</a>	0.8658	9.00	2009-03-11 09:41:54
20	<a href="#">acmehill</a>	0.8659	8.99	2009-04-16 06:29:35

### Progress Prize 2002 - RMSE = 0.8712 - Winning Team: KorBell

## Training Data

100 million ratings

## Held-Out Data

3 million ratings

1.5m ratings

Quiz Set:  
scores  
posted on  
leaderboard

1.5m ratings

Test Set:  
scores  
known only  
to Netflix

Scores used in  
determining  
final winner

# Netflix Prize

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## Leaderboard

 Showing Test Score. [Click here to show quiz score](#)

 Display top  leaders.

Rank	Team Name	Best Test Score	% Improvement	Best Submit Time
<b>Grand Prize - RMSE = 0.8567 - Winning Team: BellKor's Pragmatic Chaos</b>				
1	<a href="#">BellKor's Pragmatic Chaos</a>	0.8567	10.06	2009-07-26 18:18:28
2	<a href="#">The Ensemble</a>	0.8567	10.06	2009-07-26 18:38:22
3	<a href="#">Grand Prize Team</a>	0.8582	9.90	2009-07-10 21:24:40
4	<a href="#">Opera Solutions and Vandelay United</a>	0.8588	9.84	2009-07-10 01:12:31
5	<a href="#">Vandelay Industries!</a>	0.8591	9.81	2009-07-10 00:32:20
6	<a href="#">PragmaticTheory</a>	0.8594	9.77	2009-06-24 12:06:56
7	<a href="#">BellKor in BigChaos</a>	0.8601	9.70	2009-05-13 08:14:09
8	<a href="#">Dace</a>	0.8612	9.59	2009-07-24 17:18:43
9	<a href="#">Feeds2</a>	0.8622	9.48	2009-07-12 13:11:51
10	<a href="#">BigChaos</a>	0.8623	9.47	2009-04-07 12:33:59
11	<a href="#">Opera Solutions</a>	0.8623	9.47	2009-07-24 00:34:07
12	<a href="#">BellKor</a>	0.8624	9.46	2009-07-26 17:19:11

**Progress Prize 2008 - RMSE = 0.8627 - Winning Team: BellKor in BigChaos**

13	<a href="#">xiangliang</a>	0.8642	9.27	2009-07-15 14:53:22
14	<a href="#">Gravity</a>	0.8643	9.26	2009-04-22 18:31:32
15	<a href="#">Ces</a>	0.8651	9.18	2009-06-21 19:24:53
16	Invisible Ideas	0.8653	9.15	2009-07-15 15:53:04
17	<a href="#">Just a guy in a garage</a>	0.8662	9.06	2009-05-24 10:02:54
18	<a href="#">J Dennis Su</a>	0.8666	9.02	2009-03-07 17:16:17
19	<a href="#">Craig Carmichael</a>	0.8666	9.02	2009-07-25 16:00:54
20	<a href="#">acmehill</a>	0.8668	9.00	2009-03-21 16:20:50

**Progress Prize 2007 - RMSE = 0.8723 - Winning Team: KorBell**

# Netflix Prize

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## Leaderboard

Showing Test Score. [Click here to show quiz score](#)Display top  leaders.

Rank	Team Name	Best Test Score	% Improvement	Best Submit Time
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Grand Prize - RMSE = 0.8567 - Winning Team: BellKor's Pragmatic Chaos

1	<a href="#">BellKor's Pragmatic Chaos</a>	0.8567	10.06	2009-07-26 18:18:28
2	<a href="#">The Ensemble</a>	0.8567	10.06	2009-07-26 18:38:22
3	<a href="#">Grand Prize Team</a>	0.8582	9.88	2009-07-10 21:24:40
4	<a href="#">Opera Solutions and Vandelay United</a>	0.8588	9.84	2009-07-10 01:12:31
5	<a href="#">Vandelay Industries!</a>	0.8591	9.81	2009-07-10 00:32:20
6	<a href="#">PragmaticTheory</a>	0.8594	9.77	2009-06-24 12:06:56
7	<a href="#">BellKor in BigChaos</a>	0.8601	9.70	2009-05-13 08:14:09
8	<a href="#">Dace</a>	0.8612	9.59	2009-07-24 17:18:43
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Progress Prize 2008 - RMSE = 0.8627 - Winning Team: BellKor in BigChaos

13	<a href="#">xiangliang</a>	0.8642	9.27	2009-07-15 14:53:22
14	<a href="#">Gravity</a>	0.8643	9.26	2009-04-22 18:31:32
15	<a href="#">Ces</a>	0.8651	9.18	2009-06-21 19:24:53
16	Invisible Ideas	0.8653	9.15	2009-07-15 15:53:04
17	<a href="#">Just a guy in a garage</a>	0.8662	9.06	2009-05-24 10:02:54
18	<a href="#">J Dennis Su</a>	0.8666	9.02	2009-03-07 17:16:17
19	<a href="#">Craig Carmichael</a>	0.8666	9.02	2009-07-25 16:00:54
20	<a href="#">acmehill</a>	0.8668	9.00	2009-03-21 16:20:50

Progress Prize 2007 - RMSE = 0.8723 - Winning Team: KorBell

# Million Dollars Awarded Sept 21<sup>st</sup> 2009



# Lessons Learned

- Scalability is important
  - e.g., stochastic gradient descent on sparse matrices
- Latent factor models work well on this problem
  - Previously had not been explored for recommender systems
- Understanding your data is important, e.g., time-effects
- Combining models works surprisingly well
  - But final 10% improvement can probably be achieved by judiciously combining about 10 models rather than 1000's
  - This is likely what Netflix will do in practice
- Surprising amount of collaboration among participants

## Netflix Competitors Learn the Power of Teamwork

By STEVE LOHR

Published: July 27, 2009

A contest set up by [Netflix](#), which offered a [\\$1 million prize](#) to anyone who could significantly improve its movie recommendation system, ended on Sunday with two teams in a virtual dead heat, and no winner to be declared until September.

[Enlarge This Image](#)



Ozier Muhammad/The New York Times

Chris Volinsky, a scientist at AT&T Research, left, is on a high-ranking team in a Netflix contest. With him is Robert Bell.

But the contest, which began in October 2006, has already produced an impressive legacy. It has shaped careers, spawned at least one start-up company and inspired research papers. It has also changed conventional wisdom about the best way to build the automated systems that increasingly help people make online choices about movies, books, clothing, restaurants, news and other goods and services.

These so-called recommendation engines are computing models that predict what a person might enjoy based on statistical scoring of that person's stated preferences, past consumption patterns and similar choices made by many others — all made possible by the ease of data collection and tracking on the Web.

### Related

[The Screens Issue: If You Liked This, You're Sure to Love That](#)  
(November 23, 2008)

Times Topics: [Netflix Inc.](#)

# Why Collaboration?

## Openness of competition structure

- Rules stated that winning solutions would be published
  - Non-exclusive license of winning software to Netflix
  - “Description of algorithm to be posted on site”
- Research workshops sponsored by Netflix
- Leaderboard was publicly visible: “it was addictive....”

# Netflix Prize

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## Netflix Prize: Forum

Forum for discussion about the Netflix Prize and dataset.

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You are not logged in.

### Announcement

**Congratulations to team "BellKor's Pragmatic Chaos" for being [awarded the \\$1M Grand Prize](#) on September 21, 2009. Stay tuned for details of the next contest, [Netflix Prize 2](#).**

### Administrivia

Forum	Topics	Posts	Last post
<a href="#">Important Announcements</a>	5	151	<a href="#">Today 04:29:38</a> by YehudaKoren
<a href="#">Registration Problems</a>	1	1	<a href="#">2006-10-05 08:37:53</a> by prizemaster
<a href="#">Administrivia</a> Administrative notes from the maintainers	3	43	<a href="#">2009-06-22 09:23:04</a> by dale5351
<a href="#">Prize and Forum FAQ</a>	15	18	<a href="#">2009-03-24 10:18:36</a> by prizemaster
<a href="#">Request for new Category or Forum</a> Want to add a new high-level Category or Forum? This is the place to ask or comment.	18	40	<a href="#">2008-04-29 20:50:19</a> by filmmakershelp

### Awarded Prizes

Forum	Topics	Posts	Last post
<a href="#">Grand Prize</a>	1	14	<a href="#">2009-10-09 12:18:23</a> by statistician
<a href="#">Progress Prize 2008</a>	2	17	<a href="#">2009-03-18 02:40:53</a> by CS1
<a href="#">Progress Prize 2007</a>	5	29	<a href="#">2008-10-06 06:51:51</a> by dinc3r

### Questions (and answers)

Forum	Topics	Posts	Last post
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# Why Collaboration?

## Development of Online Community

- Active Netflix prize forum + other blogs
- Quickly acquired “buzz”
- Forum was well-moderated by Netflix
- Attracted discussion from novices and experts alike
- Early posting of code and solutions
- Early self-identification (links via leaderboard)

# Why Collaboration?

## Academic/Research Culture

- Nature of competition was technical/mathematical
- Attracted students, hobbyists, researchers
- Many motivated by fundamental interest in producing better algorithms - \$1 million would be a nice bonus
- History in academic circles of being open, publishing, sharing

# Questions

- Does reduction in squared error metric correlate with real improvements in user satisfaction?
- Are these competitions good for scientific research?
  - Should researchers be solving other more important problems?
- Are competitions a good strategy for companies?

# Evaluation Methods

- Research papers use historical data to evaluate and compare different recommender algorithms
  - predictions typically made on items whose ratings are known
  - e.g., leave-1-out method,
    - each positive vote for each user in a test data set is in turn “left out”
    - predictions on left-out items made given rated items
  - e.g., predict-given-k method
    - Make predictions on rated items given  $k=1$ ,  $k=5$ ,  $k=20$  ratings
  - See Herlocker et al (2004) for detailed discussion of evaluation
- Approach 1: measure quality of rankings
  - Score = weighted sum of true votes in top 10 predicted items
- Approach 2: directly measure prediction accuracy
  - Mean-absolute-error (MAE) between predictions and actual votes
  - Typical MAE on large data sets ~ 20% (normalized)
    - E.g., on a 5-point scale predictions are within 1 point on average

# Evaluation with (Implicit) Binary Purchase Data

- Cautionary note:
  - It is not clear that prediction on historical data is a meaningful way to evaluate recommender algorithms, especially for purchasing
  - Consider:
    - User purchases products A, B, C
    - Algorithm ranks C highly given A and B, gets a good score
    - However, what if the user would have purchased C anyway, i.e., making this recommendation would have had no impact? (or possibly a negative impact!)
  - What we would really like to do is reward recommender algorithms that lead the user to purchase products that they would not have purchased without the recommendation
    - This can't be done based on historical data alone
  - Requires direct “live” experiments (which is often how companies evaluate recommender algorithms)